

# Following the Multicomponent Phase Diagram to the Origin of the Moon



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# Acknowledgements

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## References

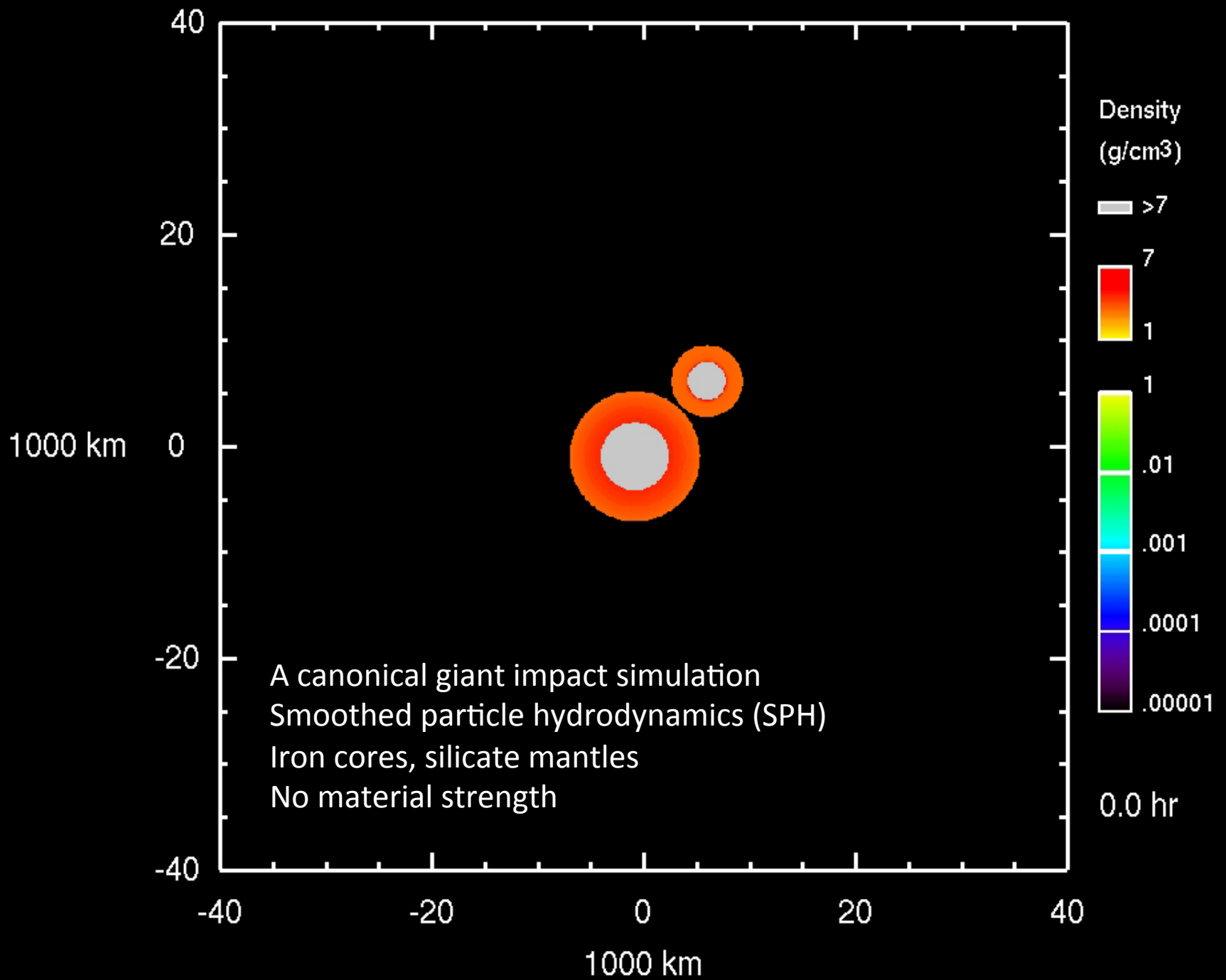
Simon J. Lock & Sarah T. Stewart, The structure of terrestrial bodies: Impact heating, corotation limits and synestias, J. Geophysical Research Planets, in press

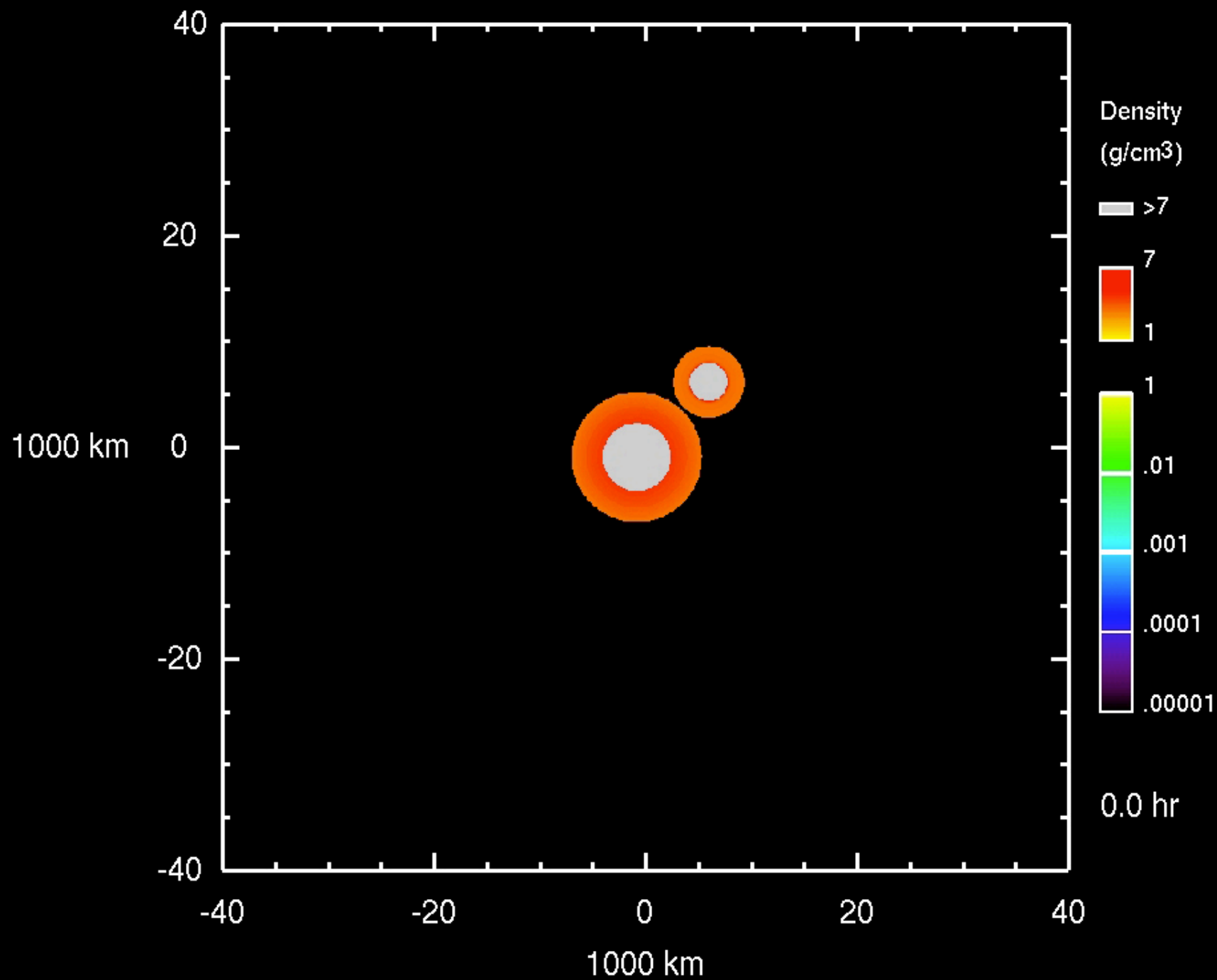
Simon J. Lock, Sarah T. Stewart, Michail I. Petaev, Zöe M. Leinhardt, Mia T. Mace, Stein B. Jacobsen, Matija Cuk, The origin of the Moon within a terrestrial synestia, J. Geophysical Research Planets, submitted

# The Giant Impact Hypothesis for Lunar Origin



Hartmann & Davis 1975  
Ward & Cameron 1976





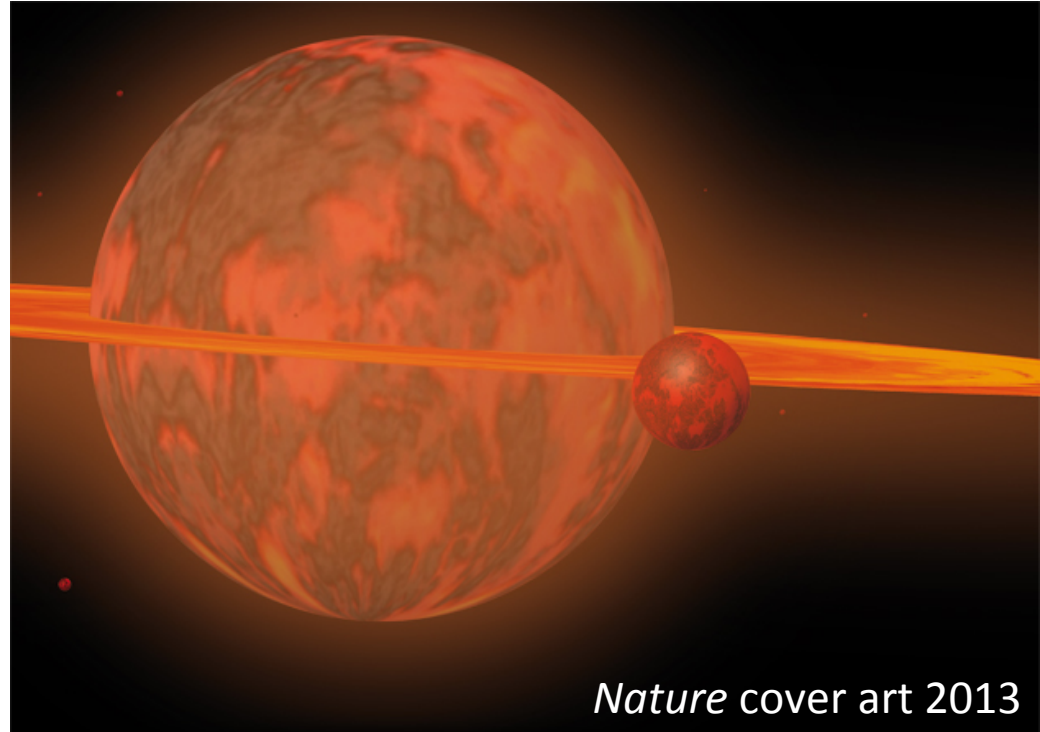
# Lunar Accretion from a Circumterrestrial Disk

Calculated moons are small.  
Hard to make lunar mass  
satellite from mixed phase  
disk.

(Salmon & Canup 2012, 2014)

Poorly understood physics in  
a vapor-rich disk.

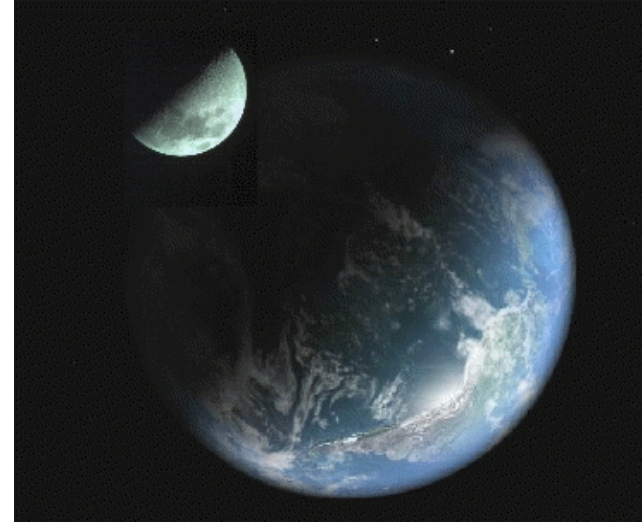
(Charnoz & Michaut 2015)



Misleading artist drawing!!

**Disk is made mostly of impactor material.**

# Earth and Moon are Isotopic Twins



(Nearly) Identical Isotopes

O volatile, large variations in solar nebula

Ti refractory, nucleosynthetic anomalies

Cr radiogenic (3.7 Ma), variations in nebula

H volatile, large variations in solar nebula

Si moderately refractory, core formation

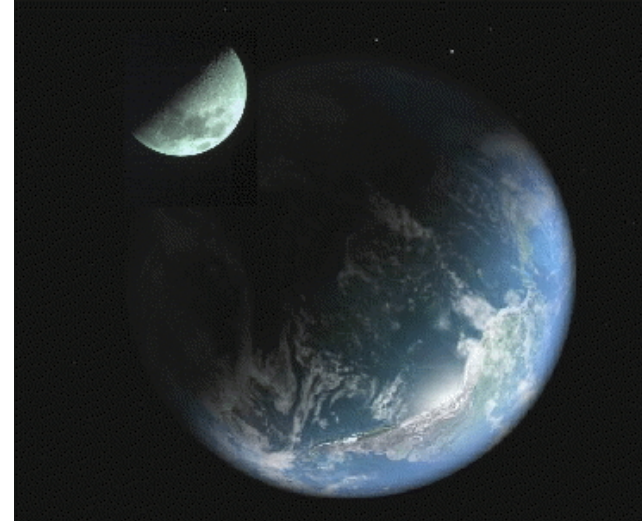
W radiogenic (8.9 Ma), core formation

**Each planetary body has a different isotopic thumbprint\*.**

Lugmair & Shukolyukov 1998, Wiechert et al. 2001, Georg et al. 2007, Zhang et al. 2011, Saal et al. 2013

W: Touboul et al. 2015, Kruijer et al. 2015 \*Dauphas et al. 2014, Dauphas 2017

# Earth and Moon are Isotopic Twins



(Nearly) Identical Isotopes

O volatile, large variations in solar nebula

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W radiogenic (8.9 Ma), core formation

**Minimalist interpretation:**

**Earth and the Moon are derived from the same material.**



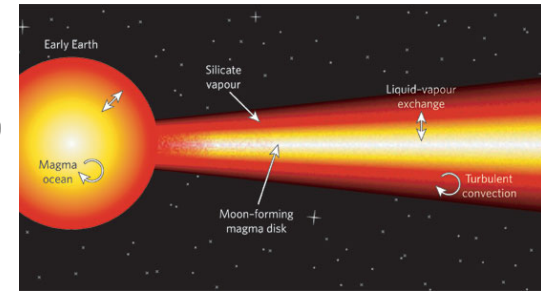
# Giant Impact Hypothesis in Crisis: Proposed Solutions

1. Impactor had same isotopes  
(Dauphas et al. 2014 but Dauphas 2017)

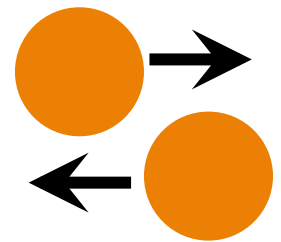
Enstatite  
chondrites



2. Mix after the impact  
(Pahlevan & Stevenson 2007 but Melosh 2014)



3. Mix during the impact  
with high angular momentum events  
(Ćuk & Stewart 2012; Canup 2012 but too special?)



4. The giant impact hypothesis is wrong  
(includes multiple moon hypothesis, Rufu et al. 2017)



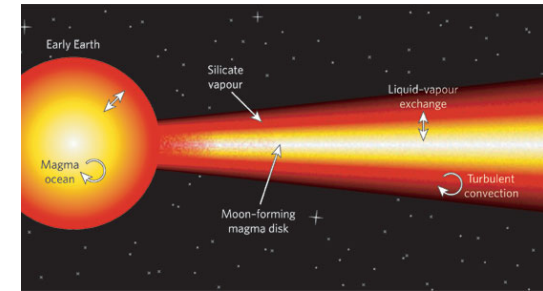
# Giant Impact Hypothesis in Crisis: New Solution (Lock et al., in review)

1. Impactor had same isotopes

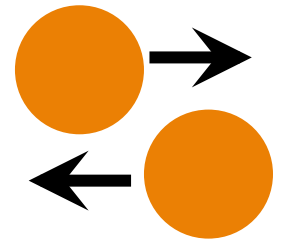
Enstatite  
chondrites



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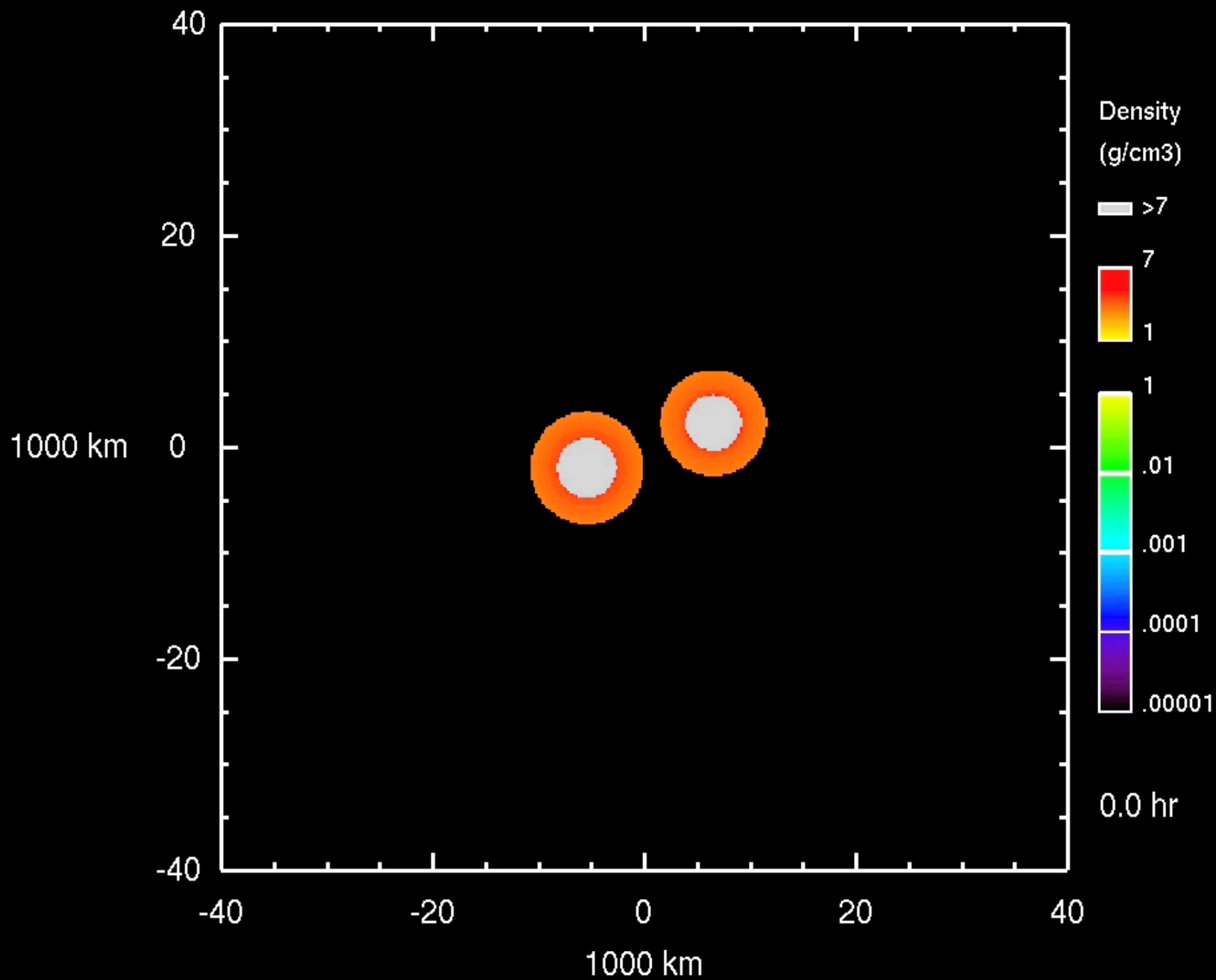
4. The giant impact hypothesis is wrong

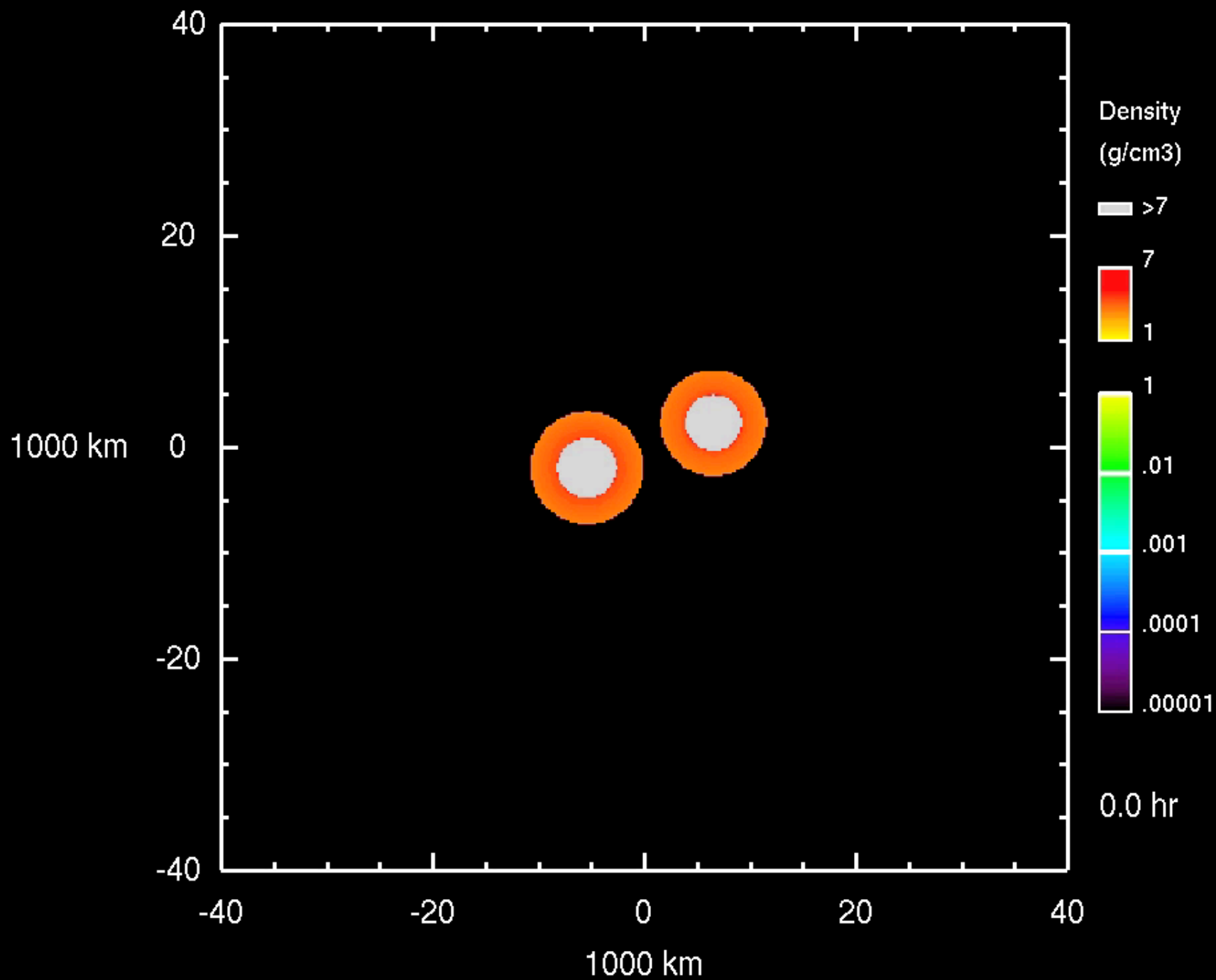


# A High-Energy, High-Angular-Momentum Giant Impact Makes a Hot, Fast-spinning Structure



What does it look like?





# The Structure of Hot, Spinning Rocky Planets

## Numerically solve for the structure

### GADGET2 SPH code

Initialize planets with  
mass of mantle, core  
constant entropy mantle  
total ang. momentum

Solve for equilibrium  
size and shape

Code modified for tabulated EOS  
iron MANEOS core  
forsterite MANEOS mantle

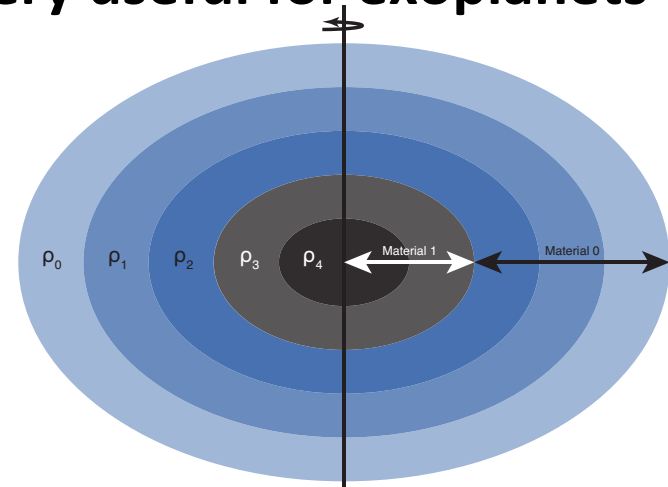
### New HERCULES code

Concentric constant density layers  
Iteratively solve for equipotential  
surfaces

Conserve AM, mass

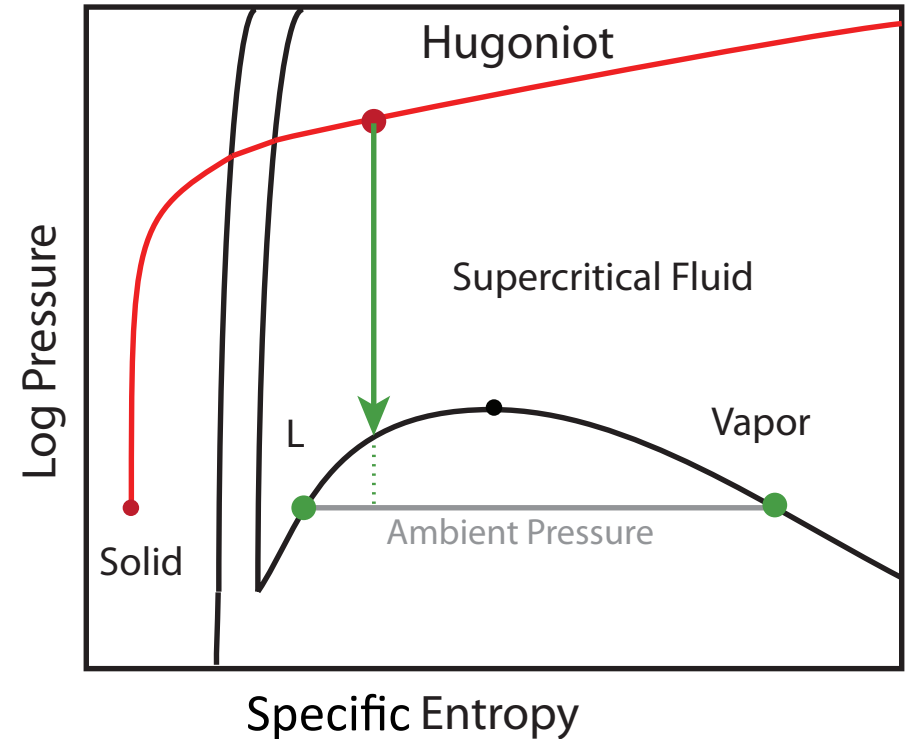
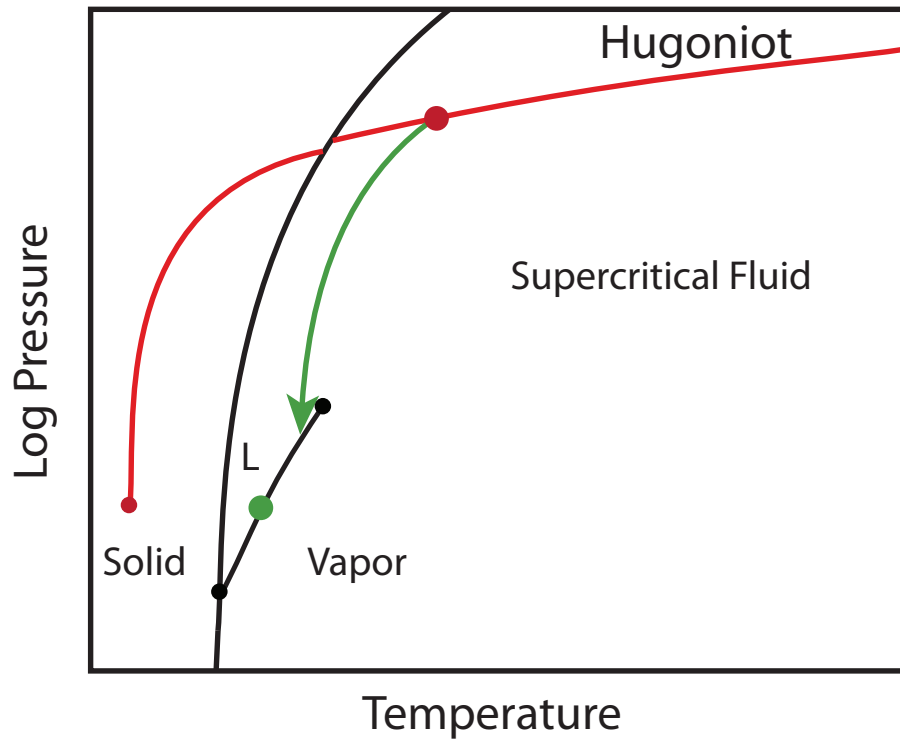
Expanded Hubbard 2013

**Very useful for exoplanets**



# The Structure of Hot, Spinning Rocky Planets

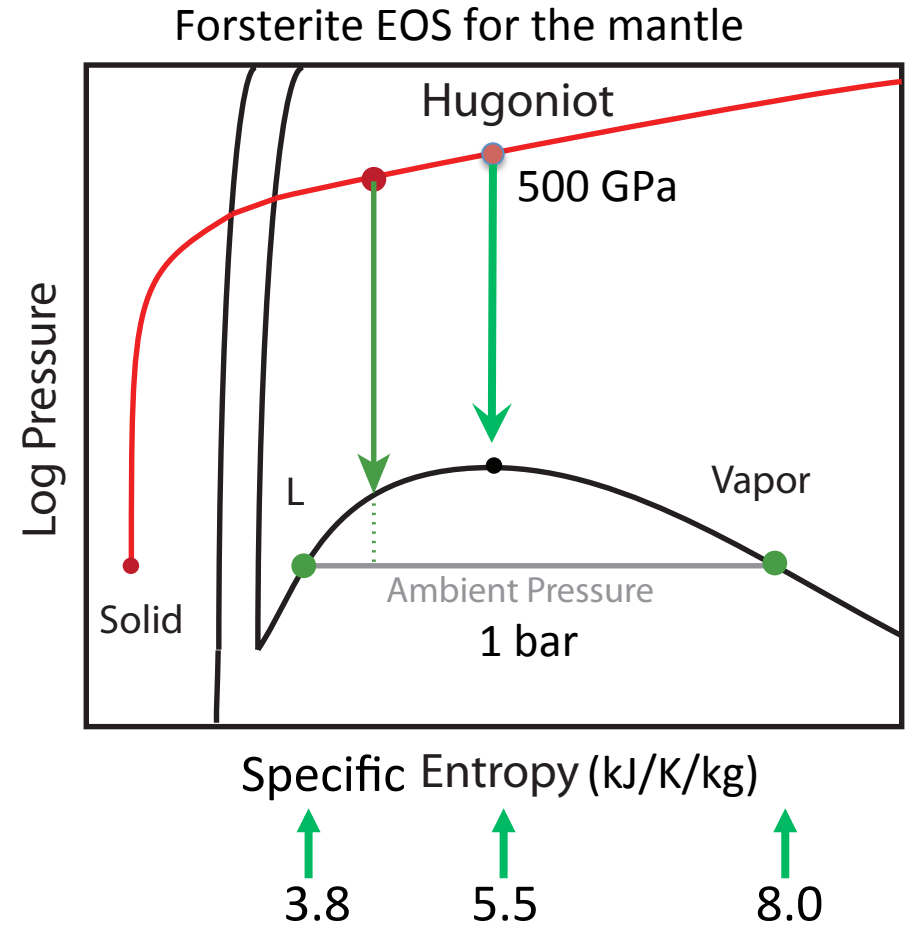
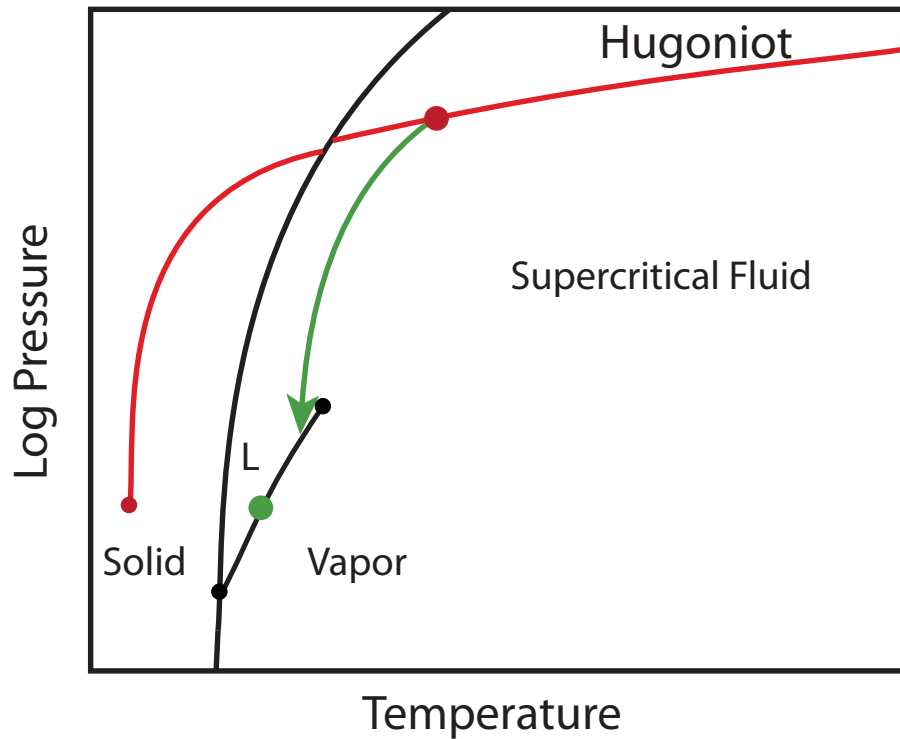
## Thermodynamics



Specific entropy used to designate thermal state.

# The Structure of Hot, Spinning Rocky Planets

## Thermodynamics

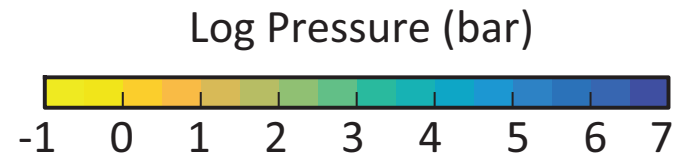


Specific entropy of outer layer of post-impact body is determined by the energy of the impact

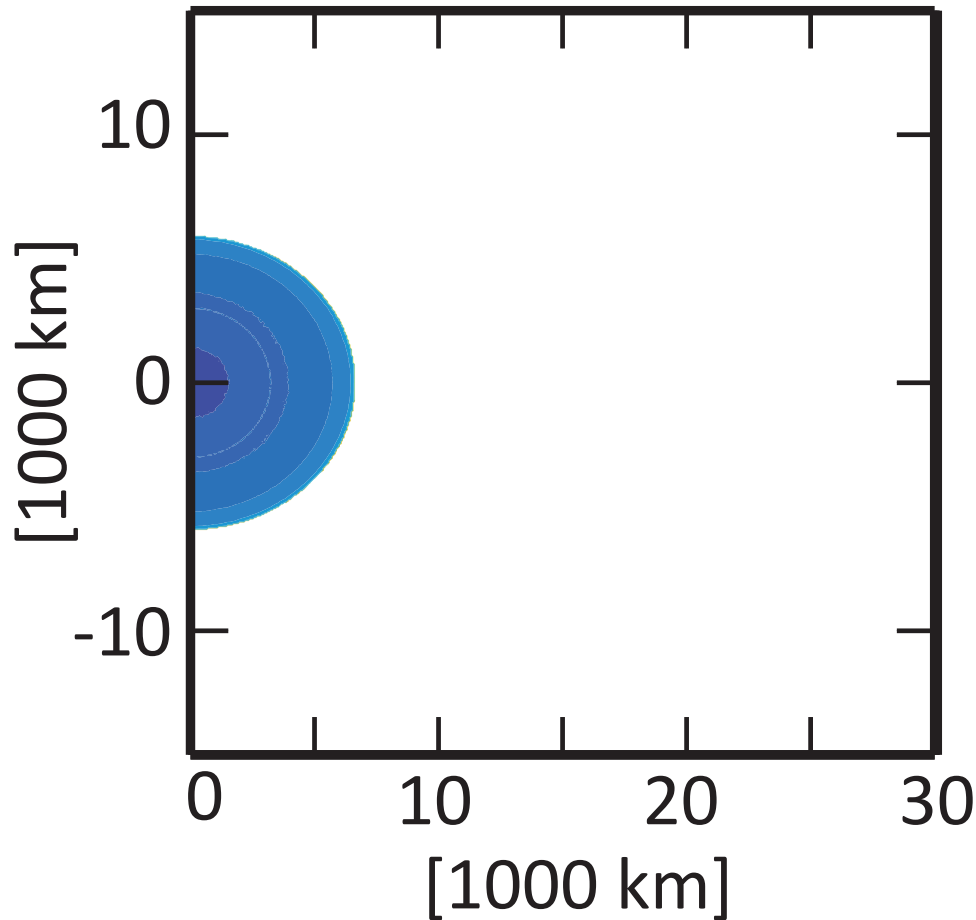


# Increasing Entropy

$1 M_{\text{Earth}}$ , Ang. Mom. =  $1 L_{\text{Earth-Moon}}$

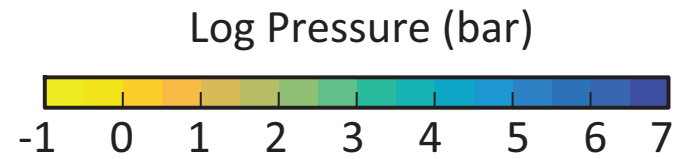


Sp. Entropy 4.0 kJ/K/kg

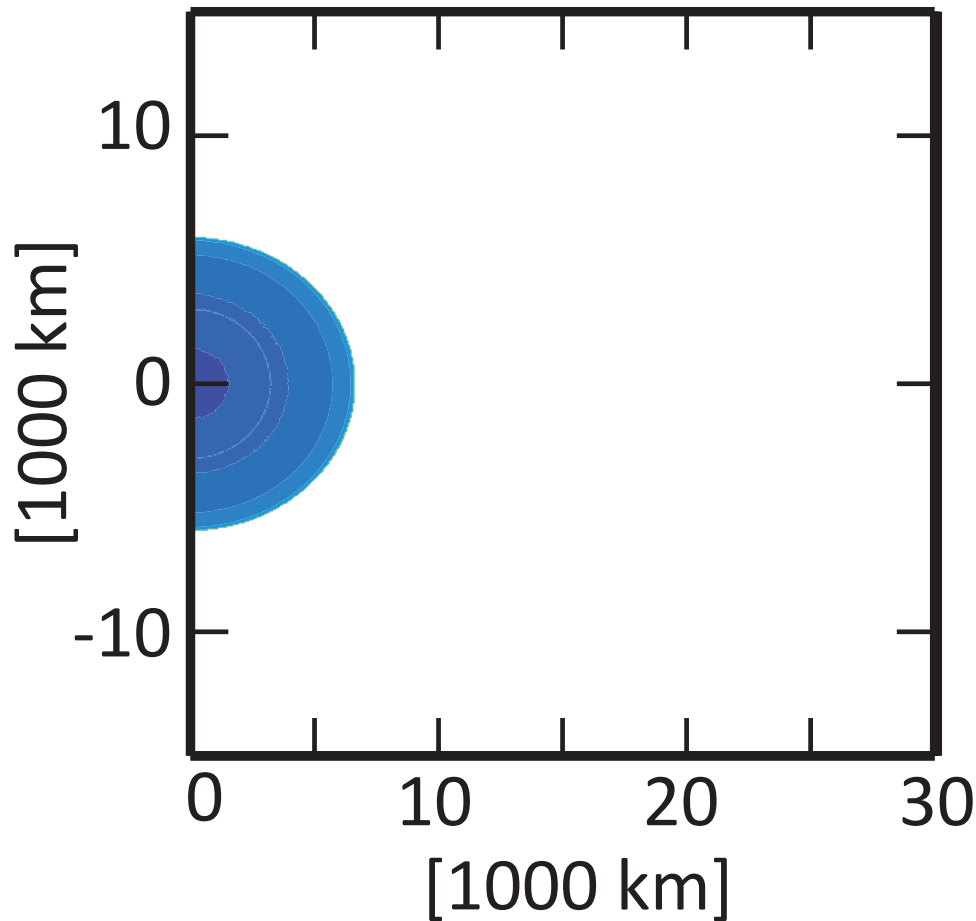


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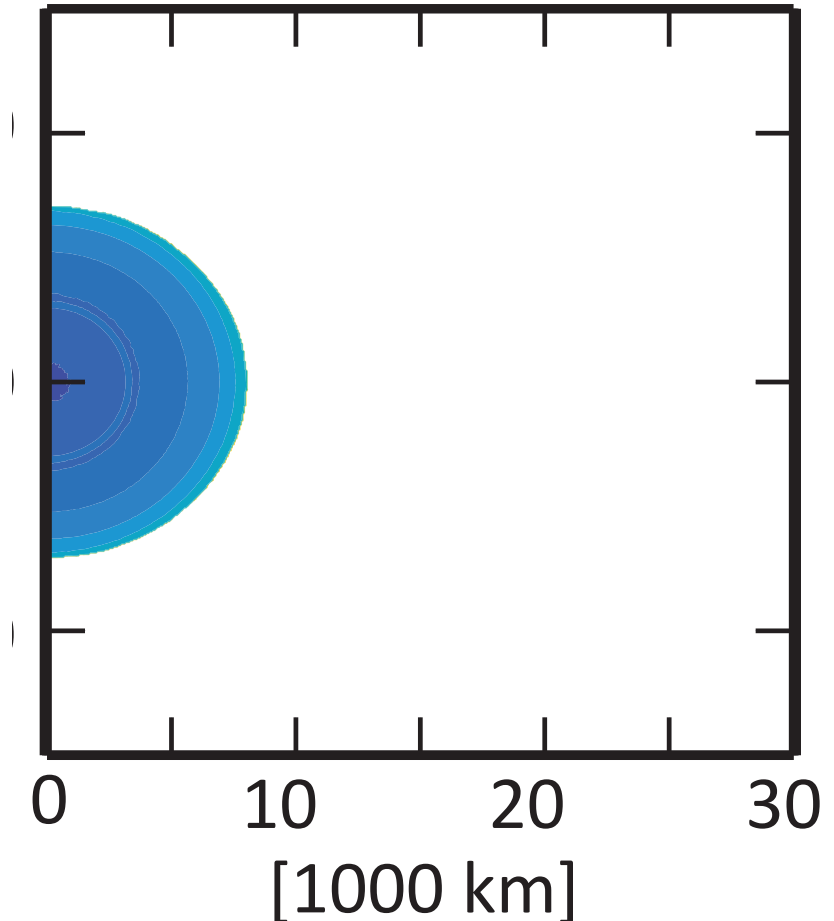
$1 M_{\text{Earth}}$ , Ang. Mom. =  $1 L_{\text{Earth-Moon}}$



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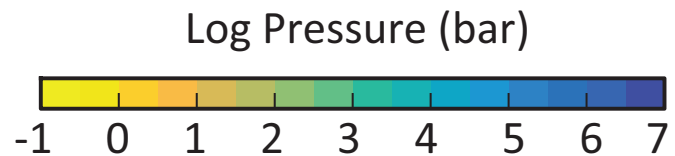


Sp. Entropy 5.74 kJ/K/kg

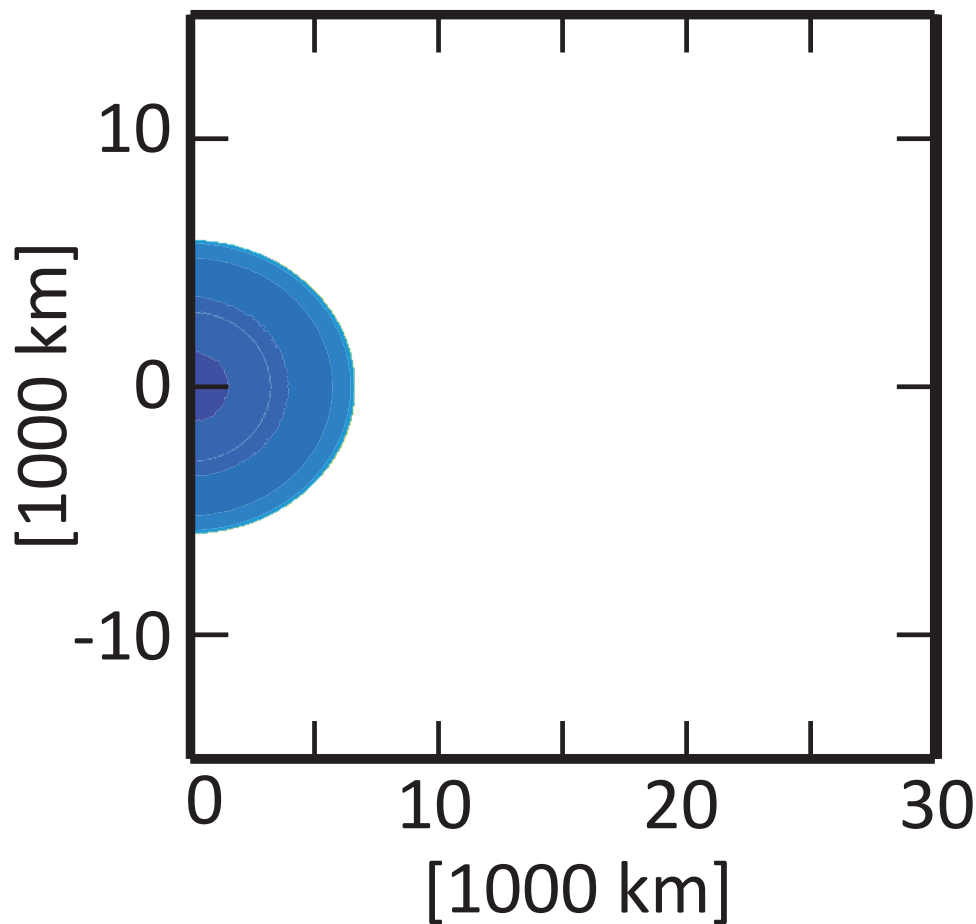


# Increasing Entropy

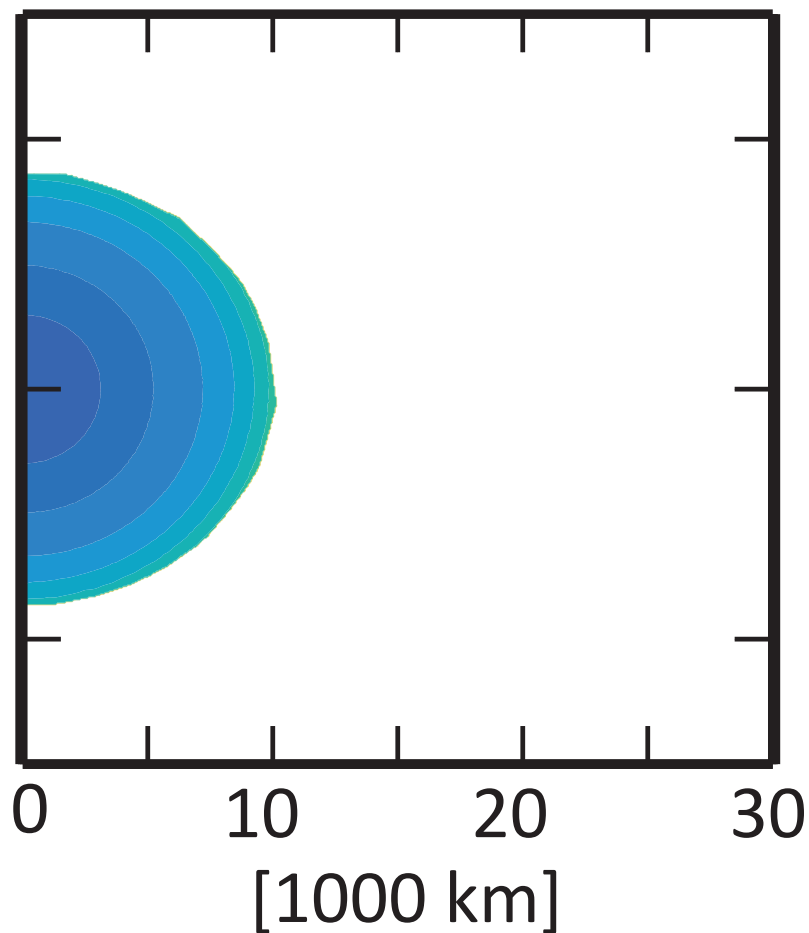
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Sp. Entropy 4.0 kJ/K/kg

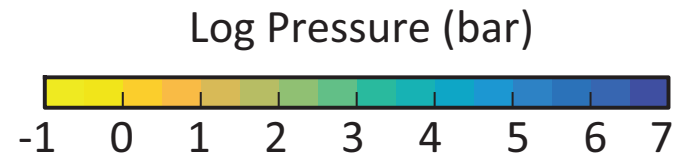


Sp. Entropy 6.24 kJ/K/kg

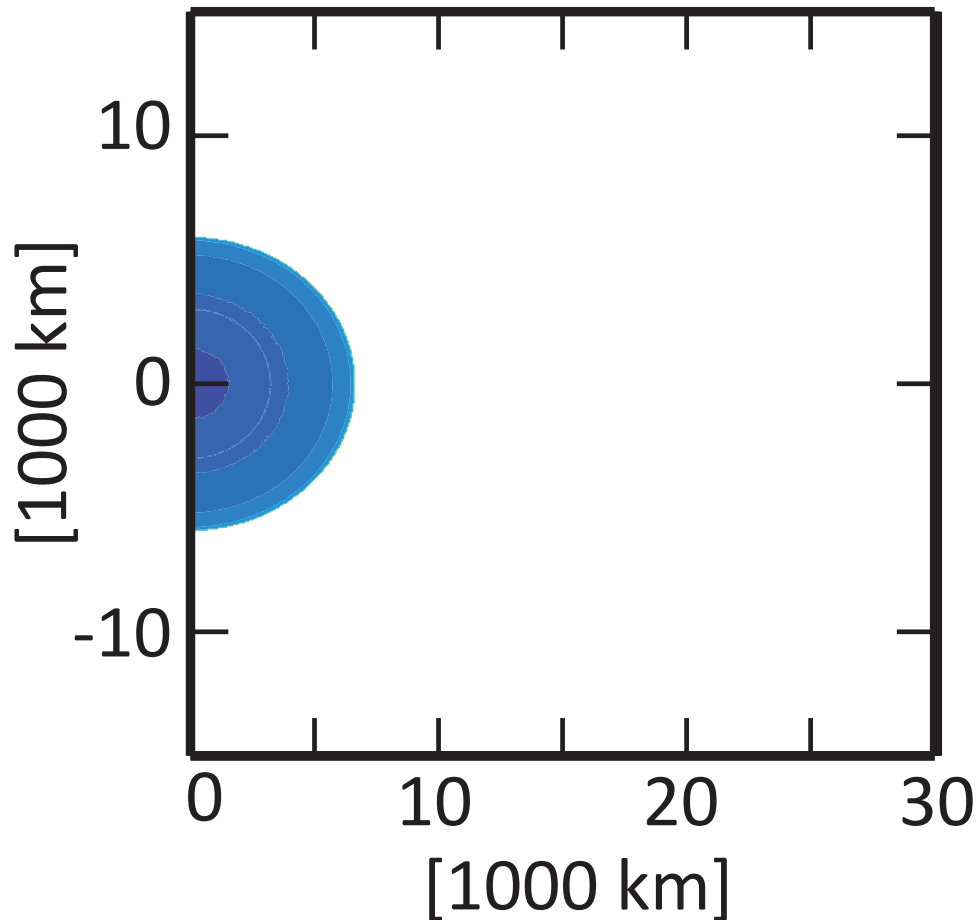


# Increasing Entropy

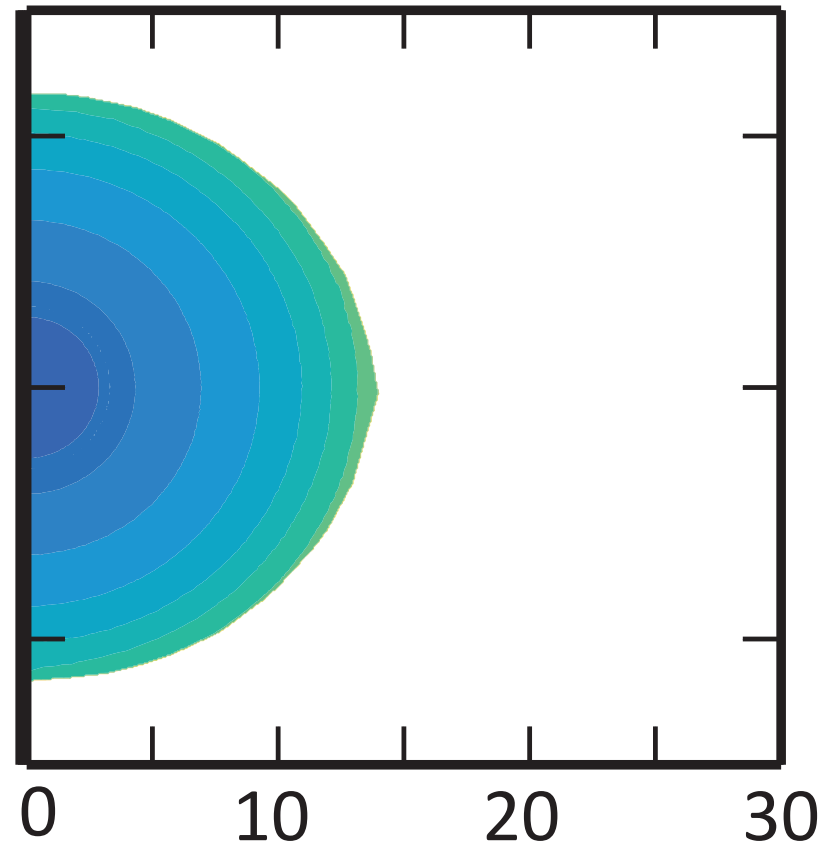
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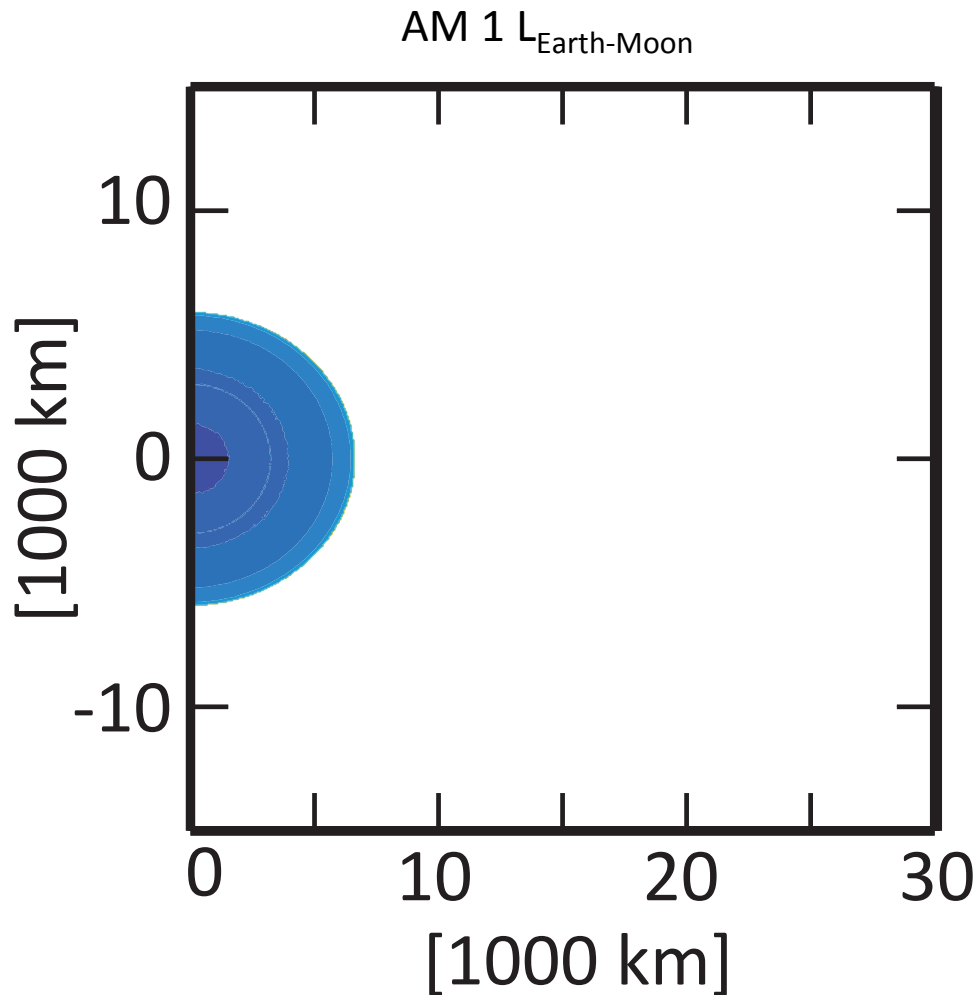
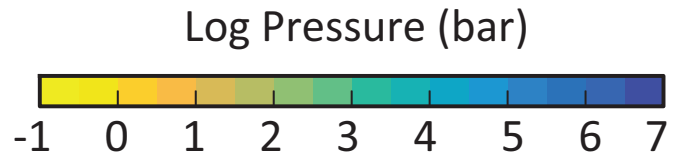
Sp. Entropy 6.74 kJ/K/kg



Large radii, low mass exoplanets:  
Hot rocky planet or sub-Neptune?

# Increasing Angular Momentum

$1 M_{\text{Earth}}, S = 4 \text{ kJ/K/kg}$



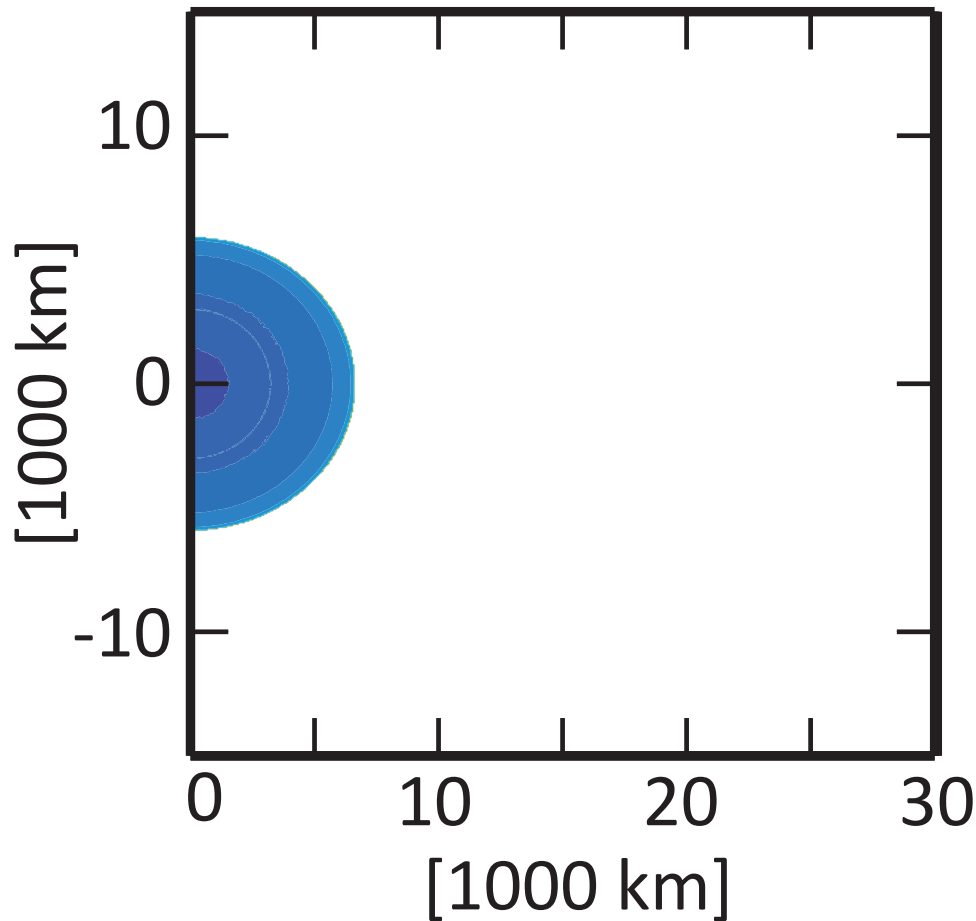
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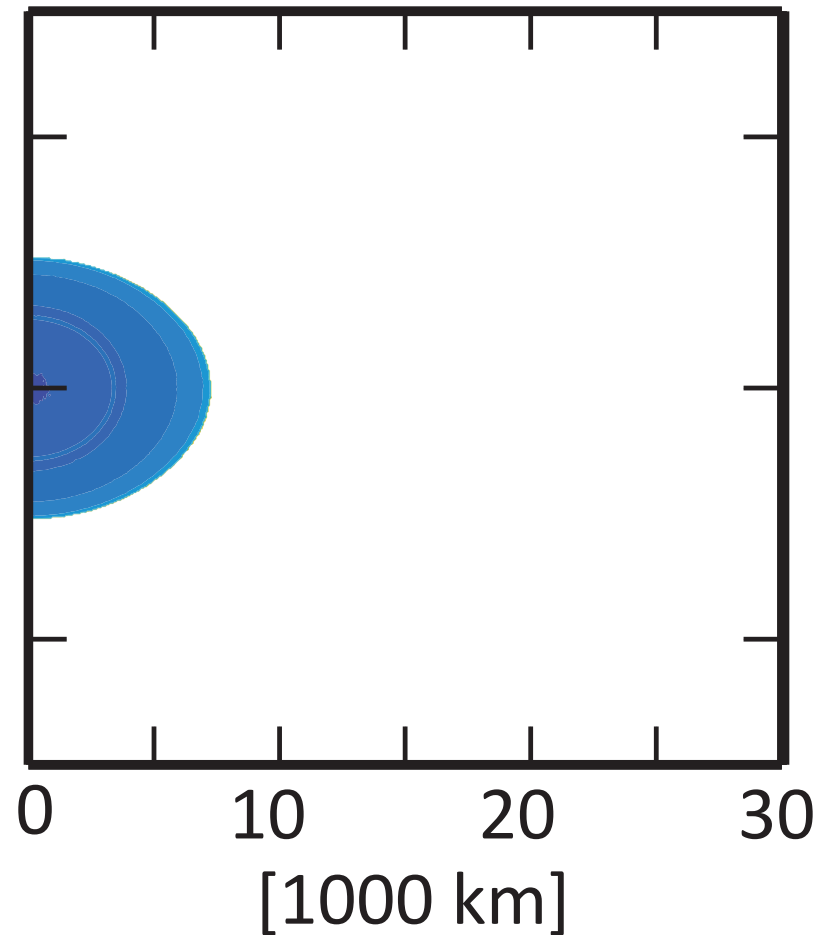
Log Pressure (bar)



AM  $1 L_{\text{Earth-Moon}}$



AM  $1.8 L_{\text{Earth-Moon}}$



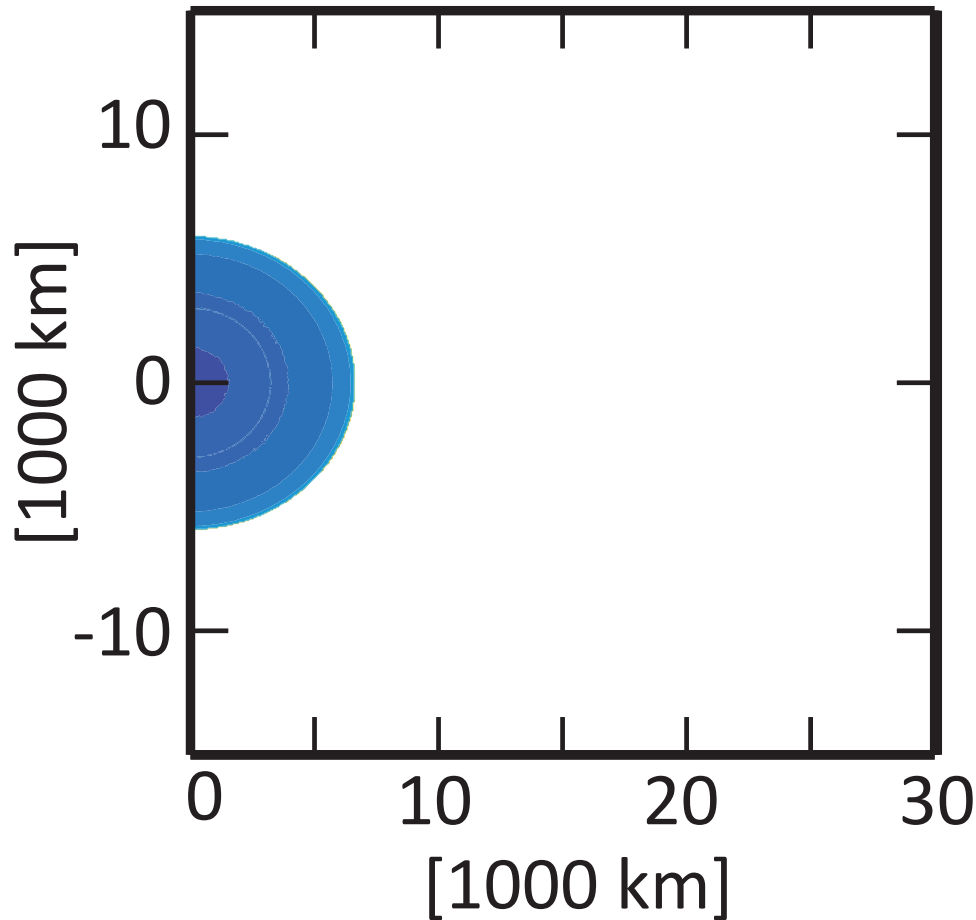
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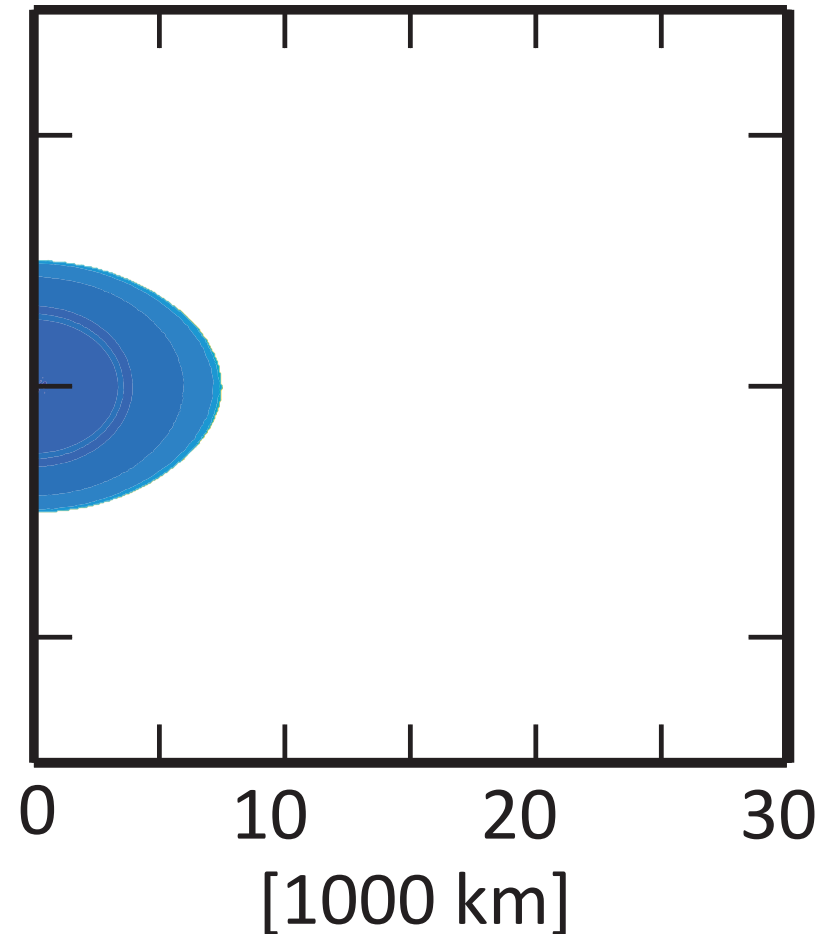
Log Pressure (bar)



AM 1  $L_{\text{Earth-Moon}}$



AM 2.0  $L_{\text{Earth-Moon}}$



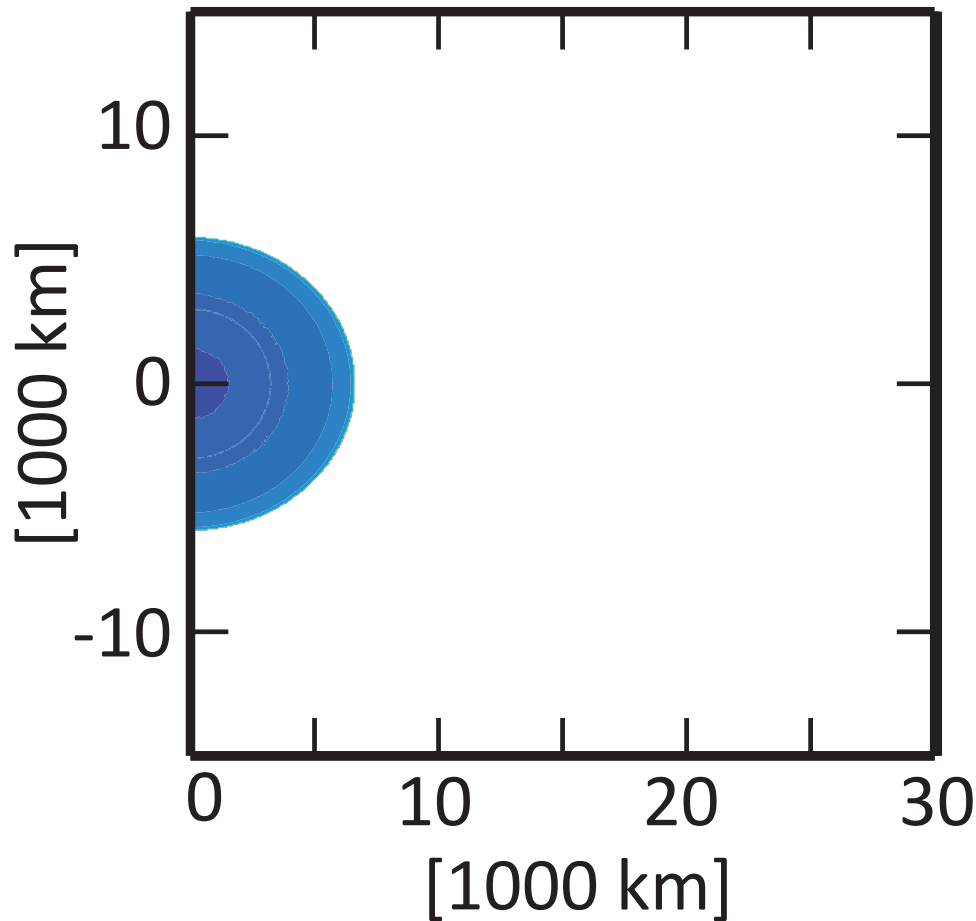
# Increasing Angular Momentum

$1 M_{\text{Earth}}, S = 4 \text{ kJ/K/kg}$

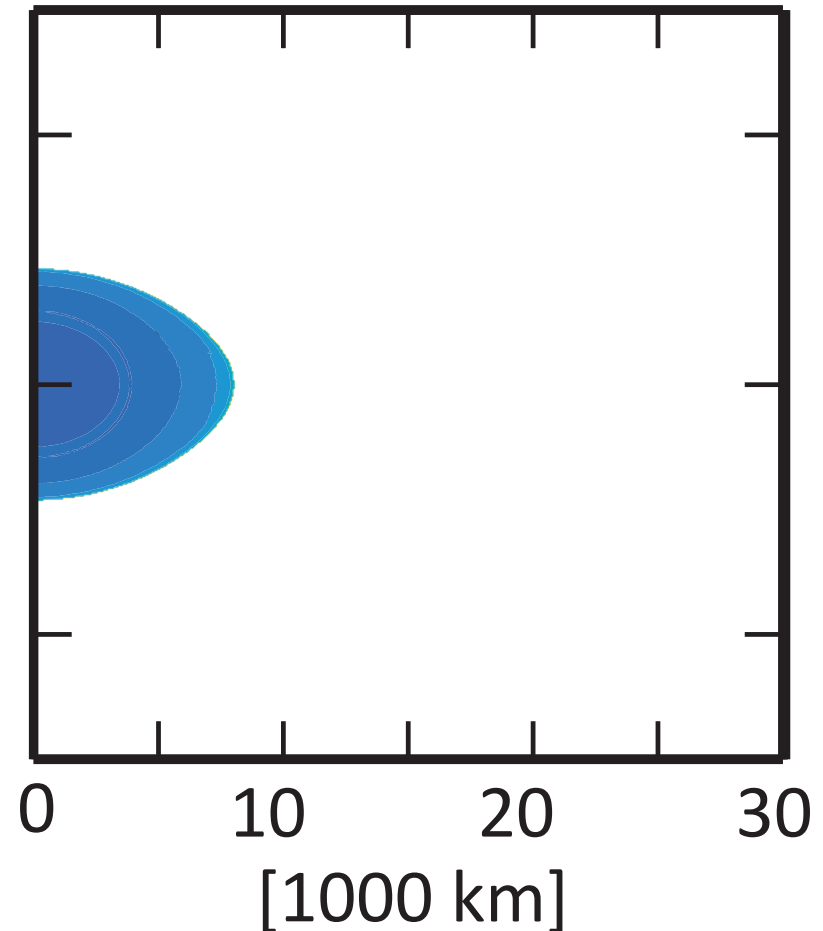
Log Pressure (bar)



AM  $1 L_{\text{Earth-Moon}}$



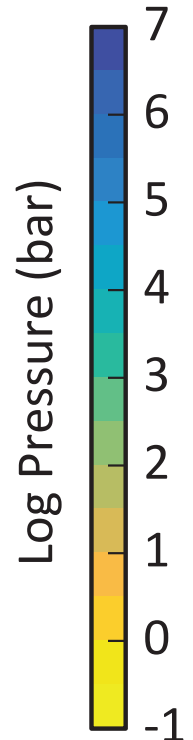
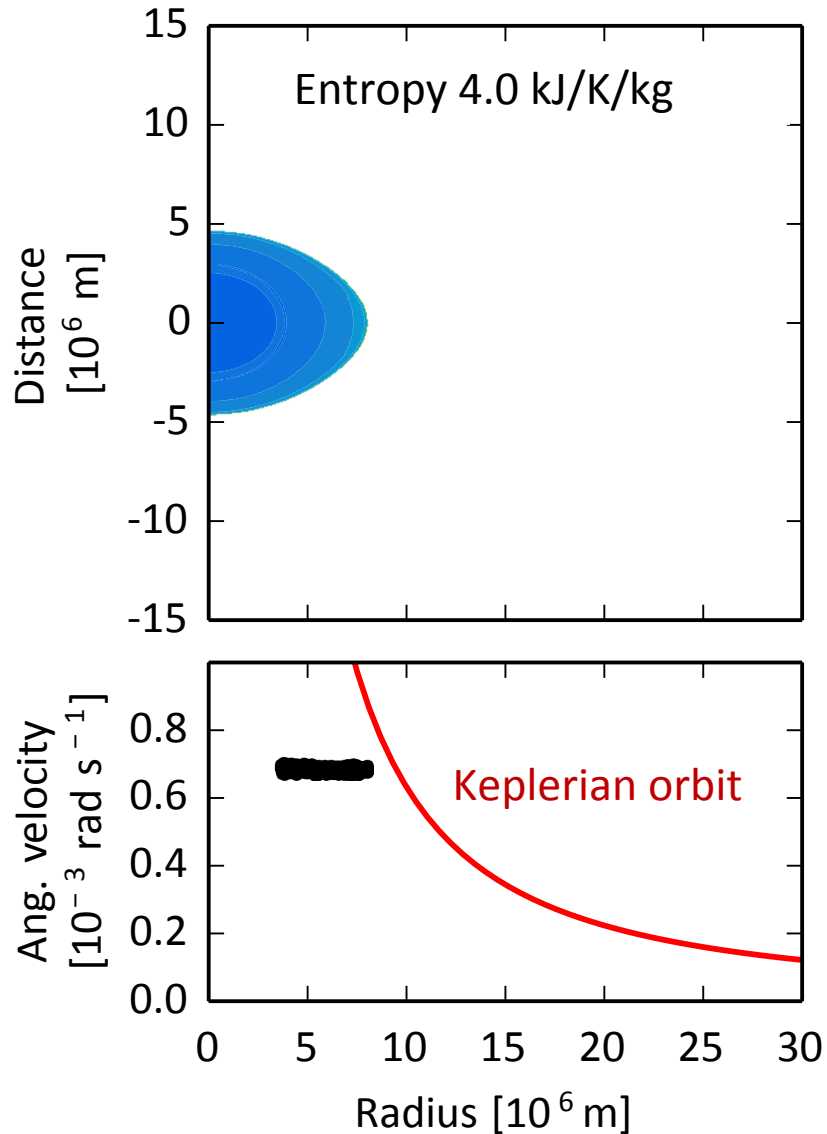
AM  $2.45 L_{\text{Earth-Moon}}$





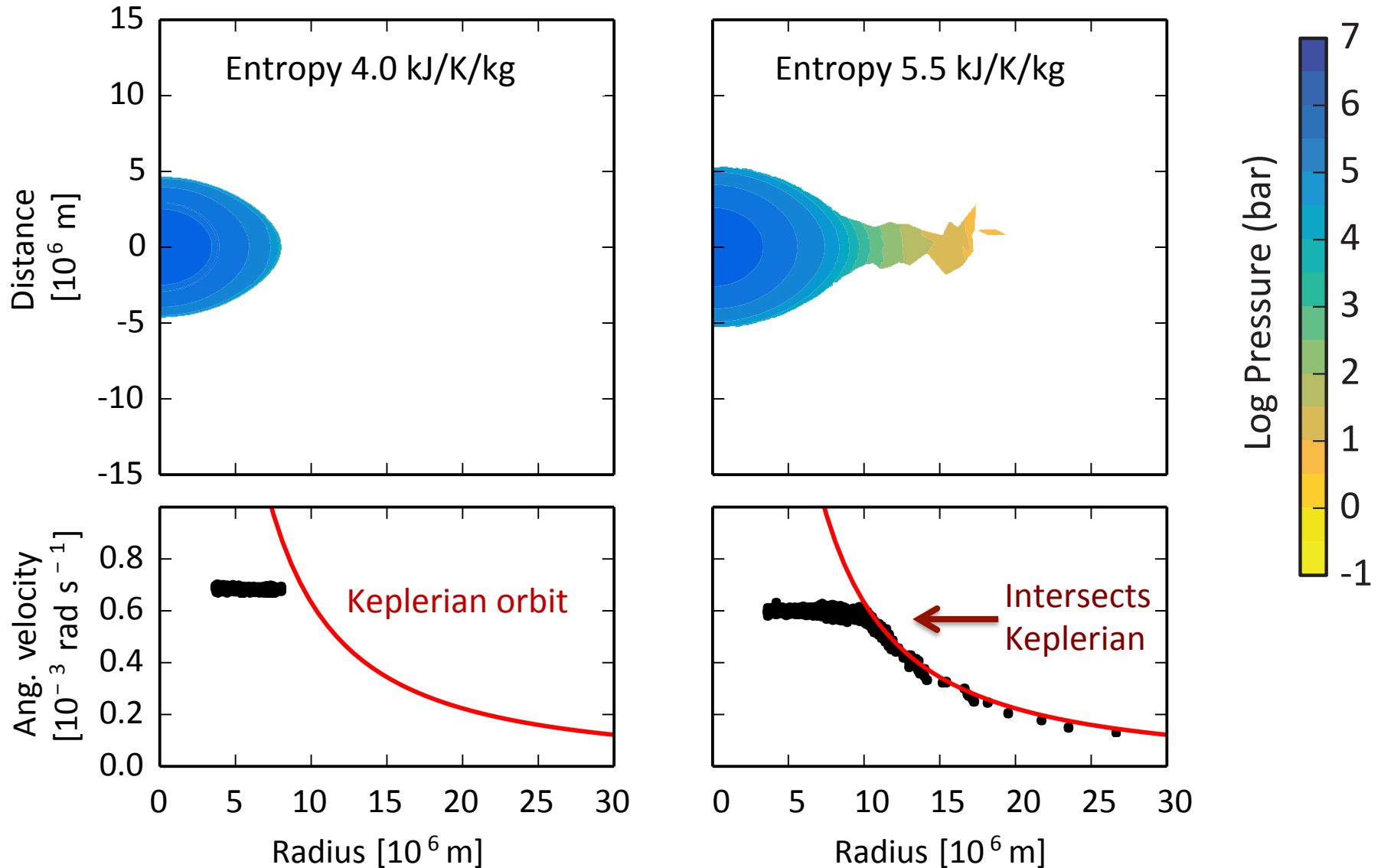
# High AM and High Entropy

Ang. Mom.= $2.45 L_{\text{Earth-Moon}}$



# High AM and High Entropy

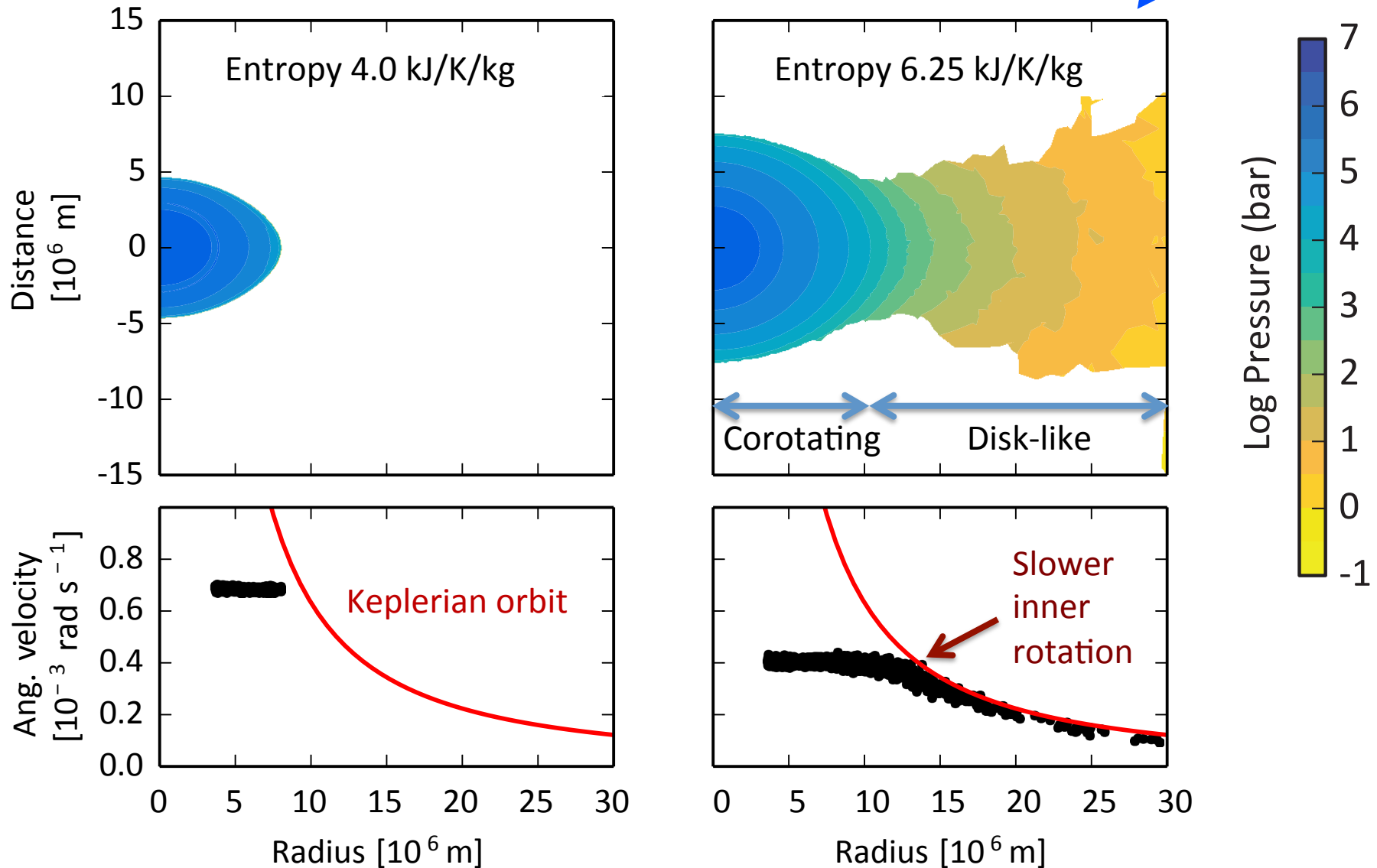
Ang. Mom.= $2.45 L_{\text{Earth-Moon}}$



# High AM and High Entropy

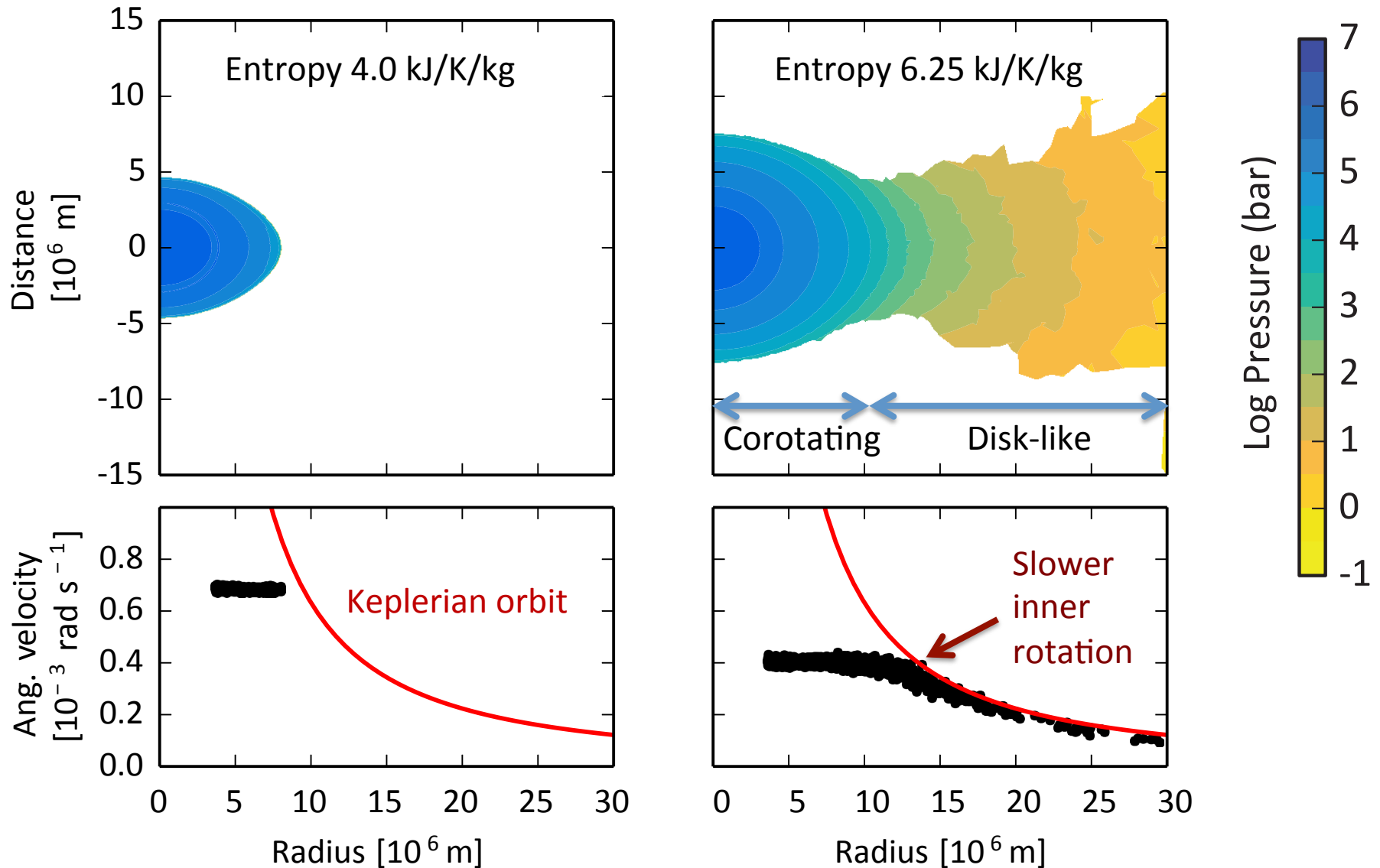
Ang. Mom.= $2.45 L_{\text{Earth-Moon}}$

A Terrestrial Synestia



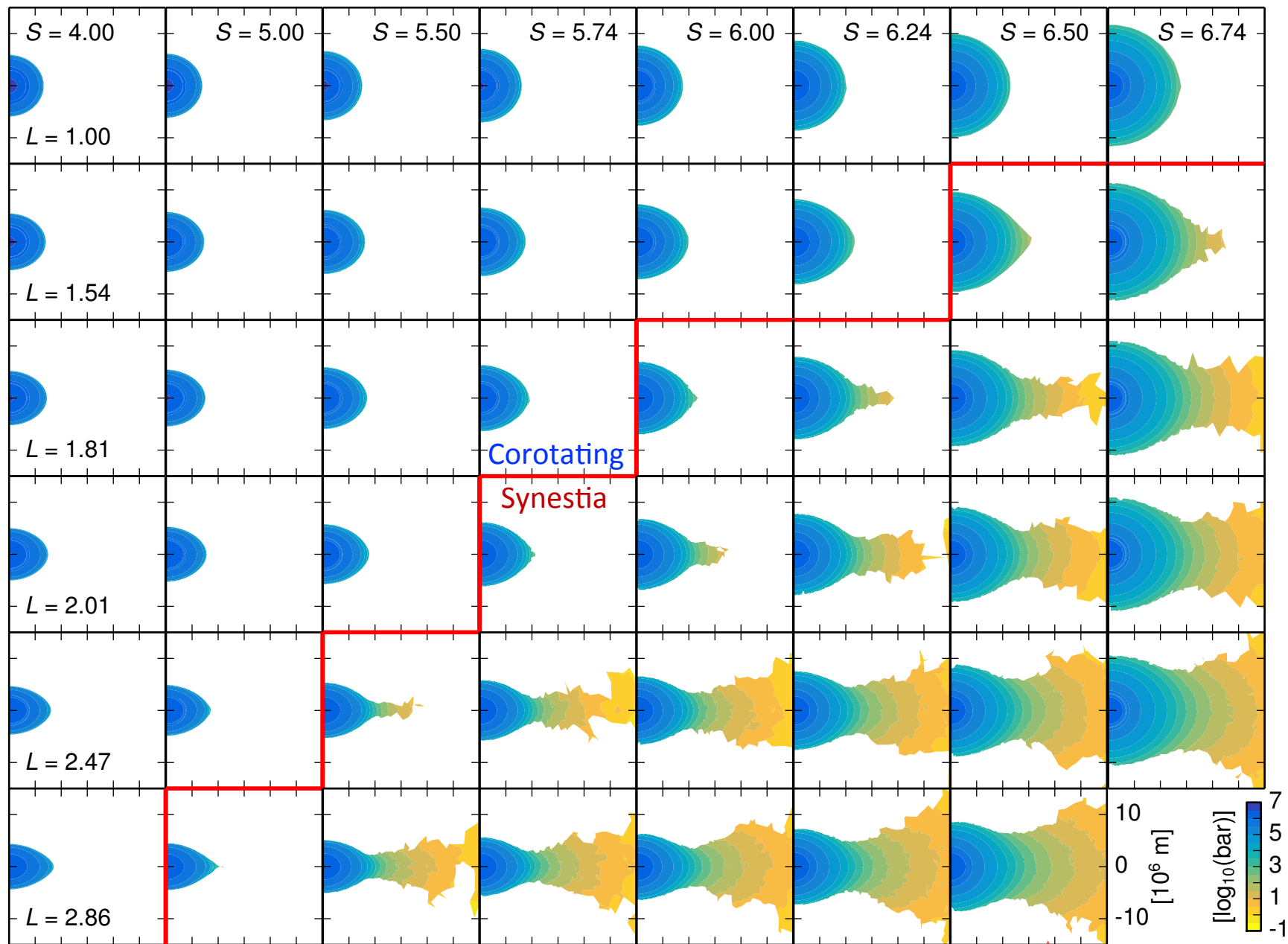
# Synestia: Connected Structure

syn + Hestia (goddess of architecture, hearth/home)

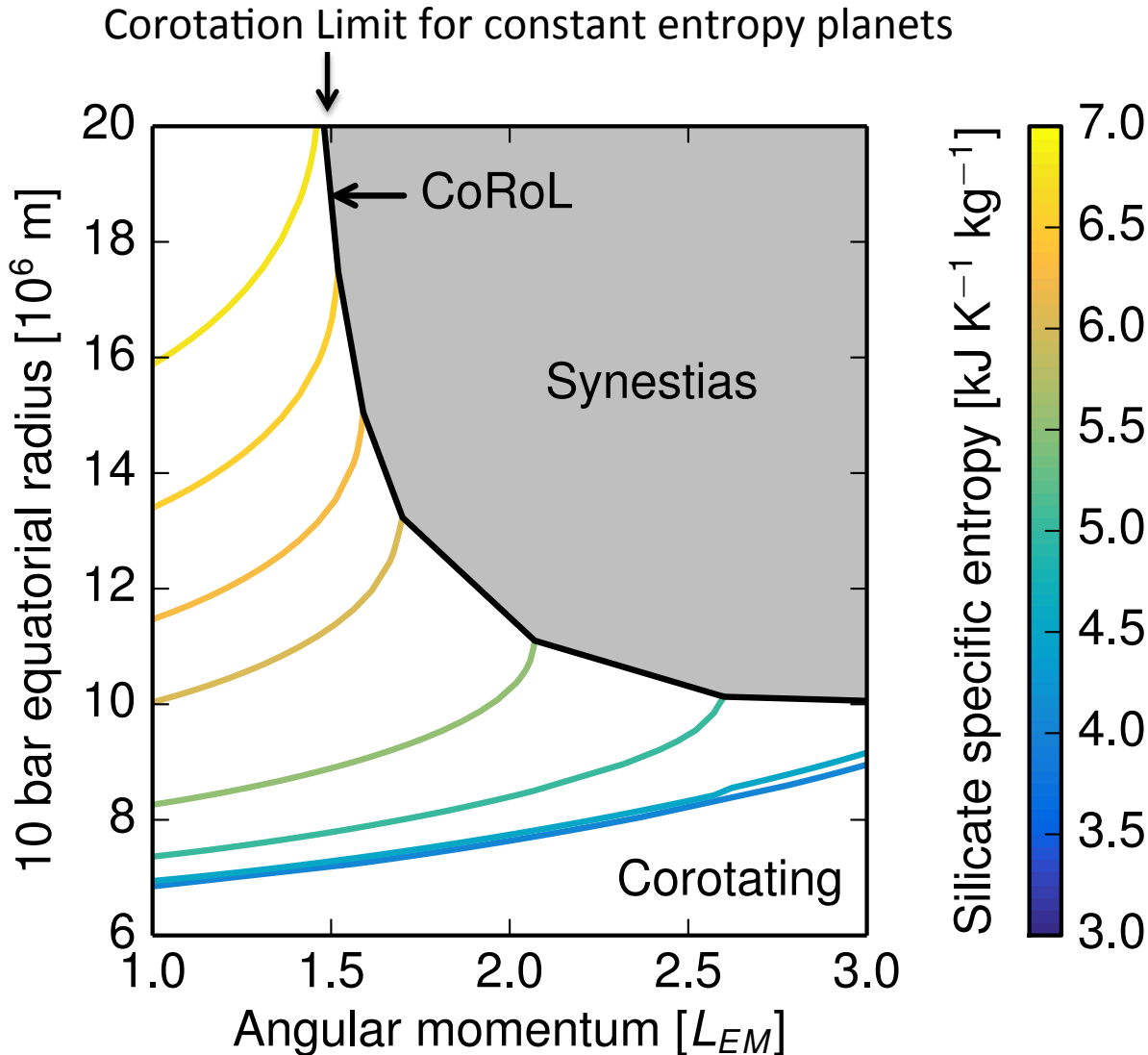


Increasing Specific Entropy (kJ/K/kg)

Increasing Ang. Mom. [ $L_{E-M}$ ]



# Corotating Planets and Synestias



Synestias are a new class of astronomical objects.

Dynamics are very different from corotating planets.

Important for rocky planet giant impacts, formation of gas giant planets and their satellites, and fast-spinning stars.

Expect multiple synestias during planet formation.

# Post-impact Synestia

Normal Planet

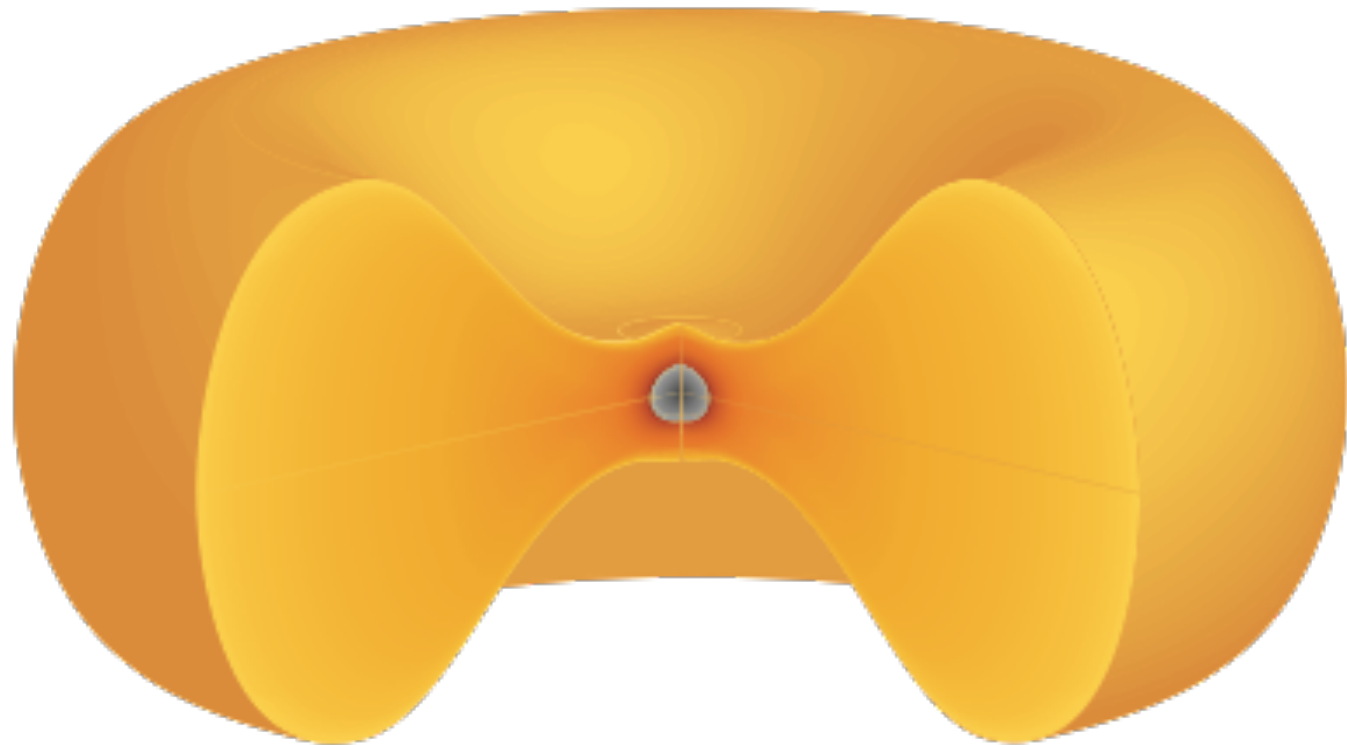


Traditional Planet and Disk



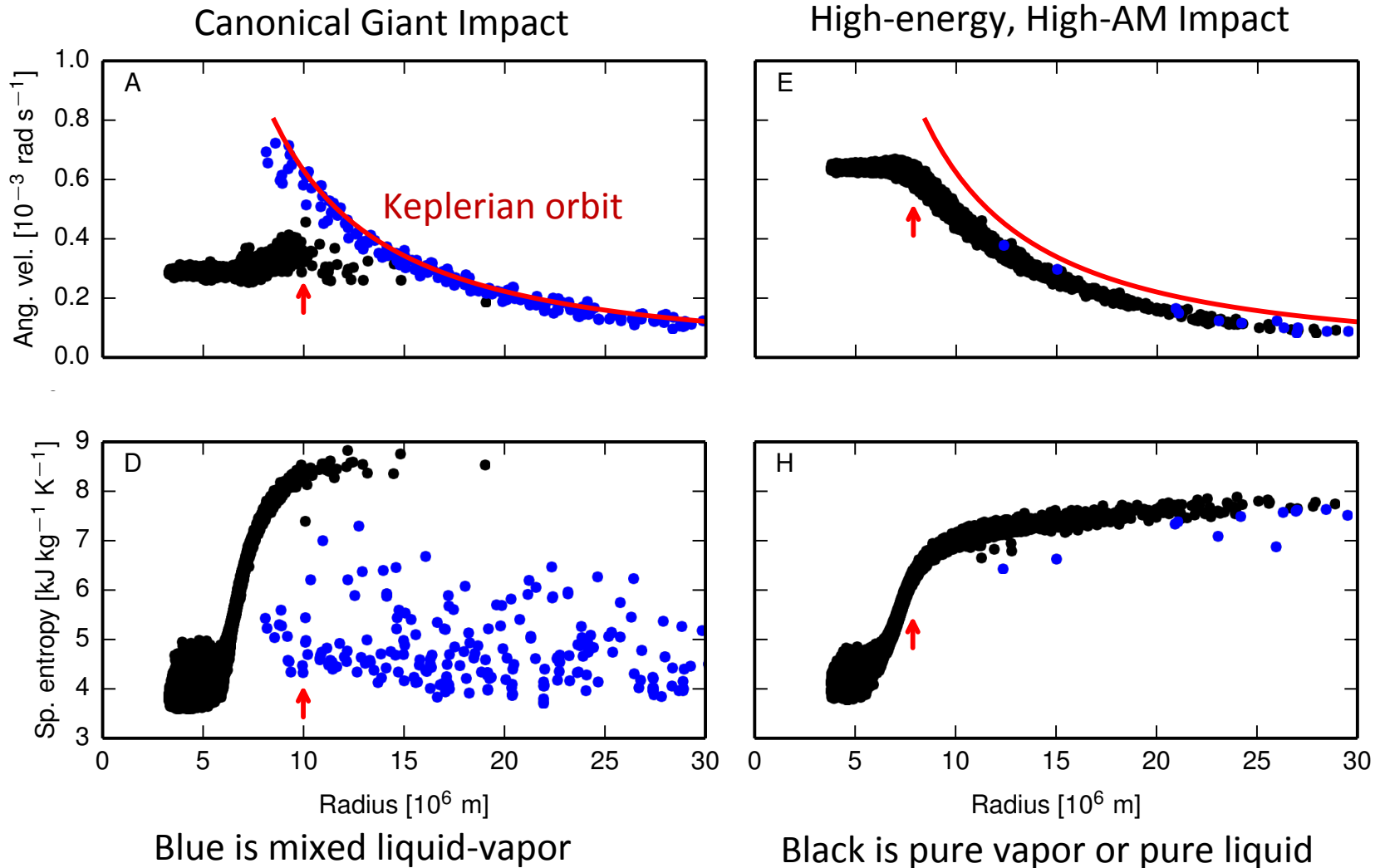
To scale

Impact-generated Synestia



# Example Post-Giant Impact Structures

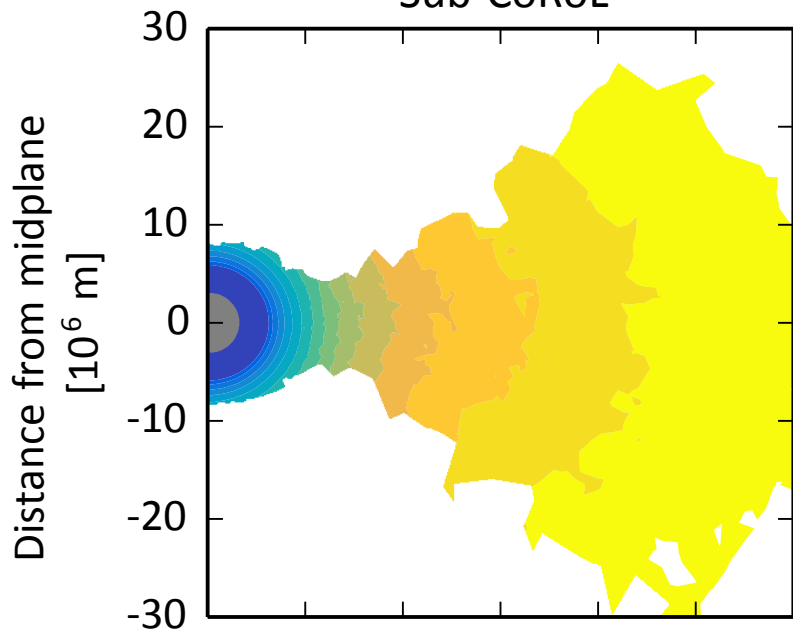
## Profile in the midplane



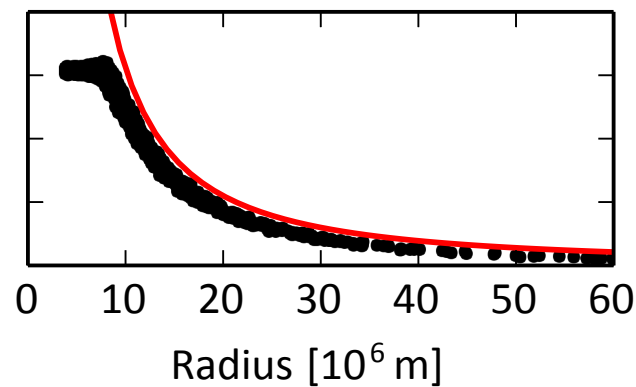
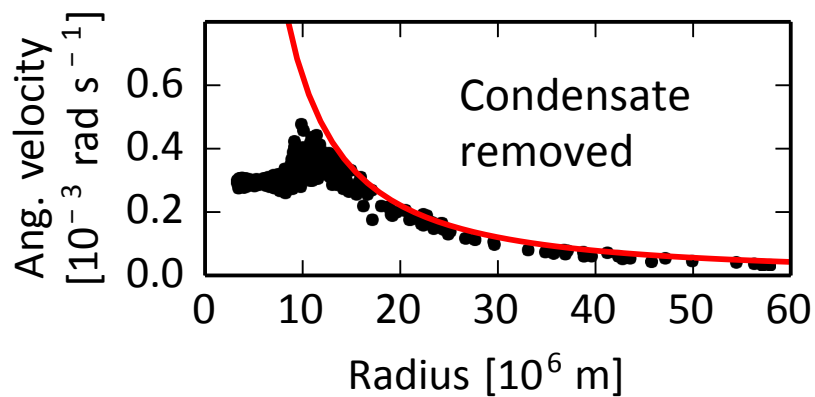
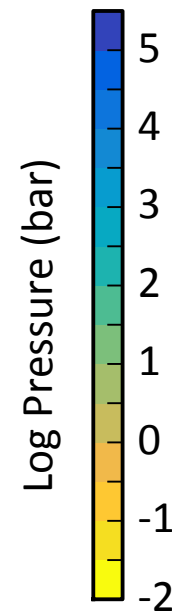
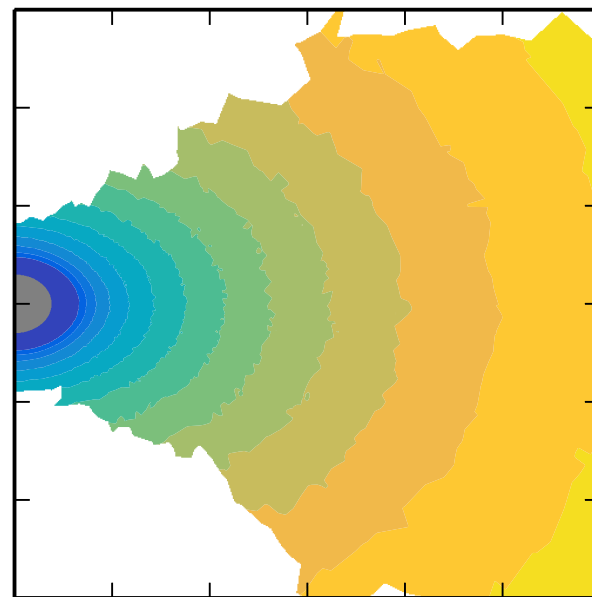


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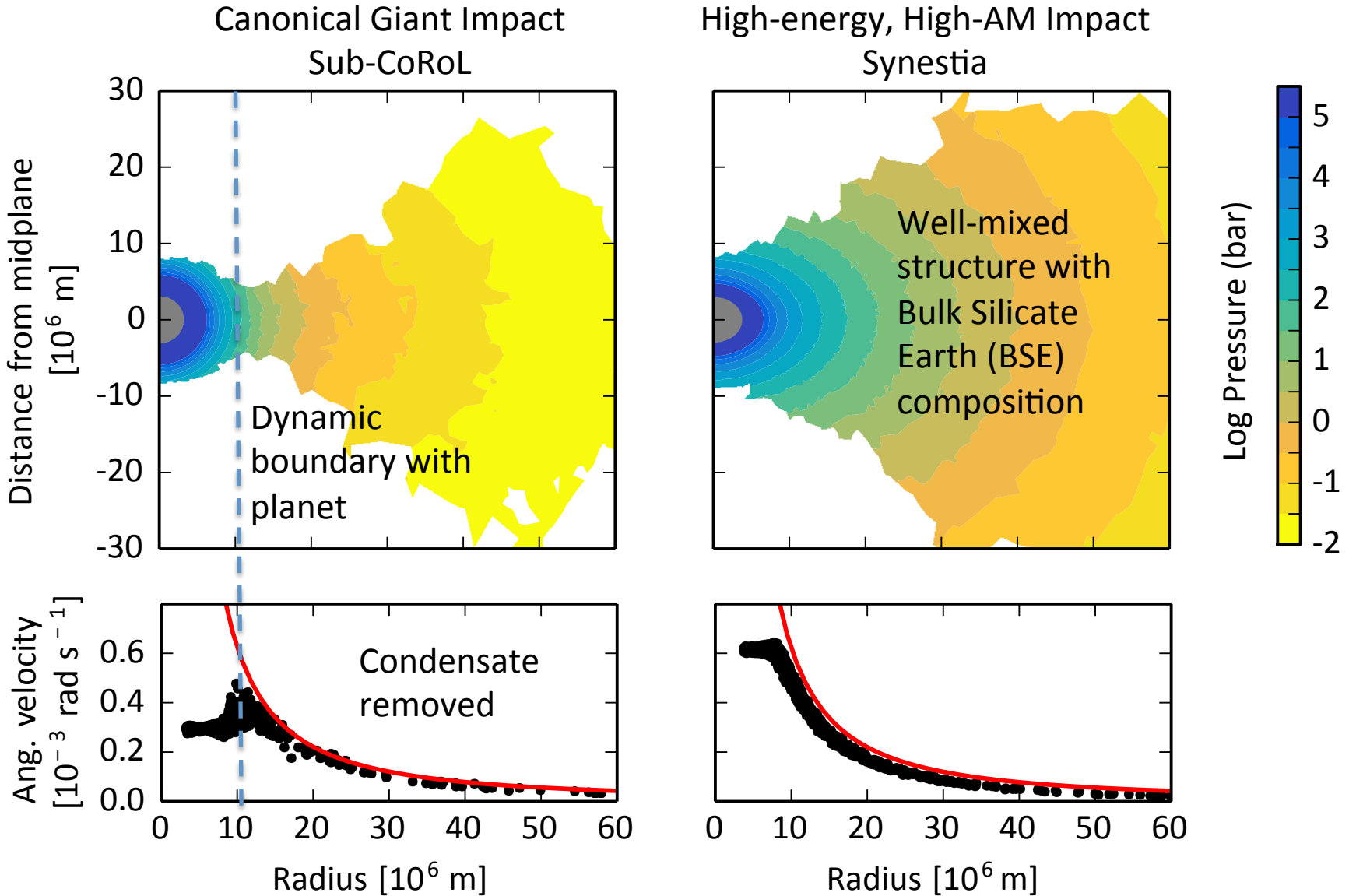
Canonical Giant Impact  
Sub-CoRoL



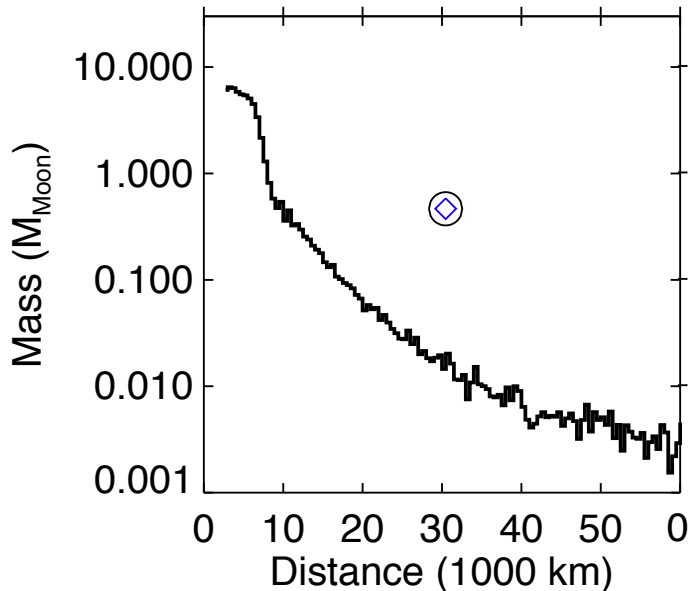
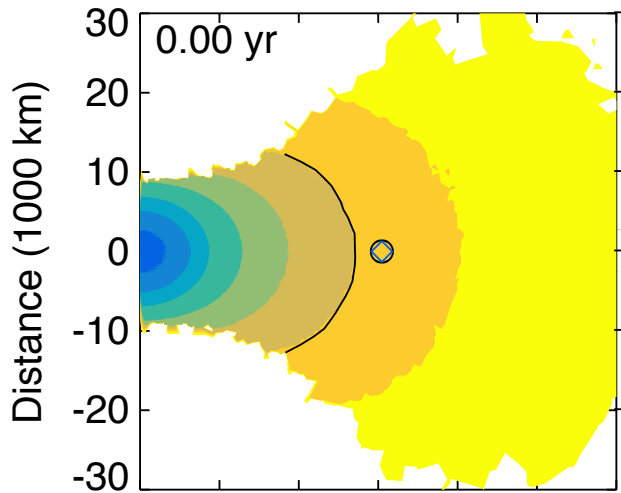
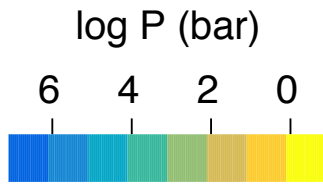
High-energy, High-AM Impact  
Synestia



# Example Post-Giant Impact Structures



# Cooling a synestia



Modified SPH code to simulate thermal equilibration and radiative cooling

No internal heating

Conservative estimate for FASTEST cooling

Condensates are extracted forming a 'lunar seed'

Structure condenses from outer radii inwards. Falling silicate 'raindrops' either re-vaporize or accrete into growing moonlets.

Condensates beyond Roche limit == growing moon

Two estimates for lunar mass and orbit

# Cooling a synestia

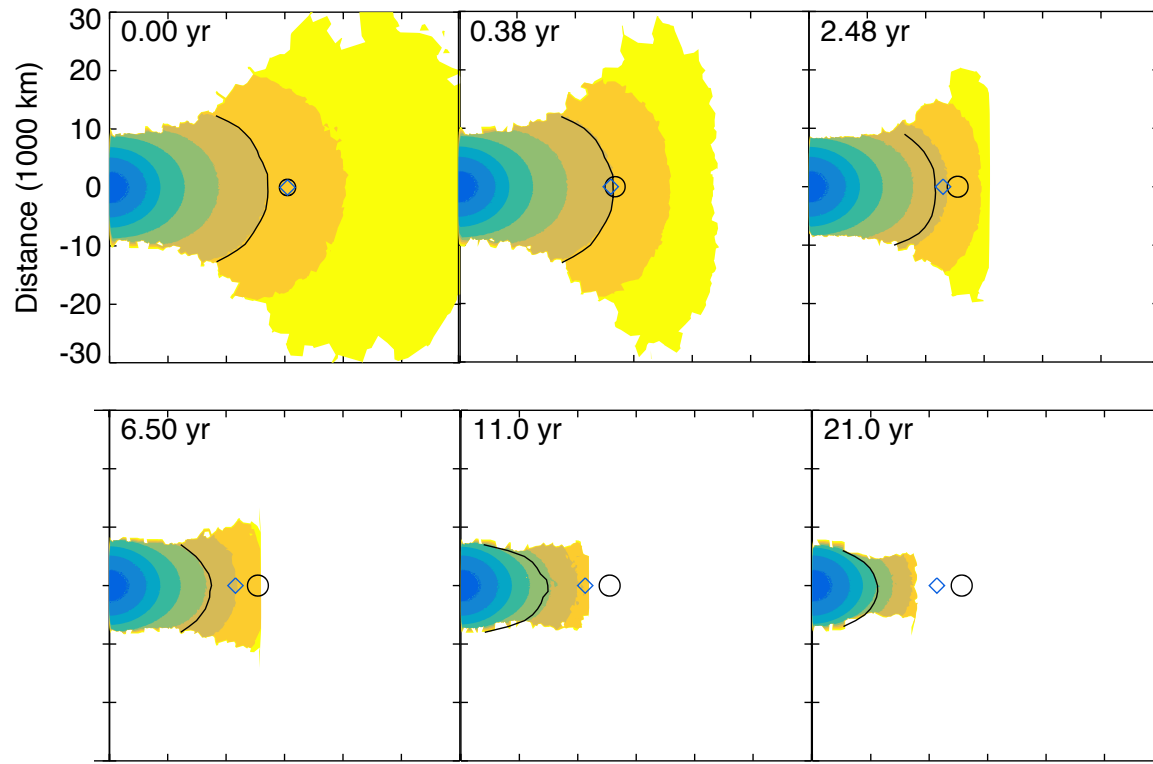
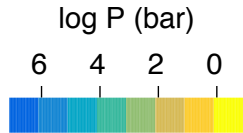
Canup 2012 style giant impact

$M_t = 0.572 M_{\text{Earth}}$

$M_p = 0.468 M_{\text{Earth}}$

$V = 12.33 \text{ km/s}$ ,  $b = 0.4$

Similar results for other impact scenarios



Black line is boundary between pure vapor and saturated vapor curve

# Cooling a synestia

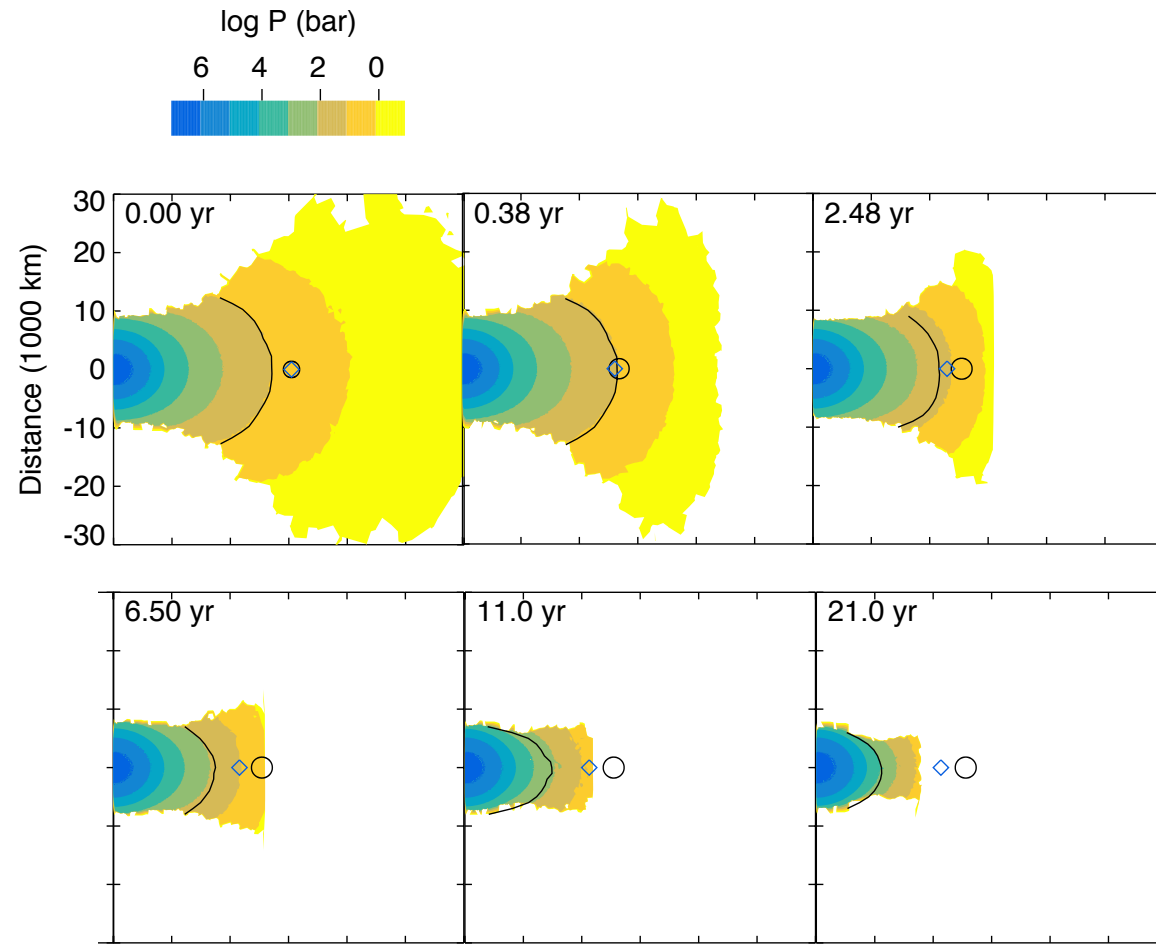
Canup 2012 style giant impact

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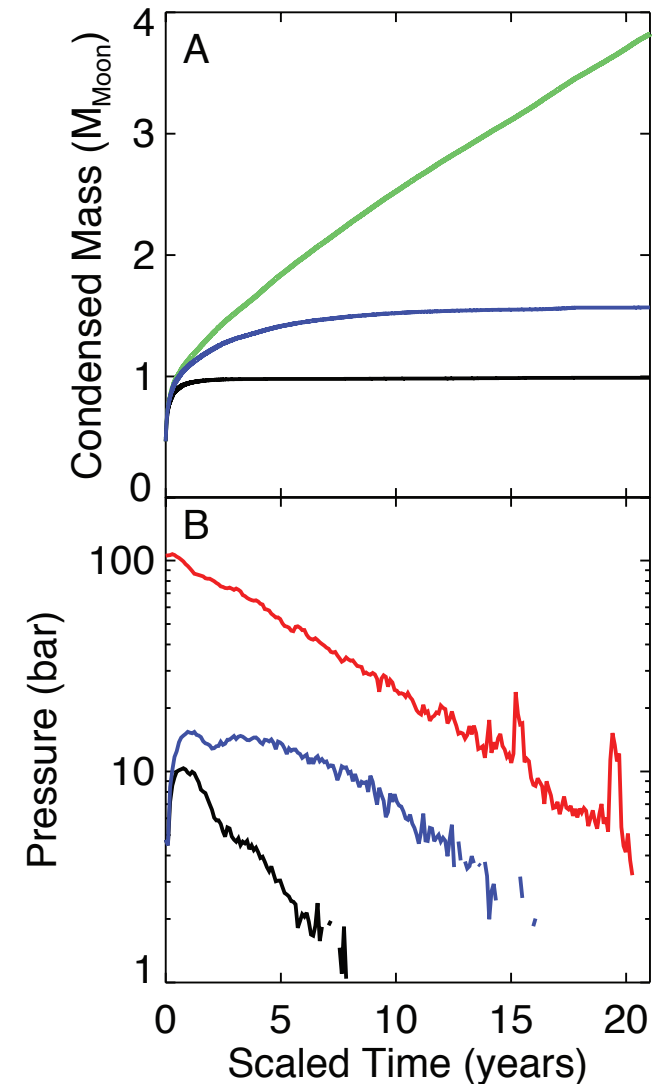
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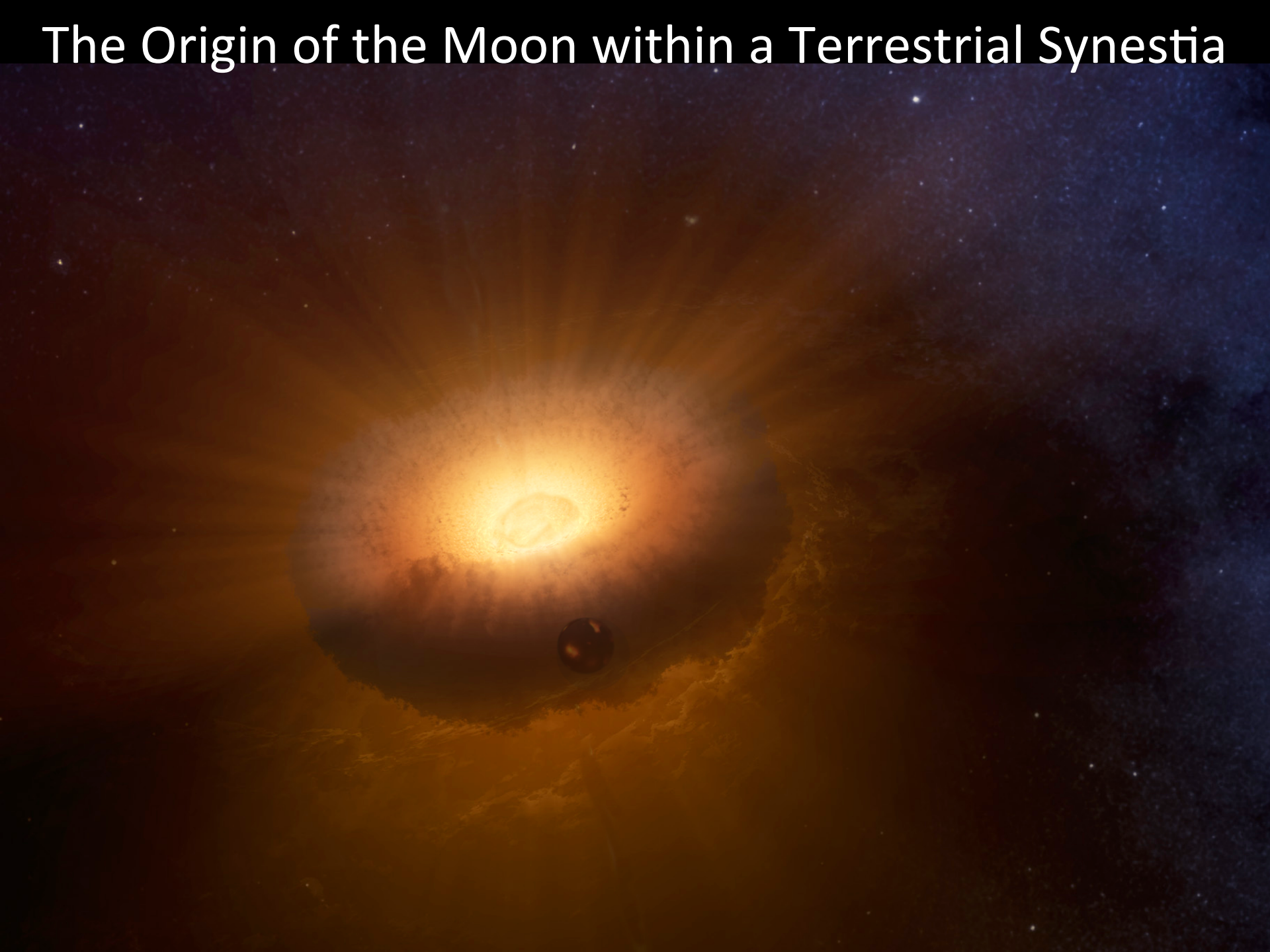
Similar results for other impact scenarios



Moon grows in  $\sim 1$  year. Orbits for several years within the synestia within 10's bars of BSE vapor.



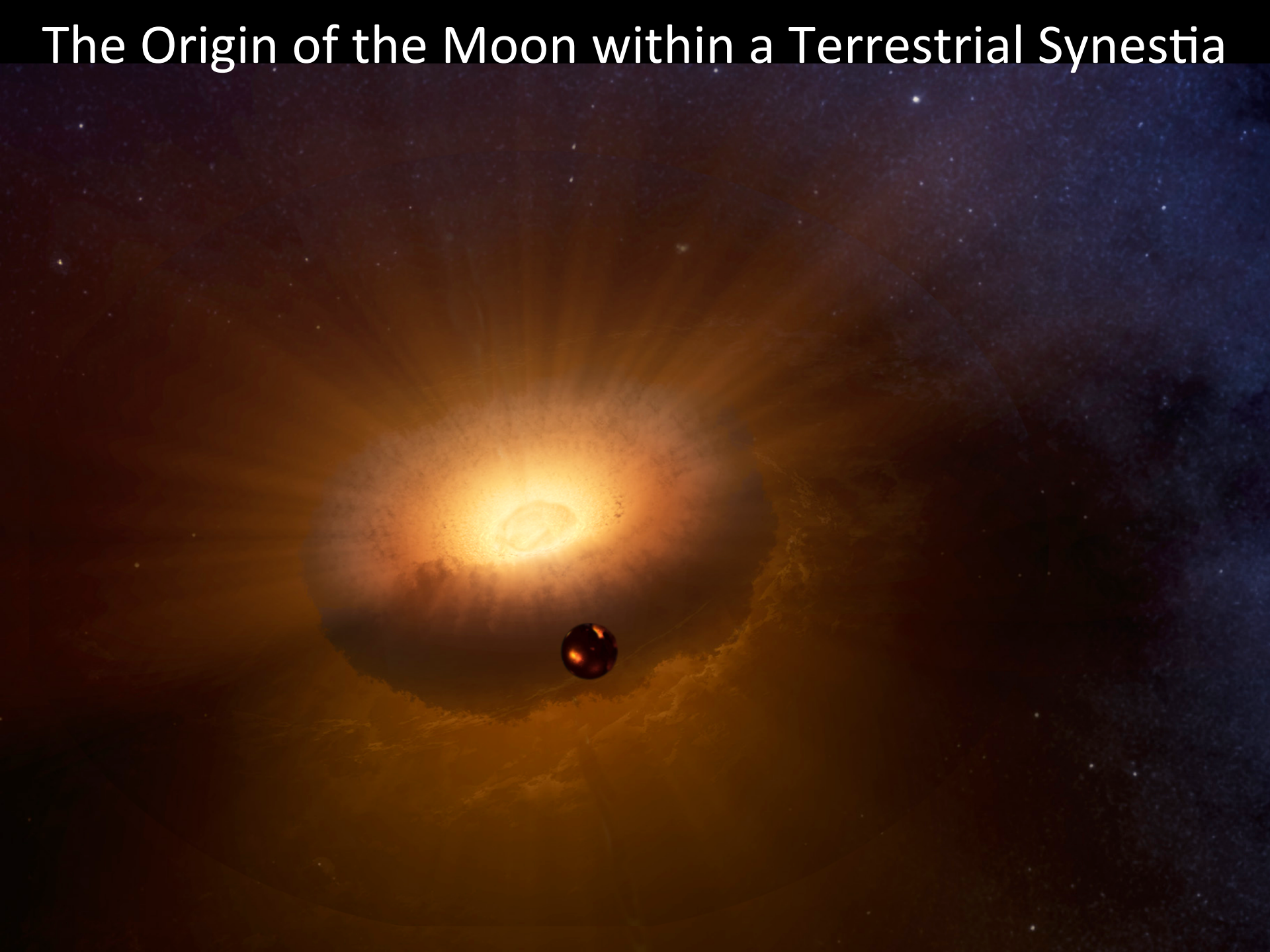
# The Origin of the Moon within a Terrestrial Synestia



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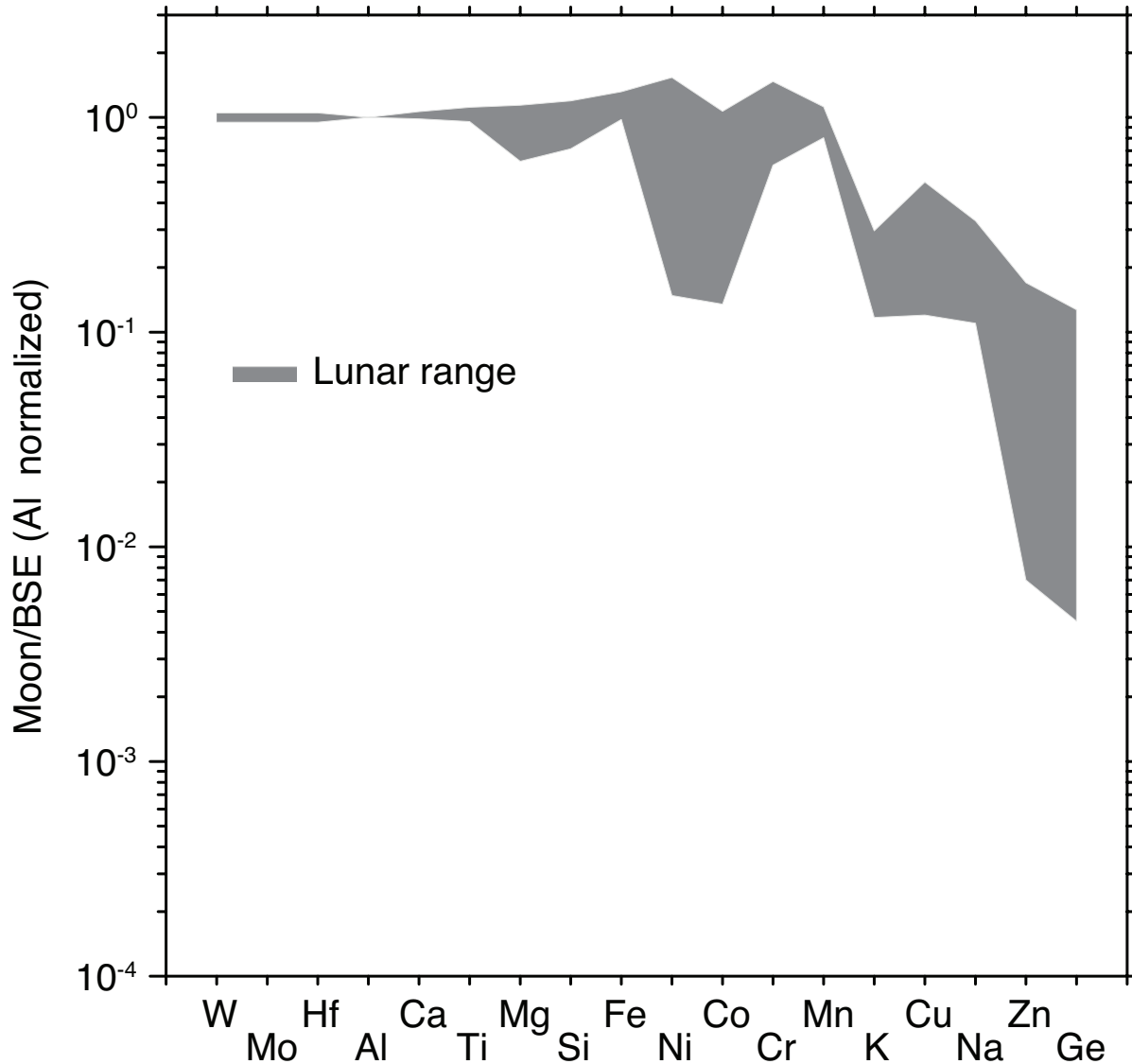


# The Origin of the Moon within a Terrestrial Synestia



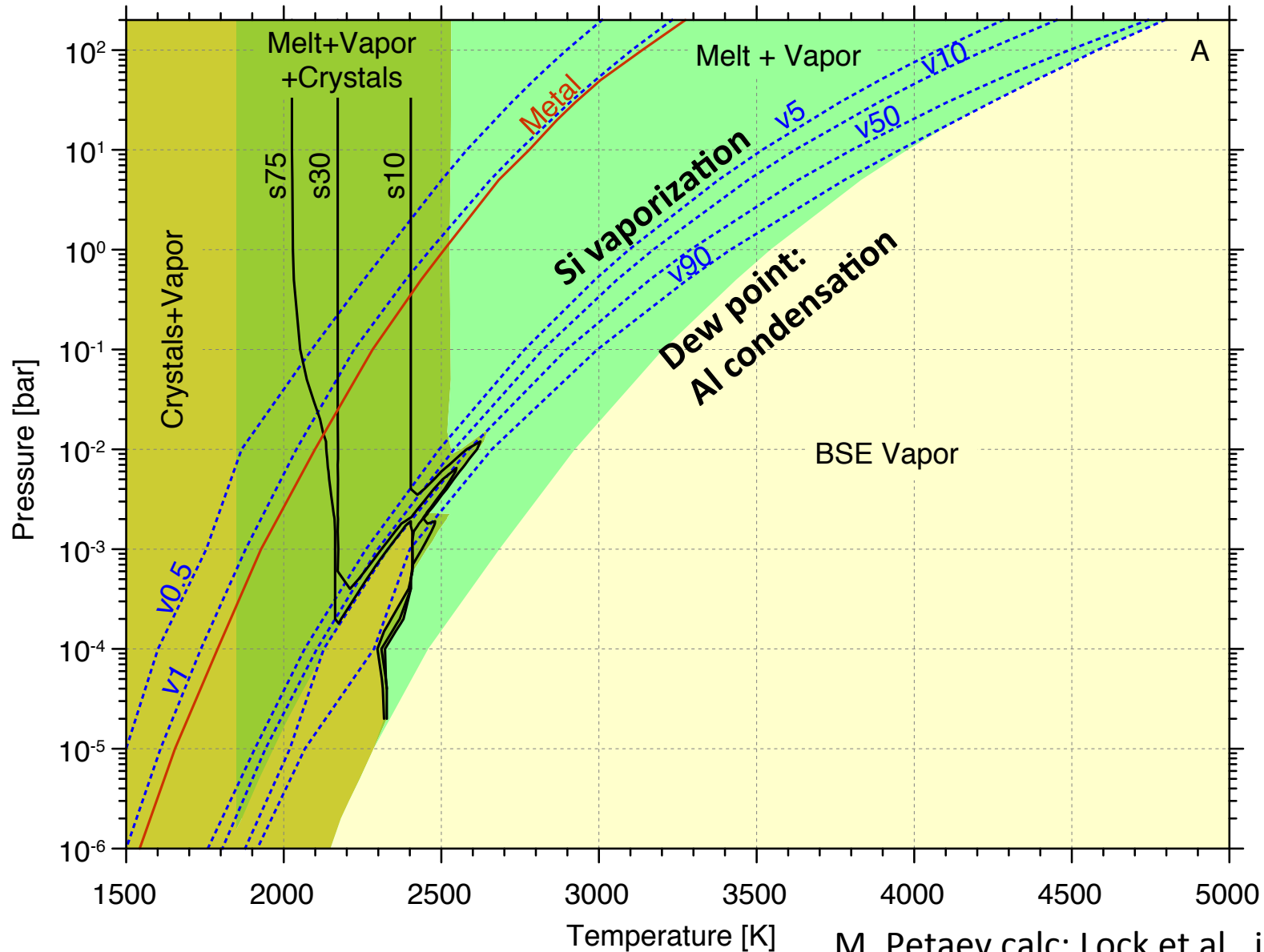


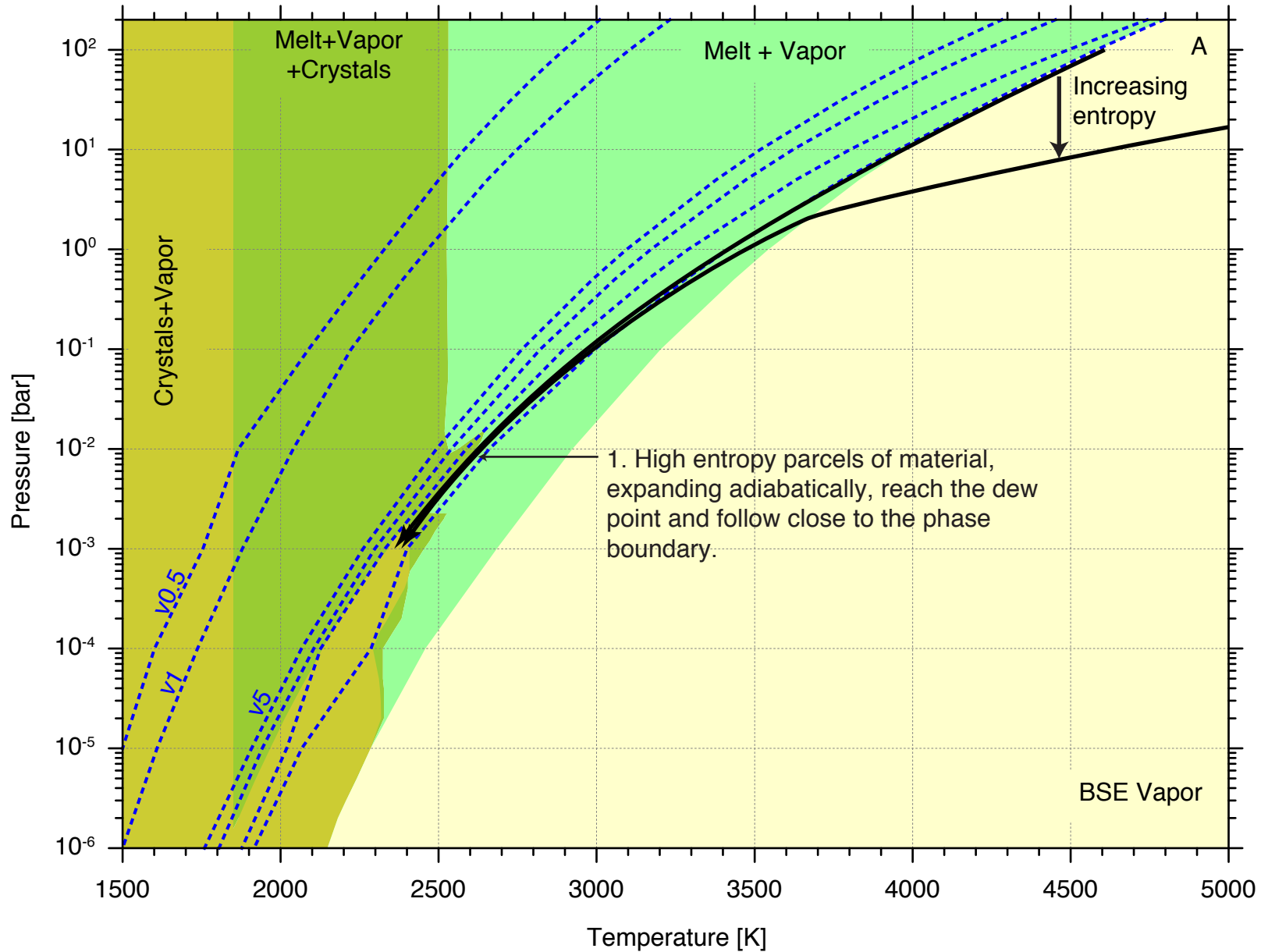
# What is the composition of the Moon?

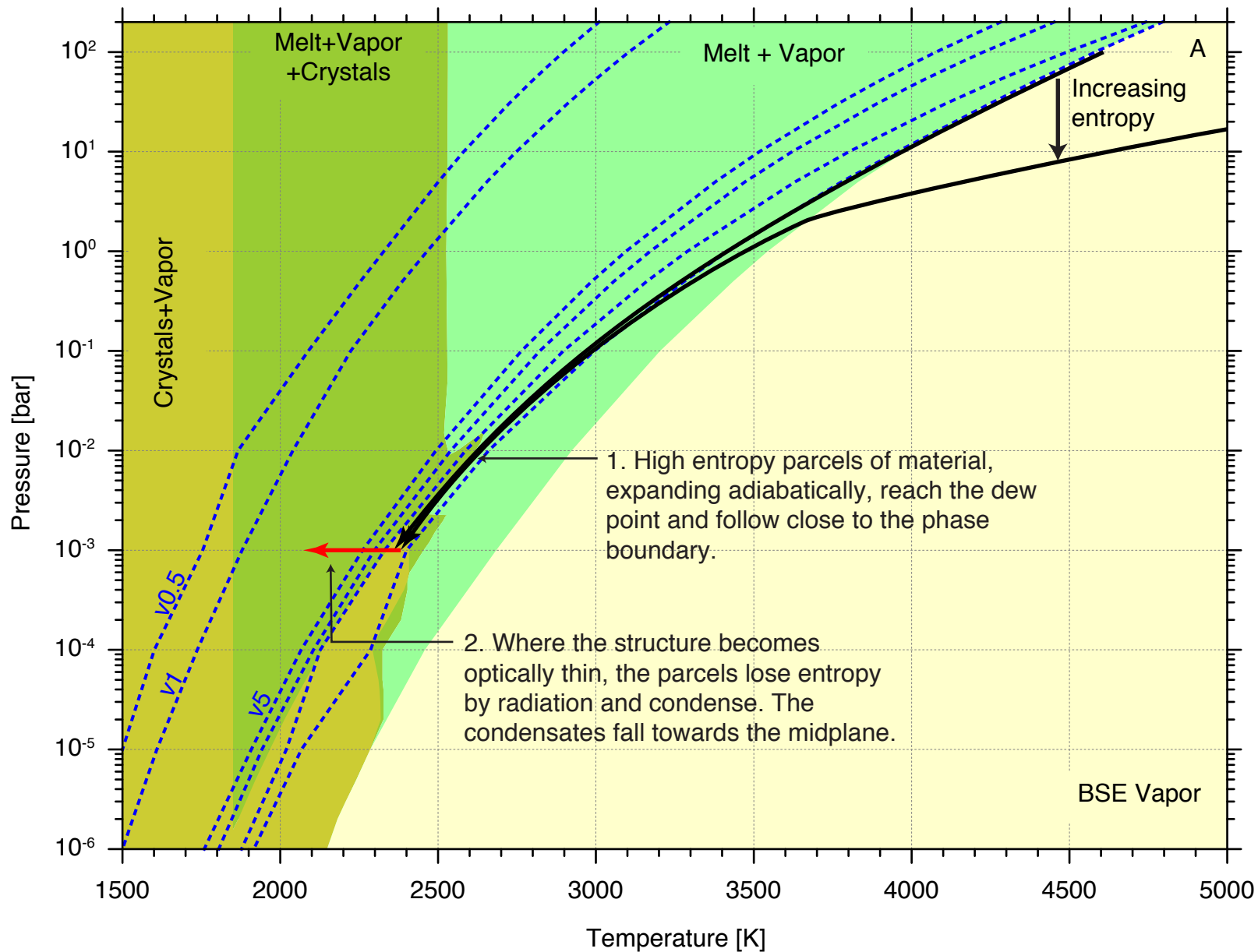


Moon is depleted in moderately volatile and volatile elements

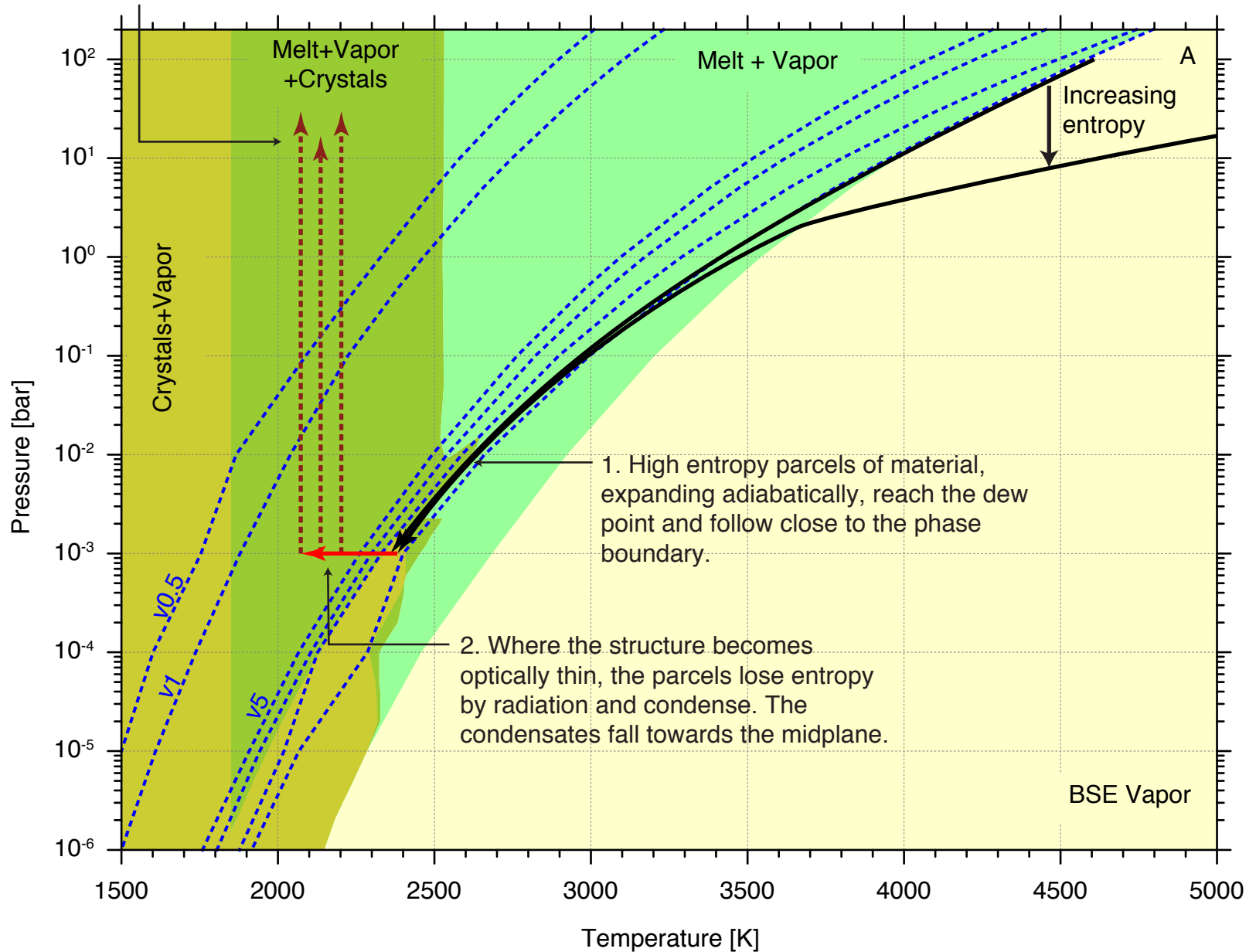
# Bulk Silicate Earth Phase Diagram





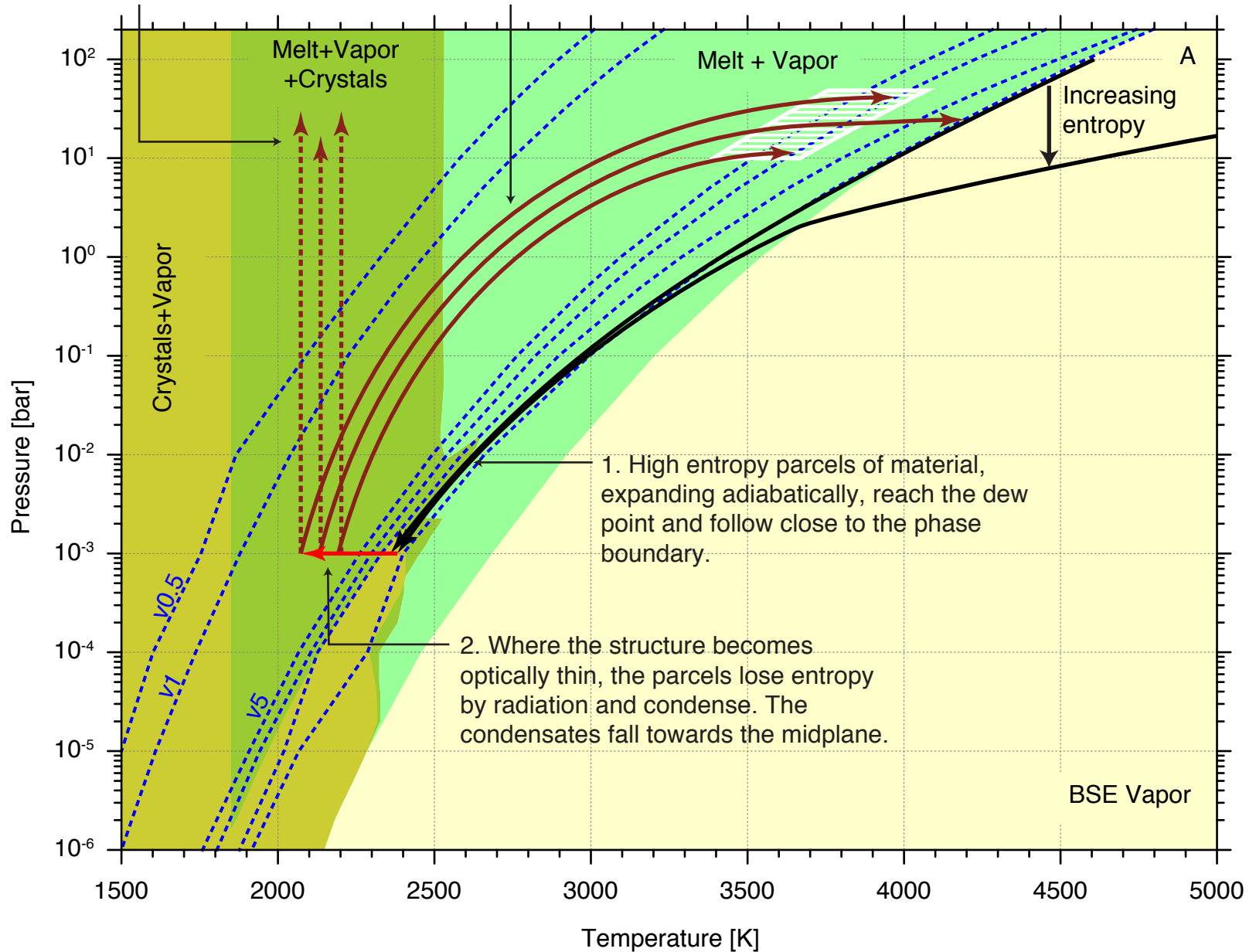


3. If the condensates were thermally isolated, then they would fall on approximately isothermal adiabats.



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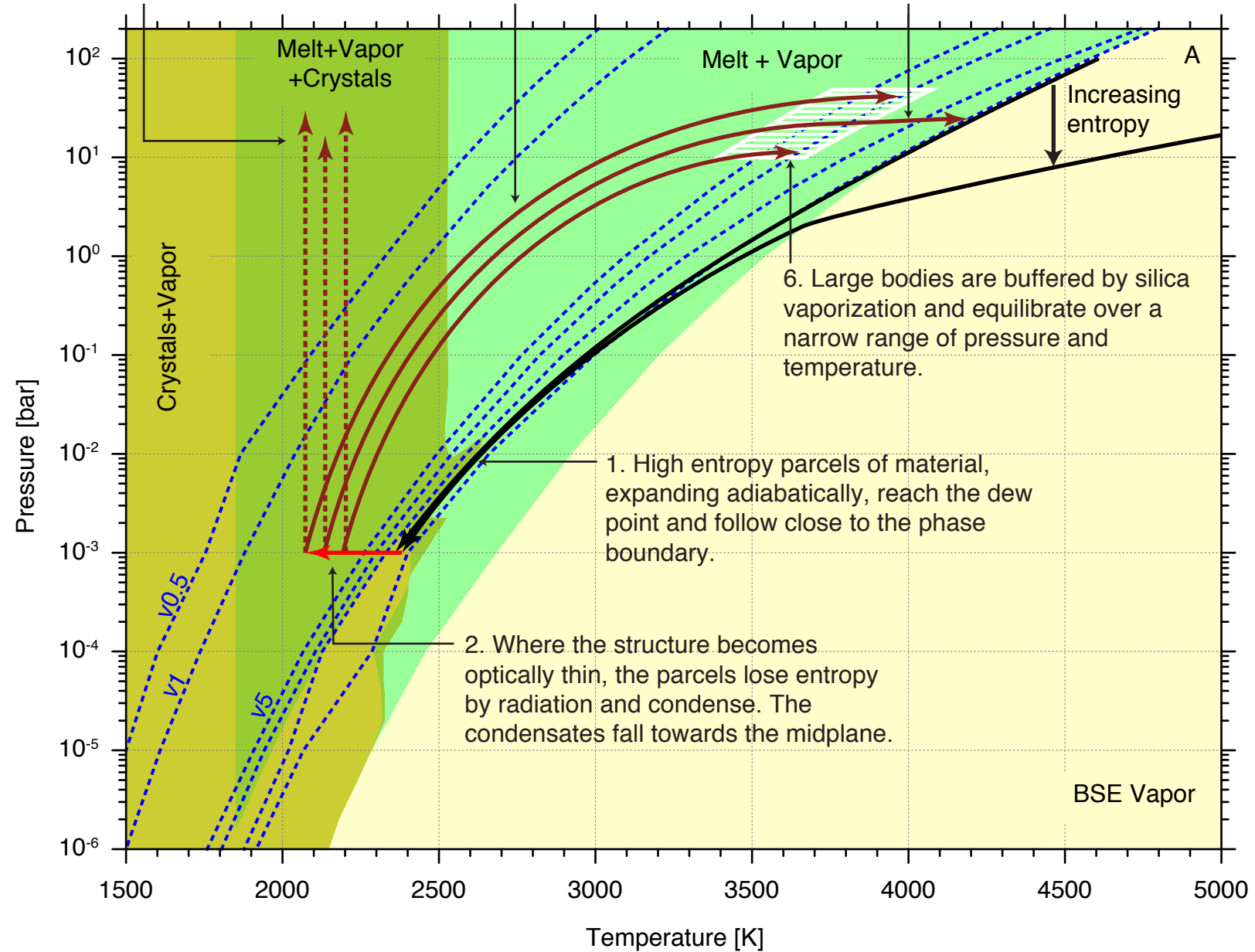
4. Falling condensates are heated by the surrounding gas and partially equilibrate leading to higher temperature paths.



3. If the condensates were thermally isolated, then they would fall on approximately isothermal adiabats.

4. Falling condensates are heated by the surrounding gas and partially equilibrate leading to higher temperature paths.

5. Condensates that are not incorporated into larger bodies vaporize rapidly and their mass is returned to the vapor structure.



Crystals+Vapor

Melt+Vapor  
+Crystals

Melt + Vapor

Increasing entropy

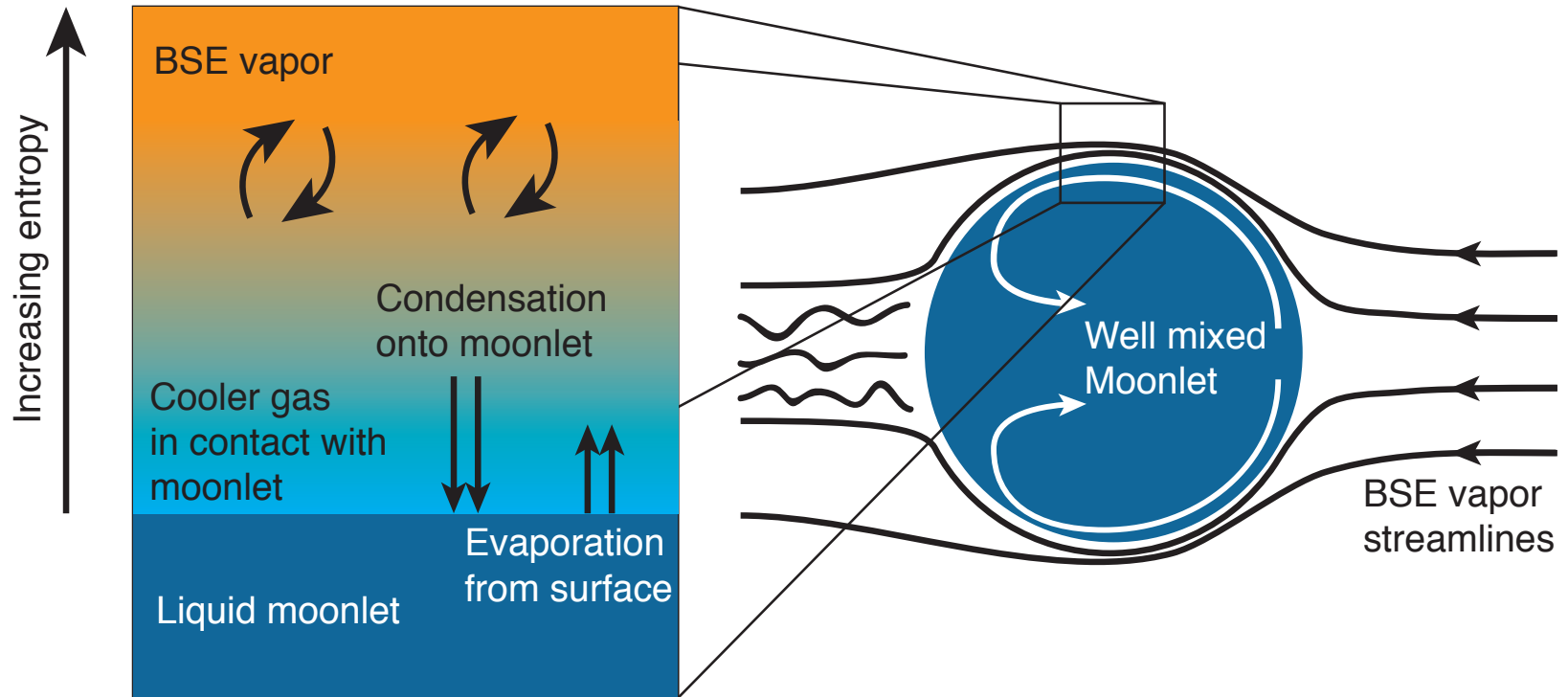
6. Large bodies are buffered by silica vaporization and equilibrate over a narrow range of pressure and temperature.

1. High entropy parcels of material, expanding adiabatically, reach the dew point and follow close to the phase boundary.

2. Where the structure becomes optically thin, the parcels lose entropy by radiation and condense. The condensates fall towards the midplane.

BSE Vapor

# Pressure & Temperature of Lunar Origin

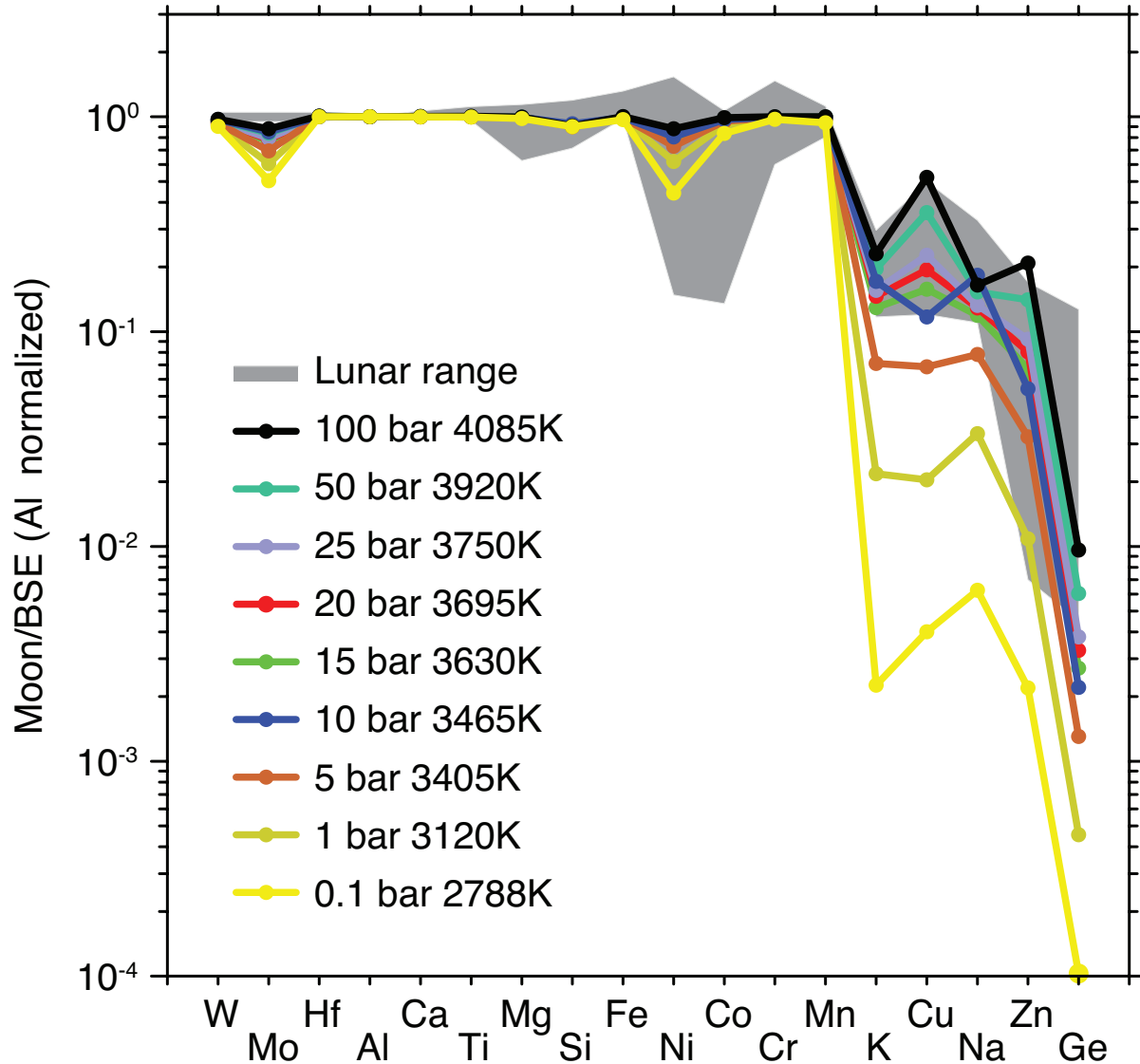


High-energy, high-AM giant impacts generate BSE vapor pressures of **10's bars** beyond the Roche limit. Well-mixed synestia and well-mixed Moon.

The liquid moon is surrounded by hotter BSE vapor. Moon is a cold trap. Moon heats to the **boiling point of silicate (about 10% Si in the vapor)**.



# Predicted Lunar Chemistry

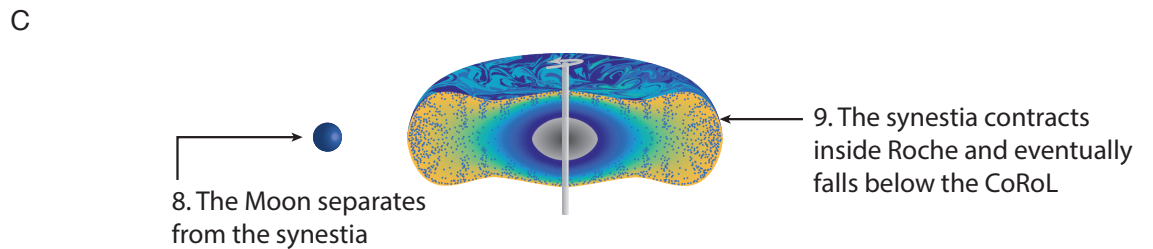
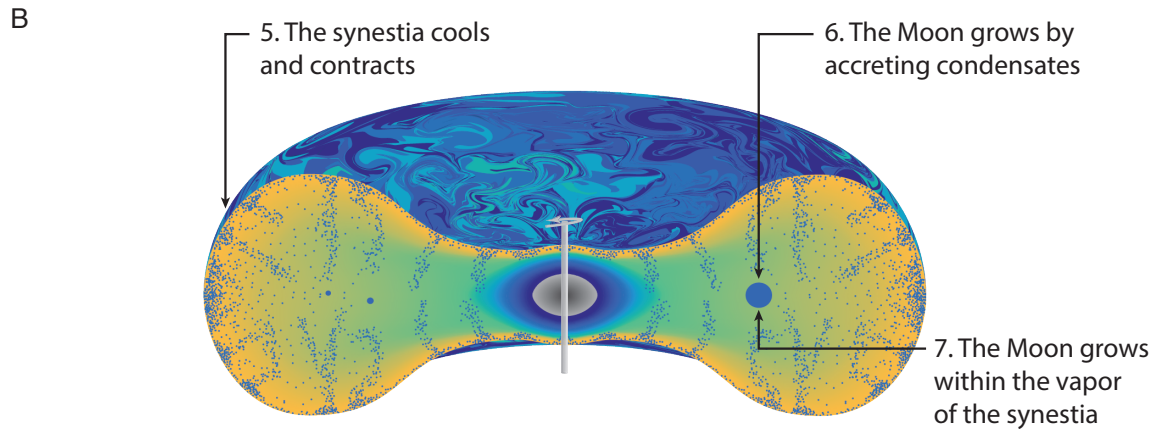
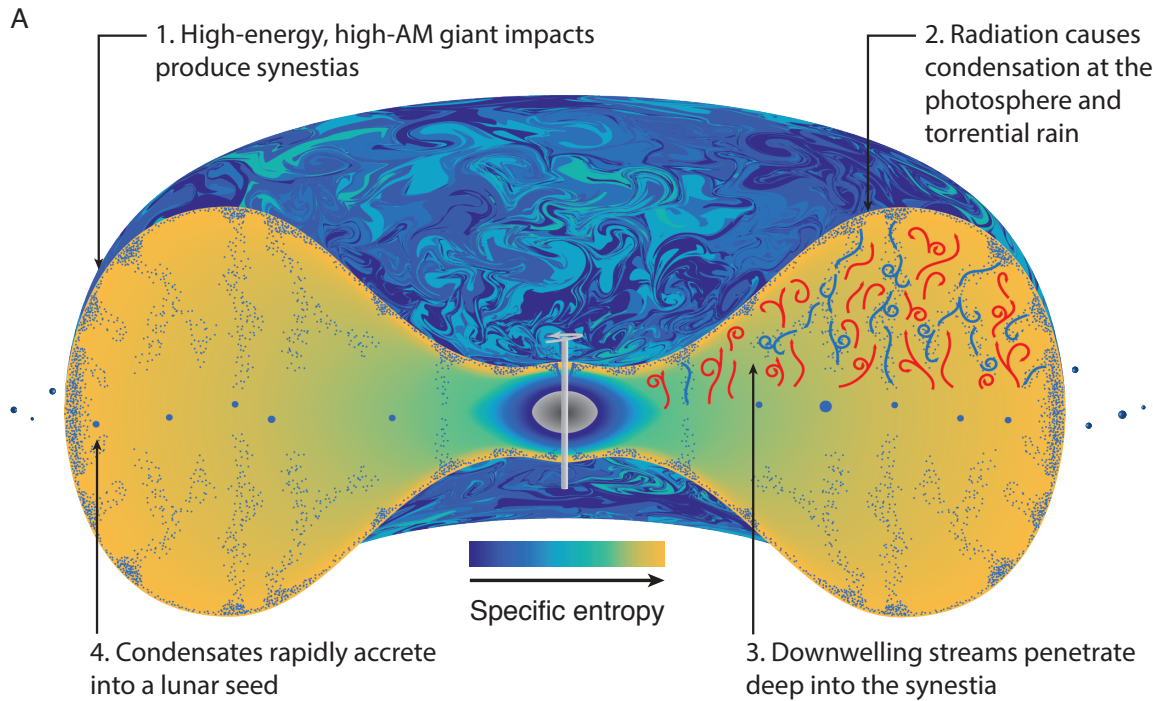


Predicted chemistry at 10's bar and 10% Si in vapor agrees very well with observations

W isotopes similar because well-mixed vapor structure (other isotopes TBD)

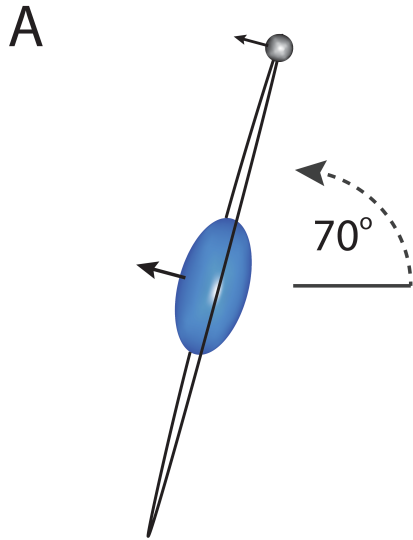
M. Petaev calculations using the GRAINS thermochemical code.

# Summary of Lunar Origin

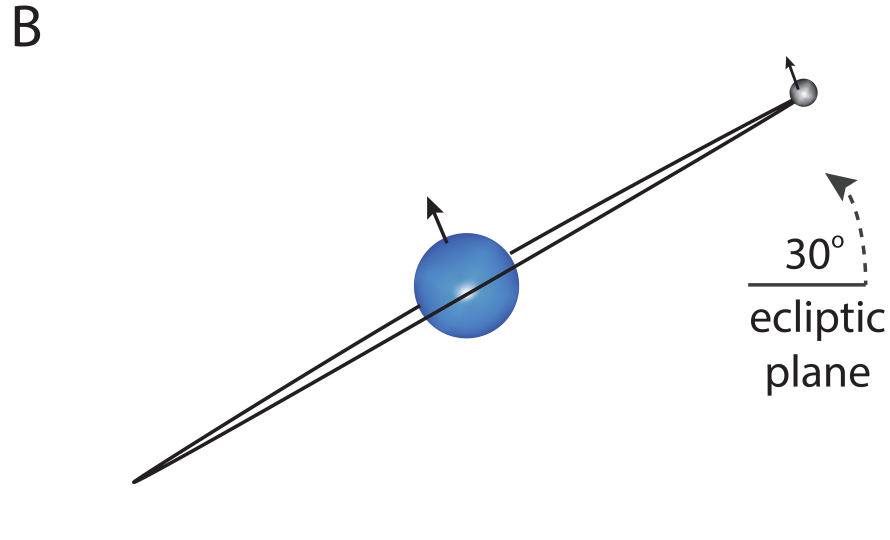


# After making the Moon.....

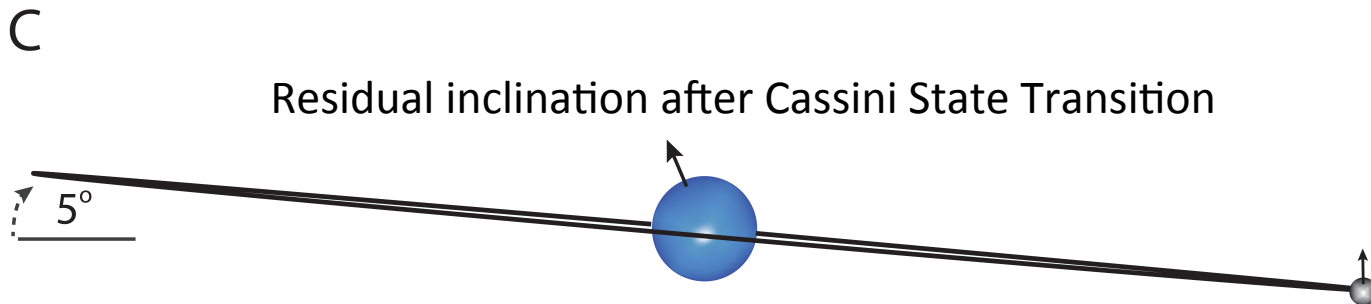
Need to explain present-day orbit (AM and lunar inclination)



After impact, high-obliquity Earth



During LaPlace plane transition, remove AM



Residual inclination after Cassini State Transition

After lunar accretion, angular momentum transferred from Earth-Moon to Sun-Earth system during tidal evolution of the Moon

Ćuk, Hamilton, Lock, Stewart, Nature, 2016