Understanding Properties of Materials under Extreme Conditions with *First-Principles* Methods for ICF/HED Applications

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Laboratory for Laser Energetics University of Rochester

Seminar @ HEDS Center at LLNL

Feb 7th, 2019



A "startup" HEDP-theory group is being built recently at LLE



High-Energy-Density Physics (HEDP) Theory Group

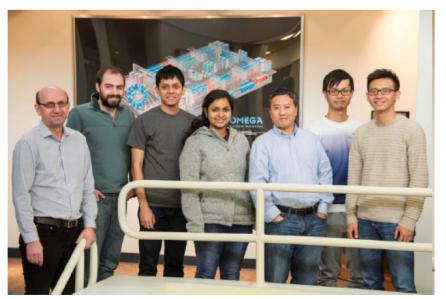
Suxing Hu Group Leade

Group Leader

Scientists Valentin Karasiev

Contents

- What is HEDP/WDM?
- <u>Why do we care about</u> <u>HEDP & WDM?</u>
- <u>Current Research Topics</u>
- <u>First-Principles/</u>
 <u>Ab-Initio Methods for HEDP</u>
- List of Selected Recent
 Publications and Preprints
- <u>Opportunities & Contact</u> <u>information</u>



Graduate Students Yanhao Ding (~2021) Maitrayee Ghosh (~2023) Josh Hinz (~2022) Reetam Paul (~2022) Tian Tang (~2023)

Undergraduate/ High School Interns Barry Xu (Columbia University, 2010) Jesse Pan (Case Western, 2012) Nathan Xu (Univ. Pennsylvania, 2014) Xilin Zhou (Harvard, 2015) Ryan Gao (Princeton, 2016)

We are currently looking for two more scientists to join us!



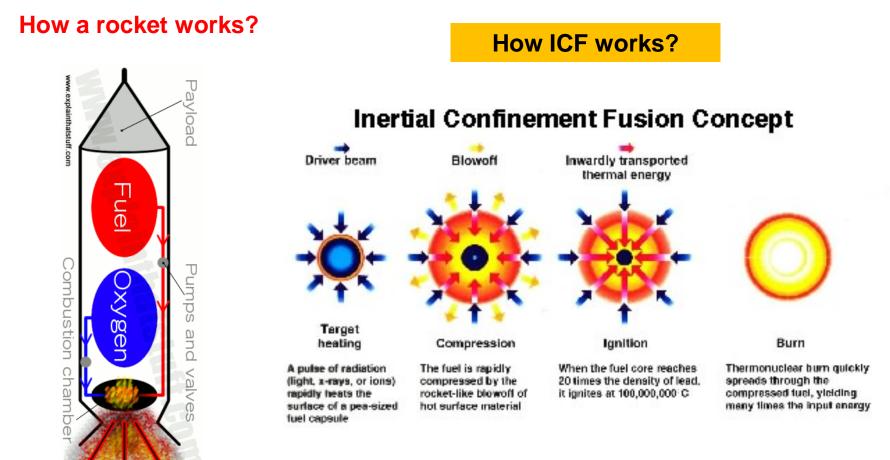
Outline



- Introduction: Why do we care about high-energy-density physics (HEDP) as ICF scientists?
- What are our "first-principles toolkits" to understand HED matter as a quantum many-body system?
 - Density-Functional-Theory (DFT)
 - Path-integral Monte-Carlo (PIMC)
 - Quantum Monte-Carlo (QMC)
- □ *First-principles*-based and *self-consistent* material properties under extreme conditions for ICF/HED applications:
 - What have we learned so far?
 - How do these knowledges impact on the ICF community?
- **Some recent focuses in a broad HEDS arena**
- **Conclusion & Outlook**



Why do we care about HEDP as ICF scientists?

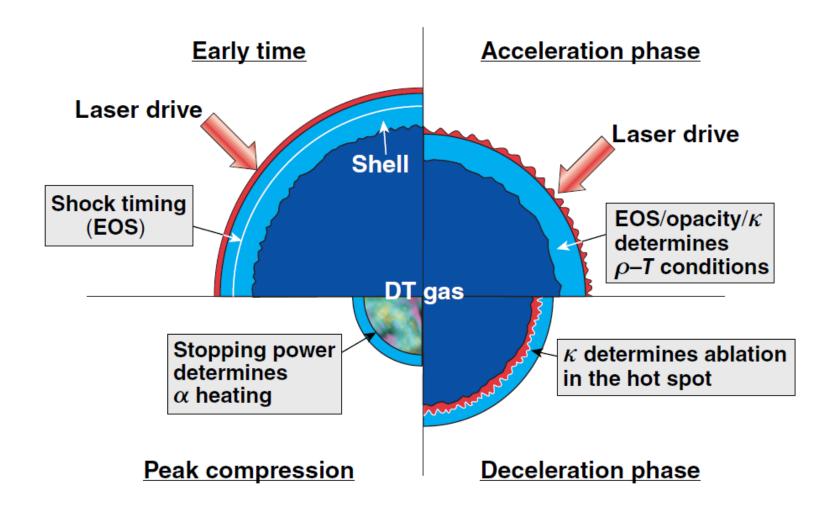


An ICF physicist is also a "rocket scientist"!



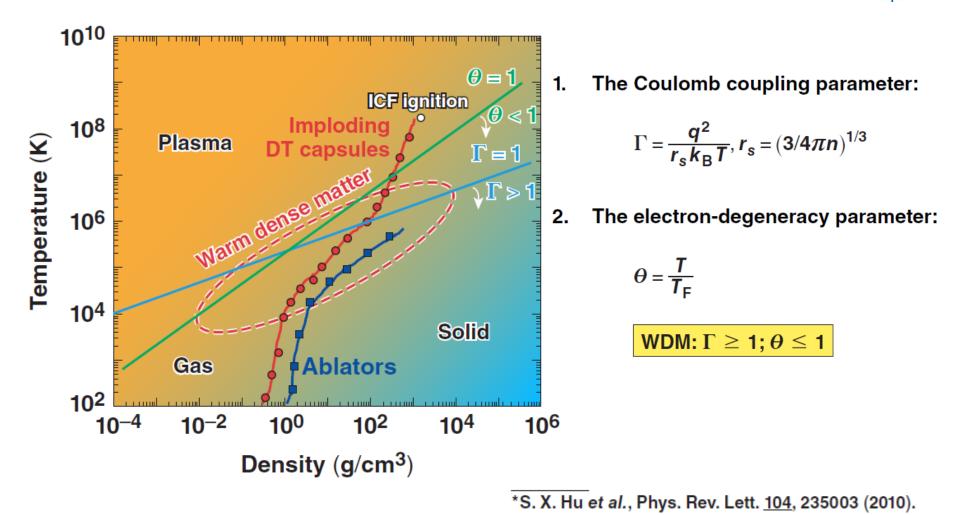
Accurate knowledge of *intrinsic* plasma properties (EOS,* opacity, thermal conductivity, and stopping power) of DT and ablators is required for ICF simulations

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ICF implosions routinely access the WDM regime,* which demands a better understanding of material properties





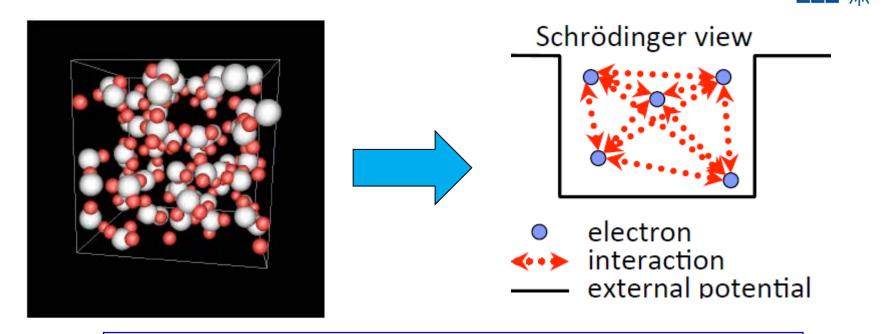
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A view of an HEDP-theorist: Warm-dense matter (dense plasmas) as *quantum many-body systems*



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Quantum many-body Schrödinger Equation

$$\left[-\frac{\hbar^2}{2m}\sum_{i}^{2} \nabla^2 + V(r_{1,r_{2,}}\dots,r_{n})\right]\Psi(r_{1,r_{2,}}\dots,r_{n}) = E\Psi(r_{1,r_{2,}}\dots,r_{n})$$



Quantum many-body Schrödinger Equation: Well-defined equation, but no easy solution



Quantum Mechanics

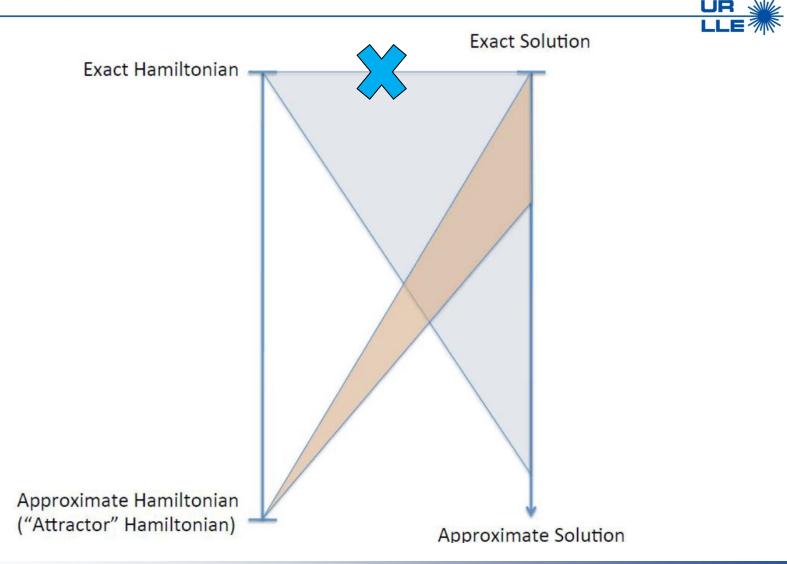
Dirac (1929)

"The general theory of quantum mechanics is now almost complete... The underlying physical laws necessary for the mathematical theory of a large part of physics and the whole of chemistry are thus completely known, and the difficulty is only that the exact application of these laws leads to equations much too complicated to be soluble."

P.A.M. Dirac, Proc. R. Soc. London Ser. A 123, 714 (1929).



How can we learn the many-body physics and chemistry from the Quantum Mechanics equations?





Our "first-principles toolkits" for quantum many-body systems



>Density-Functional-Theory (DFT)*

>Path-integral Monte-Carlo (PIMC)**

>Quantum Monte-Carlo (QMC)***

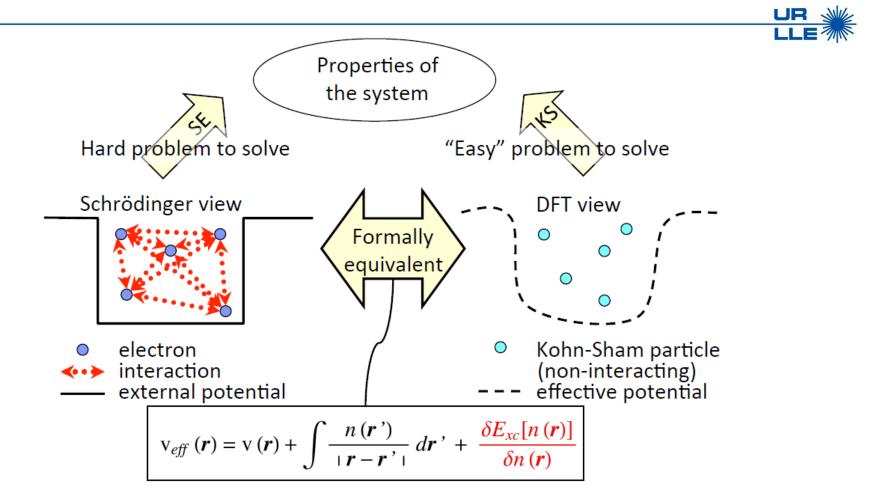
* W. Kohn and L. J. Sham, Phys. Rev. 140, A1133 (1965).

** D. M. Ceperley, Rev. Mod. Phys. 67, 279 (1995).

*** E. Fermi & R. D. Richtmyer (1948) and many papers afterwards [e.g., R. C. Clay, M. Holzmann, D. M. Ceperley, and M. A. Morales, Phys. Rev. B 93, 035121 (2016).]



DFT versus the Schrödinger Equation



All many-body effects are included in the effective potential via the Exchange-Correlation functional, $E_{xc}[n(\mathbf{r})]$.

*Courtesy of Ann Mattsson

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Kohn-Sham equations:



$$\left(-\frac{\hbar^2}{2\,m}\,\nabla^2 + \mathbf{v}_{eff}\left(\mathbf{r}\right)\right)\psi_{\nu}\left(\mathbf{r}\right) = \epsilon_{\nu}\,\psi_{\nu}\left(\mathbf{r}\right)\,\nu = 1,\,2,\,...,\,N$$

$$n(\mathbf{r}) = \sum_{\nu=1}^{N} |\psi_{\nu}(\mathbf{r})|^{2}$$

$$v_{eff}(\mathbf{r}) = v(\mathbf{r}) + \int \frac{n(\mathbf{r'})}{|\mathbf{r} - \mathbf{r'}|} d\mathbf{r'} + \frac{\delta E_{xc}[n(\mathbf{r})]}{\delta n(\mathbf{r})}$$

If we had the divine exchange-correlation functional, self-consistently solving these equations would give exactly the same density as the Schrödinger Equation, and thus via the HK theorem, we should be able to extract all information about the system.



Finding the best exchange-correlation functional is the key to have made DFT practical

LDA for V_{xc}

	Alex Zunger			All	Since 2013
	University of Colorado ,Boulder ,Colorado.Renewable and Sustainable Energy Institute	nable	Citations h-index i10-index	88351 136 613	28397 77 366
	Physics Material Science nano science photovoltaics				
TITLE				CITED BY	YEAR
Self-interaction electron system JP Perdew, A Zun Physical Review B	ger	oproximations for		$\frac{18405}{V_{\chi_C}}$	1981
	John P. Perdew				

Since 2013 All 234190 110367 Citations **Temple University** h-index 103 65 density functional theory i10-index 275 189 materials theory quantum chemistry TITLE CITED BY YEAR Generalized gradient approximation made simple 86940 1996 JP Perdew, K Burke, M Ernzerhof

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JP Perdew, K Burke, M Ernzerhof Physical review letters 77 (18), 3865

The journey of searching for more and more accurate XC-functionals still continues: Meta-GGA, Hybrid, temperature-dependent,.....



Quantum Molecular Dynamics (QMD) method is based on the thermal density-functional theory (DFT)*

The thermal-DFT is a "mean-field" theory of many-electron system at finite temperatures:

$$\left\{-\frac{1}{2}\Delta + V_Z(r) + V_H[n](r) + V_{xc}[n](r)\right\}\psi_i = \epsilon_i\psi_i$$

n(r) = $\sum_{i=1}^N f_i |\psi_i(r)|^2$, $V_H[n](r) = \int \frac{n(r')}{|r-r'|} dr'$

- □ Since V_H and V_{xc} terms depend on electron density n(r), which depends on the ψ_i , the thermal-DFT equation can be solved in a self-consistent (i.e., *iterative*) way, once the V_{xc} is known!
- The resulting electronic force together with ionic forces will drive the classical ions to move, through the Newton's equation, in the MD simulations.

*P. Hohenberg and W. Kohn, Phys. Rev. <u>136</u>, B864 (1964).
W. Kohn and L. J. Sham, Phys. Rev. <u>140</u>, A1133 (1965).
N. D. Mermin, Phys. Rev. <u>137</u>, A1441 (1965).



A variety of material properties can be self-consistently calculated from QMD simulations

- EOS are direct outputs from QMD simulations
- Transport properties can be calculated using the Kubo-Greenwood formalism:

$$L_{ij}(\omega) = \frac{2\pi (-e)^{4-i-j}}{3Vm_e^2 \omega} \sum_{mn} \mathbf{F}_{mn} \left| D_{mn} \right|^2$$

$$\times \left(\frac{E_m + E_n}{2} - H\right)^{i+j-2} \delta(E_m - E_n - \hbar \omega),$$

 Thermal/Electrical conductivities and optical absorption coefficients can be derived from these Onsager coefficients L_{ii}(ω):

$$\sigma = L_{11}; \ \kappa = \frac{1}{T} \left(L_{22} - \frac{L_{12}^2}{L_{11}} \right); \ \alpha_m(\omega) = \frac{\alpha_K(\omega)}{\rho} = \frac{4\pi \overline{\sigma}_1(\omega)}{c \times \overline{n}(\omega)} \times \frac{1}{\rho}$$



PIMC*, based on the convolution of density matrix, uses Monte-Carlo method to efficiently evaluate multi-dimensional integrations

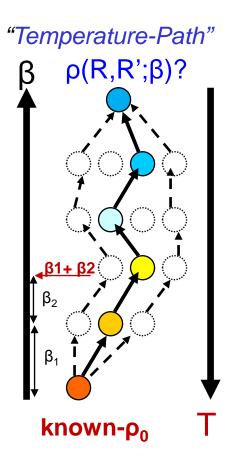
 Density-matrix ρ(R,R';T), introduced by <u>John von</u> <u>Neumann</u> in 1927, describes the statistical distribution of a quantum system in thermal equilibrium:

$$\rho(R, R'; T) = < R \mid e^{-\bar{H}/kT} \mid R' > = \sum_{n} \varphi_{n}(R) \varphi_{n}(R') e^{-E_{n}/kT}$$

 The convolution property of ρ(R,R';β) can be written as:

$$\rho(R, R'; \beta_1 + \beta_2) = < R | e^{-(\beta_1 + \beta_2)\bar{H}} | R' >$$

$$= \int dR_1 \rho(R, R_1; \beta_1) \rho(R_1, R'; \beta_2)$$
with $\beta_1 = 1/kT_1$ and $\beta_2 = 1/kT_2$.



Difficult (if not impossible) to obtain transport and optical properties

*D. M. Ceperley, Rev. Mod. Phys. <u>67</u>, 279 (1995).



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First-principles-based and self-consistent material properties under extreme conditions for ICF/HED applications:

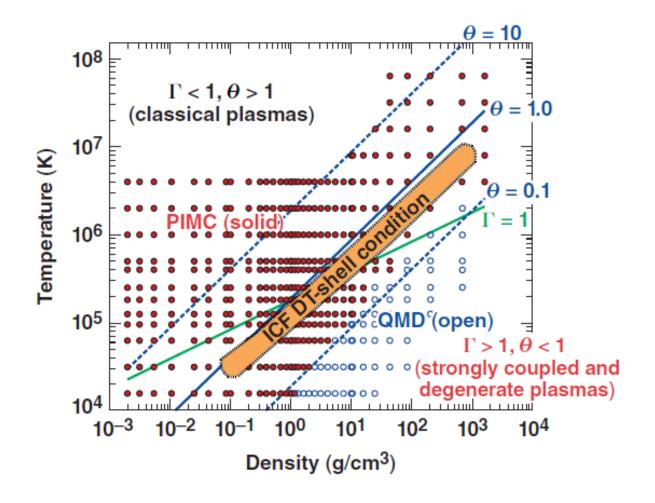
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We studied the properties of deuterium* in a wide range of conditions by combining PIMC and QMD methods

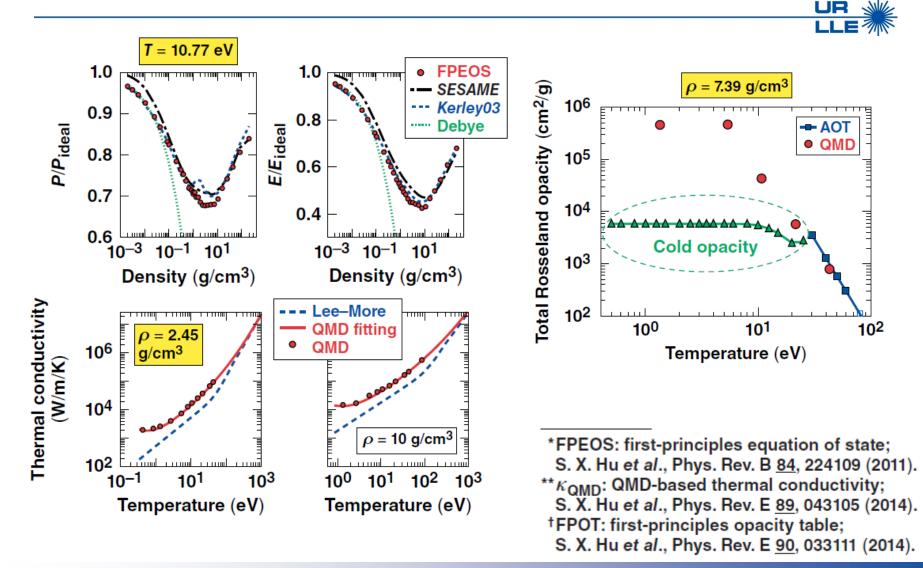


*S. X. Hu et al., Phys. Rev. Lett. 104, 235003 (2010).

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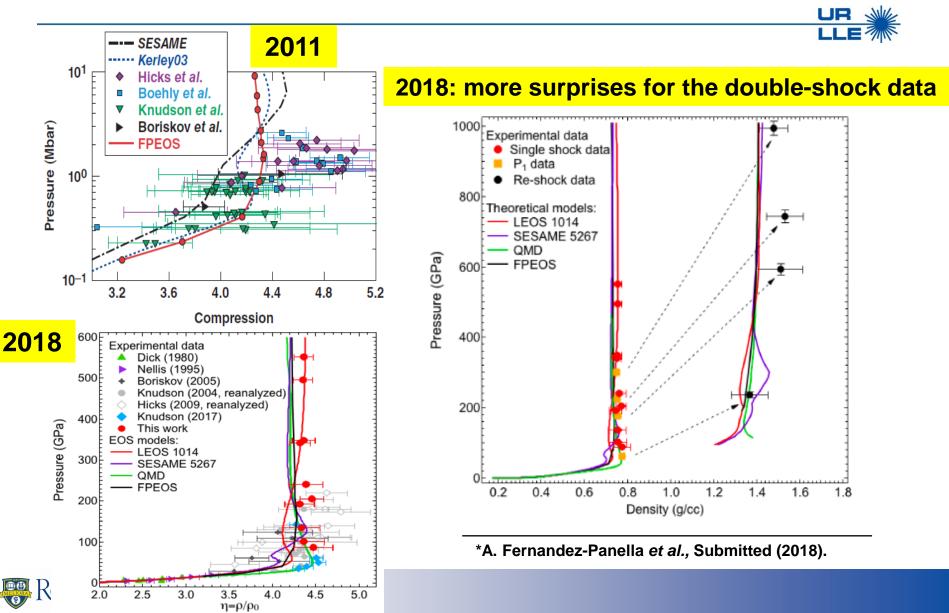


Significant differences have been identified for warm dense deuterium when FPEOS,* κ_{QMD} ,** and FPOT[†] are compared with traditional models

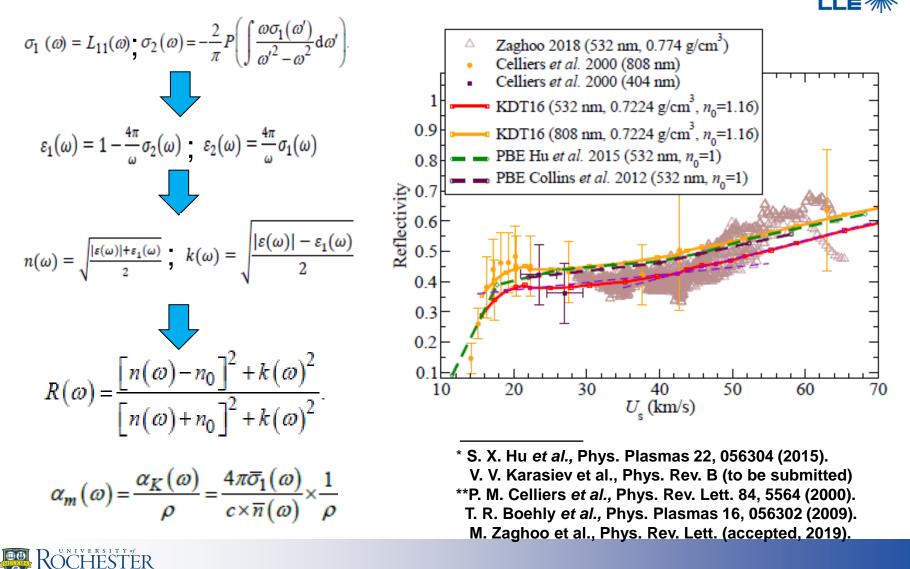


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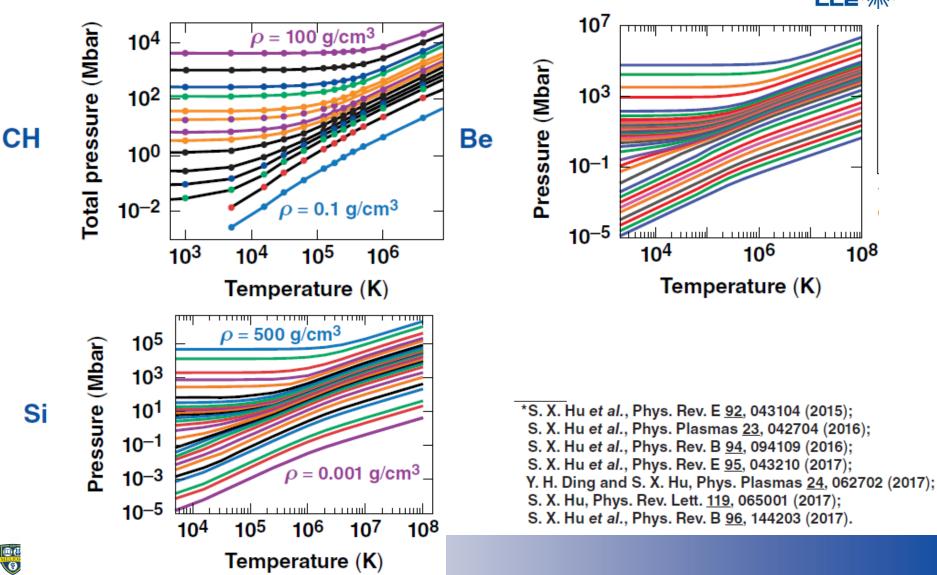
New experiments* continue to challenge our understanding of the behavior of deuterium at WDM conditions



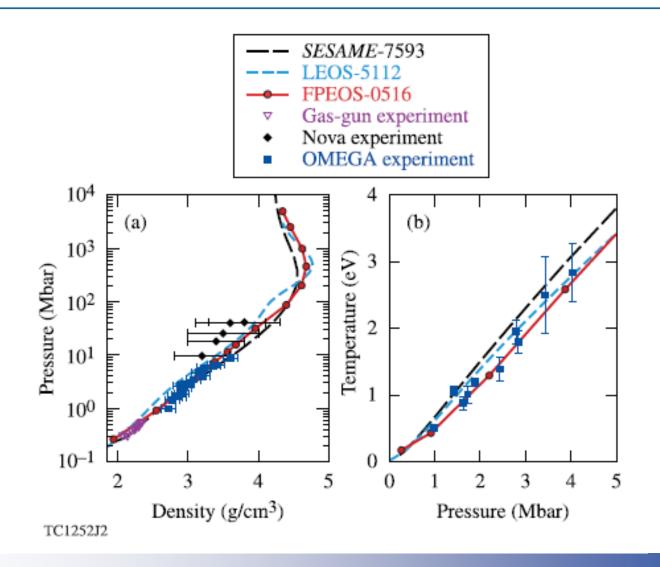
The QMD-predicted reflectivity* along the Hugoniot of deuterium agreed with NOVA and OMEGA experiments**



A wide range of material conditions of ICF-relevant ablators* has also been studied by KSMD+OFMD calculations in their liquid phase UR



The calculated principal Hugoniot* of CH from FPEOS has been well compared with experiments

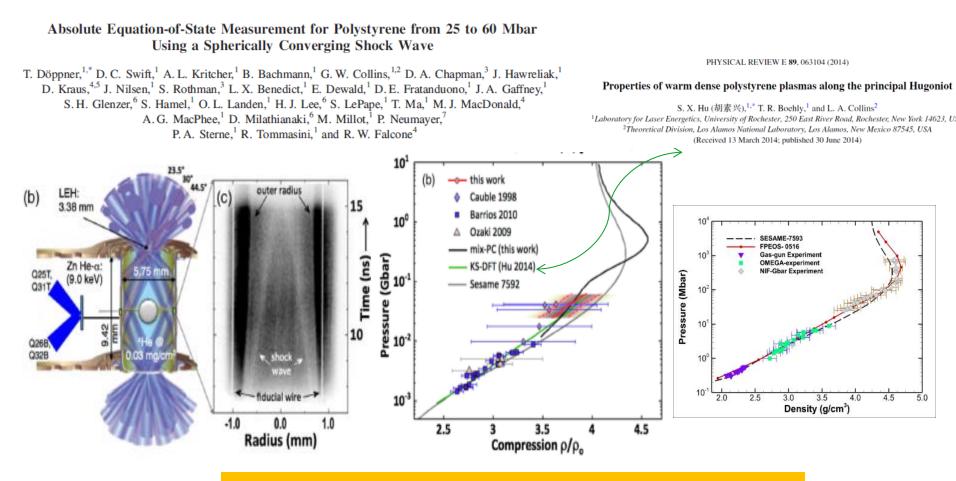


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Recent EOS measurements at high pressures on NIF are in better agreement with FPEOS than SESAME-7592

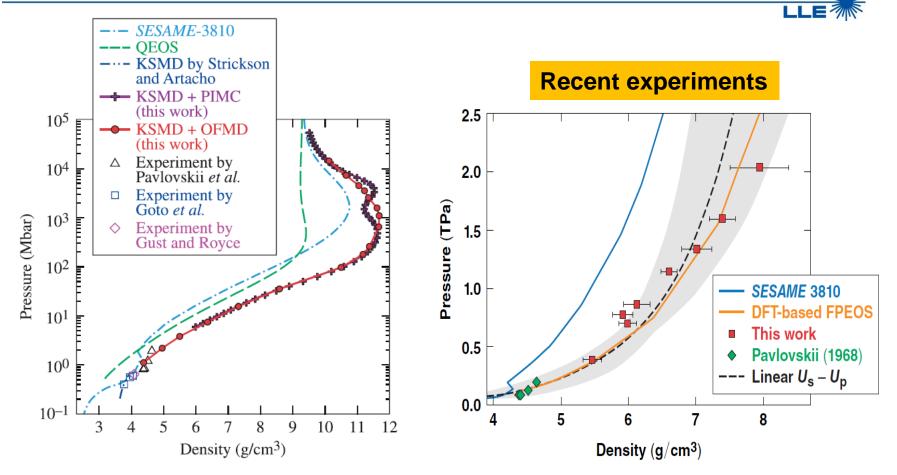
PHYSICAL REVIEW LETTERS 121, 025001 (2018)





Thanks to Phil Sterne for file-format conversion, the FPEOS tables can now be accessed by HYDRA!

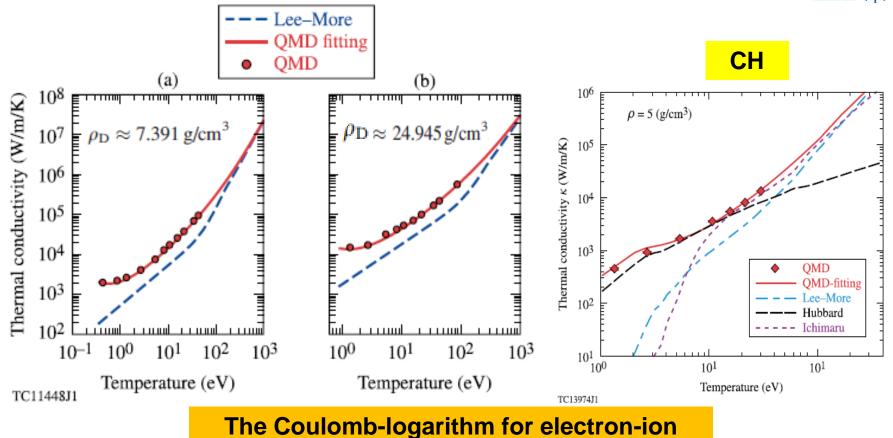
One more example: Our QMD study* has predicted a much softer Hugoniot of Si, which is proven to be true by recent experiments** on OMEGA-EP



*S. X. Hu *et al.,* Phys. Rev. B 94, 094109 (2016). ** B. Henderson et al., talk at APS-DPP (2017).



Thermal conductivity models (κ_{QMD}) based on QMD calculations* has also been developed for D₂ and ablator materials [adopted into LANL's code: *Xrage***]



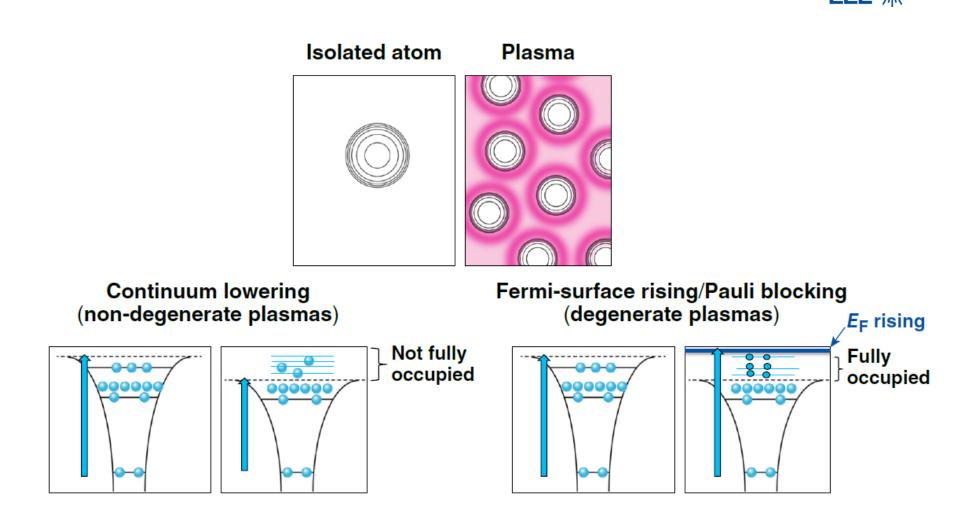
collisions is reduced in WDM condition

*S. X. Hu *et al.,* Phys. Plasmas 23, 042704 (2016).

** B. M. Haines et al., Phys. Plasmas 26, 012707 (2019).

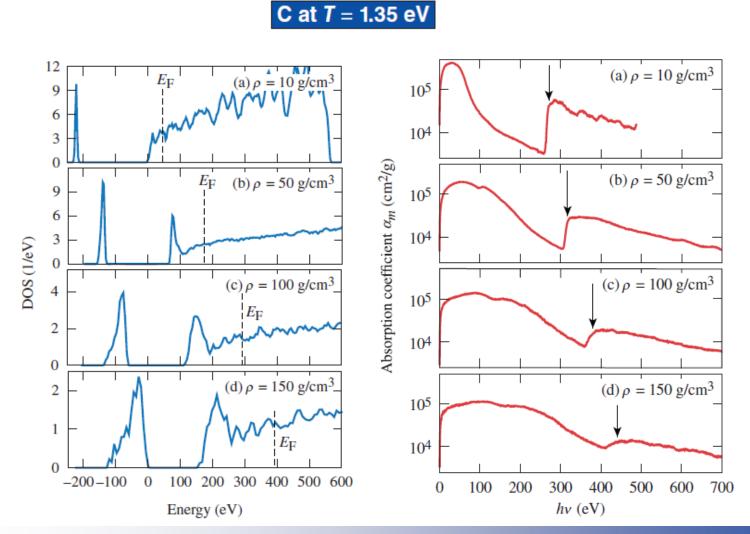


QMD calculations can also give us self-consistent optical properties of materials under HED conditions: *K-edge shifting as an example*



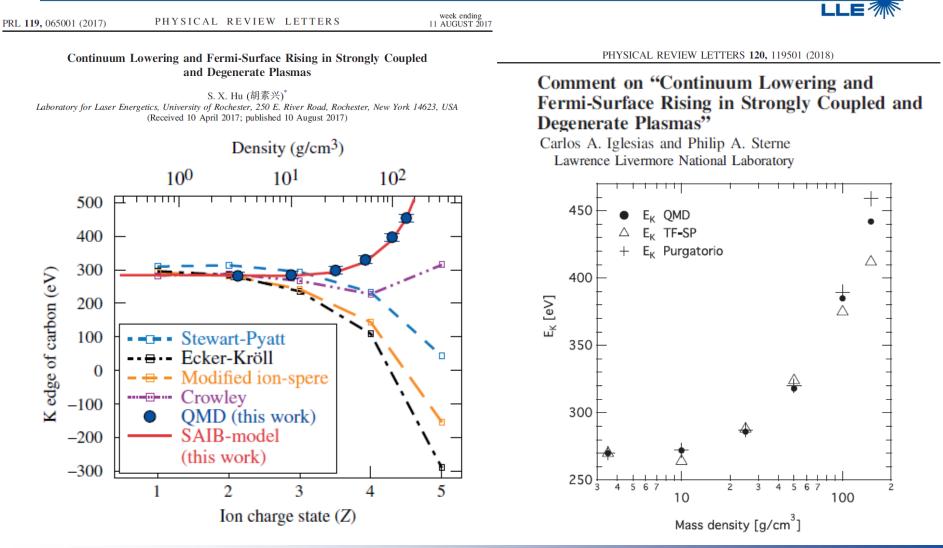


Both continuum-lowering and Fermi-surface-rising effects can be naturally included in QMD simulations



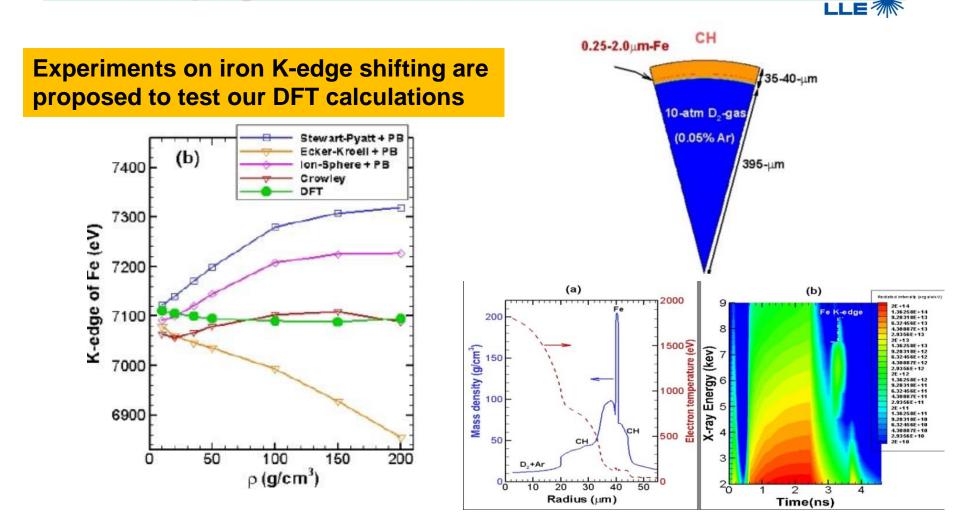
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The continuum-lowering and Fermi-surface-rising (Pauli-blocking) can explain the K-edge up-shifting in strongly-coupled and degenerate dense plasmas



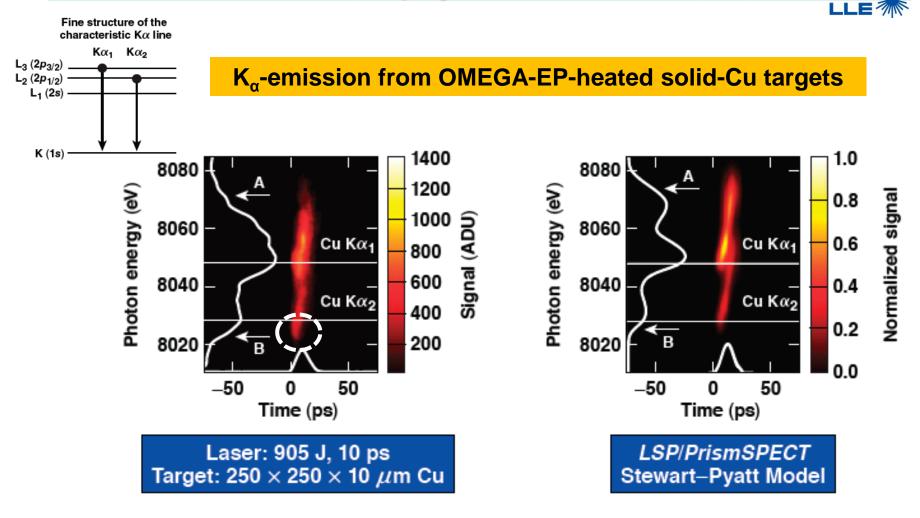
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How our physics understanding may evolve for high-Z materials is waiting to be seen form our ExtremeDFT LBS campaigns





In addition, some existing experimental data* also indicated that traditional plasma-physics models do not catch all essential physics in HED conditions



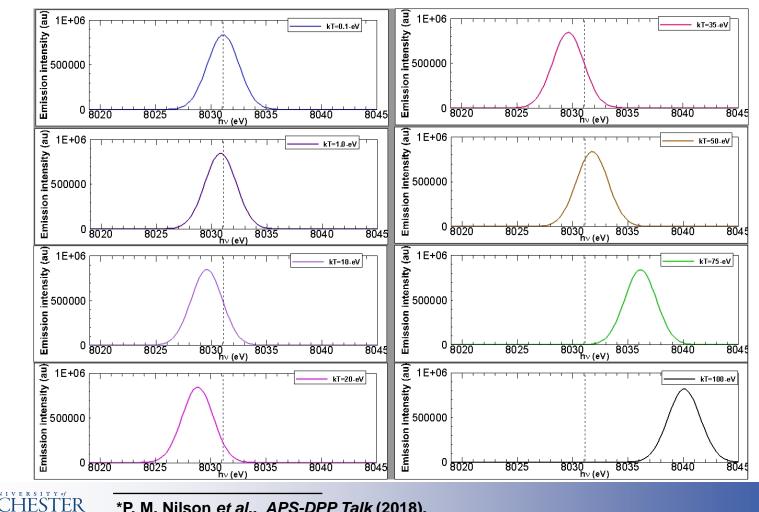
*P. M. Nilson et al., APS-DPP Talk (2018).



Preliminary DFT calculations show the red-shifts of Kα emission observed in experiment* when the target passes through warm-dense matter (WDM) regime

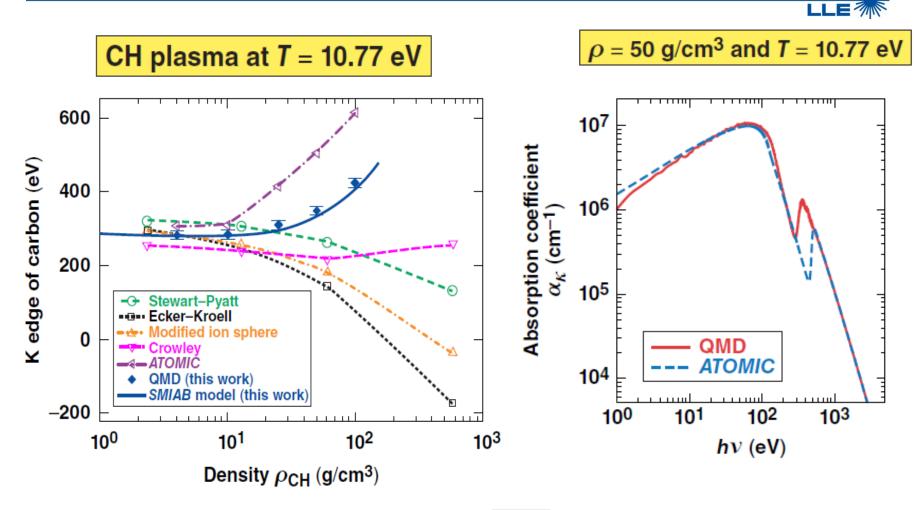
DFT-predicted K_α-line shifts in OMEGA-EP-heated solid-Cu target

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*P. M. Nilson et al., APS-DPP Talk (2018).

Another challenge for traditional physics models is how to handle the mixture in dense plasmas (e.g., CH)



*S. X. Hu et al., Phys. Rev. B <u>96</u>, 144203 (2017). **N. R. Shaffer et al., High Energy Density Phys. <u>23</u>, 31 (2017).



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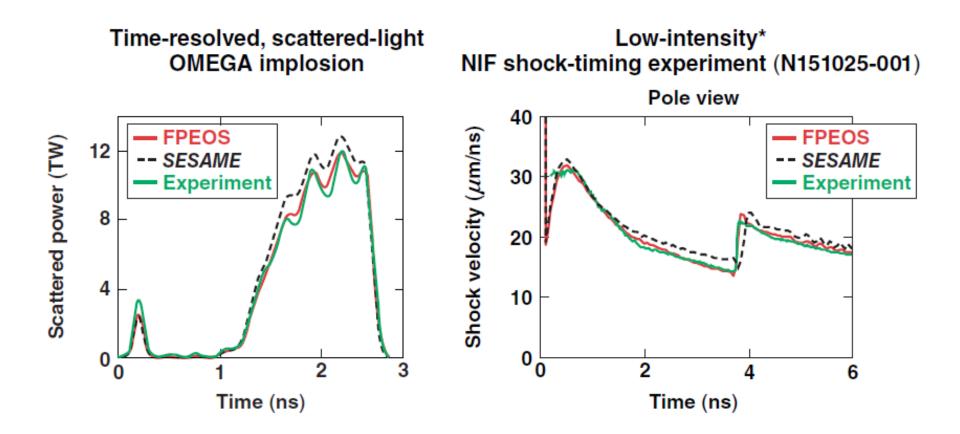
What have we learned so far?

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- Some recent focuses in a broad HEDS arena
- **Conclusion & Outlook**



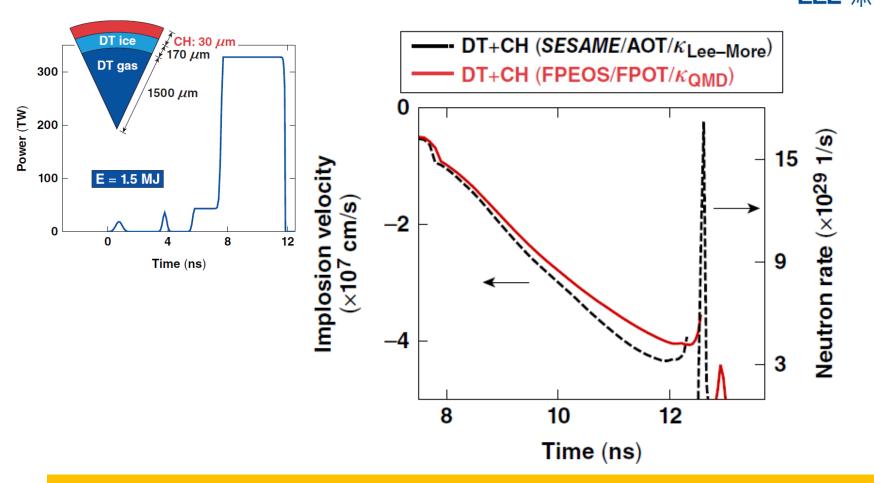
Several different experimental observables show better agreement with FPEOS than SESAME EOS for CH



*P. B. Radha et al., "Shock Velocity Measurements at the National Ignition Facility," to be submitted to Physical Review E.



How did these first-principles properties of HED plasmas affect ICF target designs?

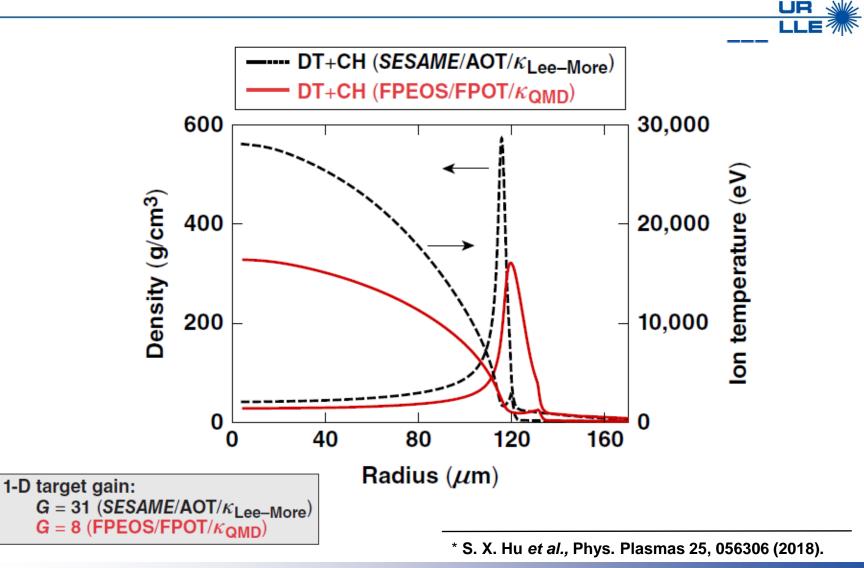


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The major differences are due to: DT-EOS, DT-Opacity, and CH-EOS



Significant variations have been seen in direct-drive ICF target designs with first-principles plasma properties





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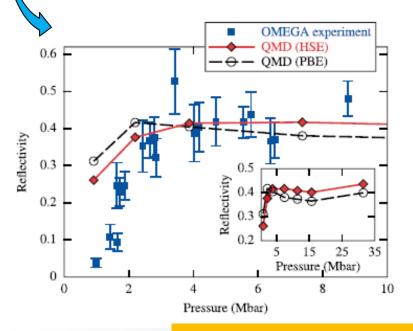
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Conclusion & Outlook



What are the current limits of DFT? How can we improve it for better understanding HEDS?

- Most of the current exchange-correlation functionals underestimate band-gaps of materials*;
- Current exchange-correlation functionals do NOT have temperature dependence*;
- Current DFT implementations are using plane-wave basis and pseudopotentials, which have *frozen* core-electrons.



PHYSICAL REVIEW LETTERS 120, 076401 (2018)

Valentin V. Karasiev,^{1,2,*} James W. Dufty,³ and S. B. Trickey¹ ¹*Quantum Theory Project, Department of Physics and Department of Chemistry, University of Florida, P.O. Box 118435, Gainesville, Florida 32611-8435, USA* ²*Laboratory for Laser Energetics, University of Florida, P.O. Box 118435, Gainesville, Florida 32611-8435, USA*

Nonempirical Semilocal Free-Energy Density Functional

for Matter under Extreme Conditions

(Received 19 December 2016; revised manuscript received 30 August 2017; published 14 February 2018)

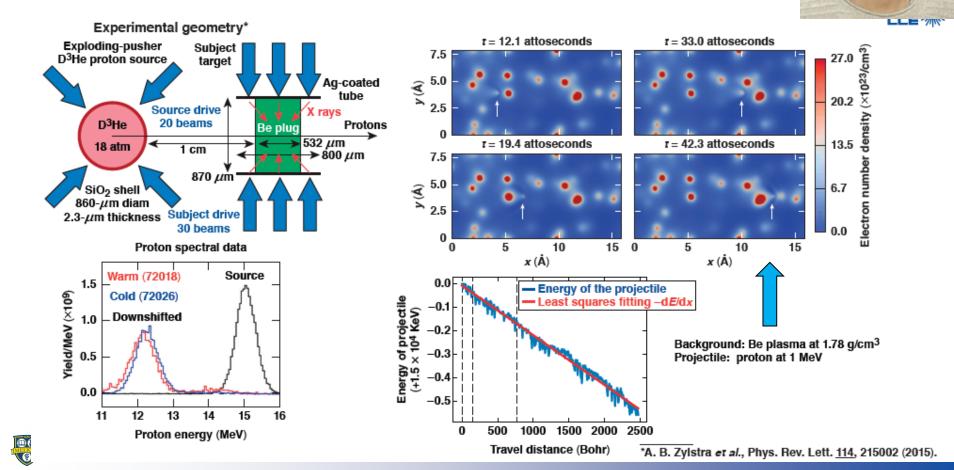
Realizing the potential for predictive density functional calculations of matter under extreme conditions depends crucially upon having an exchange-correlation (XC) free-energy functional accurate over a wide range of state conditions. Unlike the ground-state case, no such functional exists. We remedy that with systematic construction of a generalized gradient approximation XC free-energy functional based on rigorous constraints, including the free-energy gradient expansion. The new functional provides the correct temperature dependence in the slowly varying regime and the correct zero-T, high-T, and homogeneous electron gas limits. Its accuracy in the warm dense matter regime is attested by excellent agreement of the calculated deuterium equation of state with reference path integral Monte Carlo results at intermediate and elevated T. Pressure shifts for hot electrons in compressed static fcc Al and for low-density Al demonstrate the combined magnitude of thermal and gradient effects handled well by this functional over a wide T range.



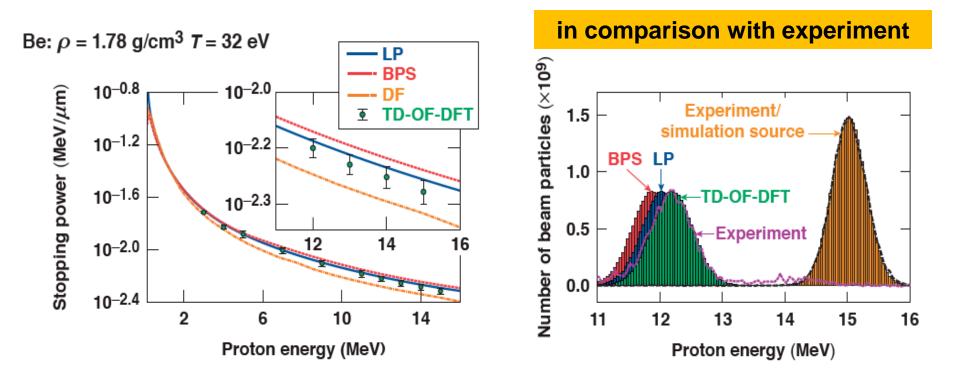
These efforts are also supported by an NSF grant

Time-Dependent Orbital-Free DFT (TD-OF-DFT)code has been developed in our group to understand stopping-power of warm-dense plasmas

proton stopping in warm-dense Be (solid @ kT=32-eV)



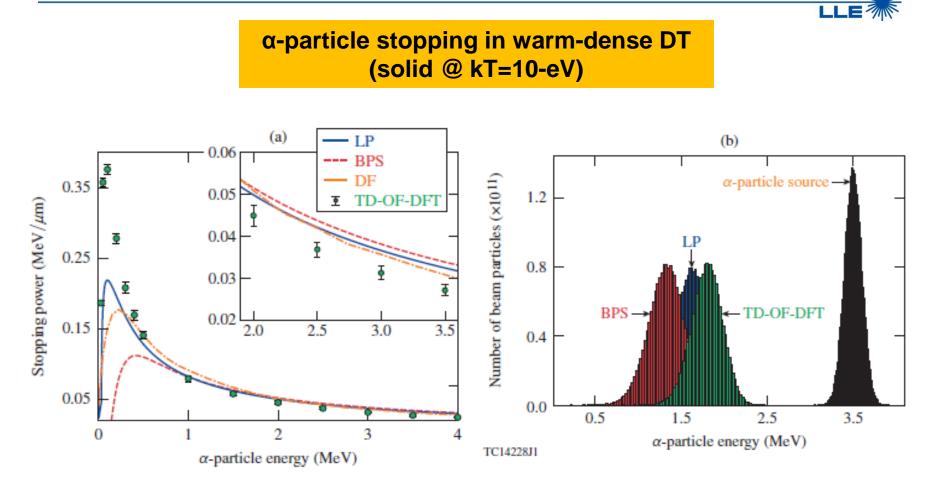
The TD-OF-DFT-calculated proton stopping power in high velocities in comparison with three stopping-power models



The stopping power calculated by TD-OF-DFT is slightly lower than predictions of the LP and BPS models by ~5% and ~11%, respectively, and higher than predicted by DF by 20%.



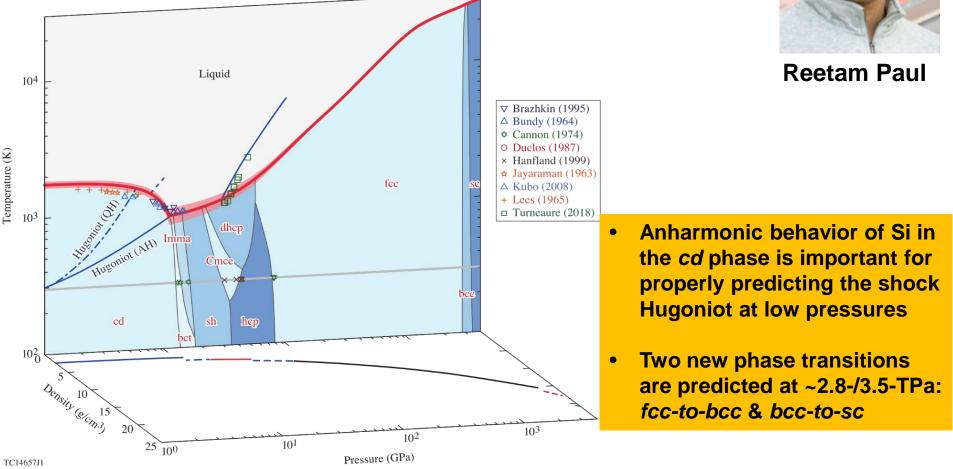
Ab-initio TD-OF-DFT calculations* indicated up to ~25% lower α-particle stopping-power in warm-dense DT than current models



* Y. H. Ding , A. J. White, S. X. Hu, O. Certik, and L. A. Collins, Phys. Rev. Lett. 121, 145001 (2018).



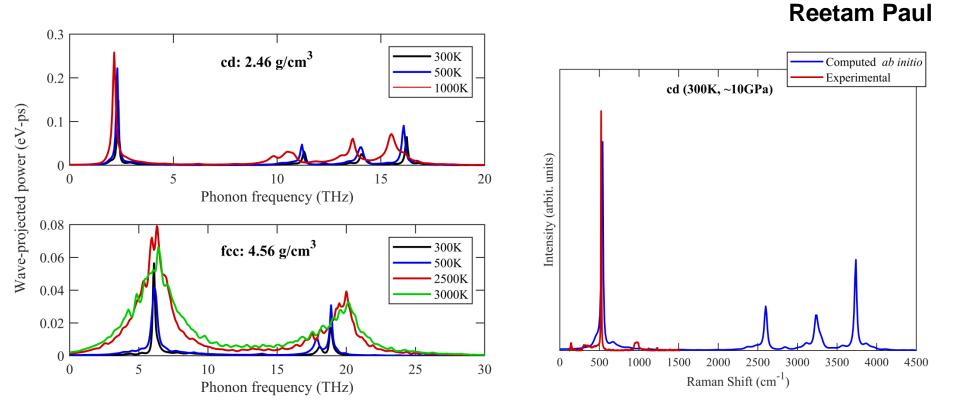
High-pressure phase diagram of silicon up to ~4-TPa has been charted from *first-principles* DFT + Phonon-dynamics calculations*



* R. Paul, S. X. Hu, V. V. Karasiev, Phys. Rev. Lett. (submitted)

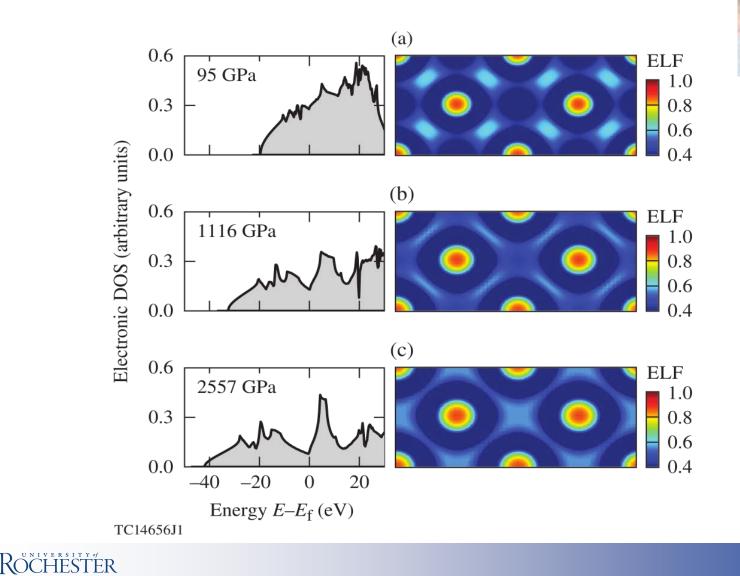


The phonon spectra (of ion vibration modes), a characteristic of different phases, can be picked up by Raman scattering measurements





Under high pressures up to ~4-Tpa, silicon is still a metallic system even though interstitial electron localization appears (hydride-like)





Reetam Paul

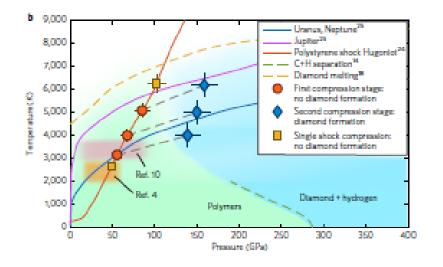
How can diamond be formed in polystyrene (CH), methane (CH₄), and other hydro-carbons under dynamic compression?

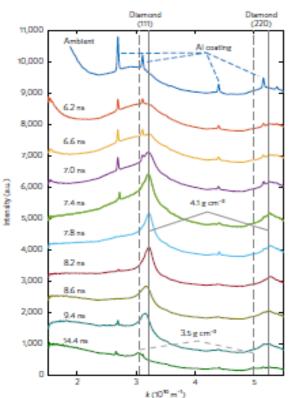
LETTERS DOI: 10.1038/s41550-017-0219-9

astronomy

Formation of diamonds in laser-compressed hydrocarbons at planetary interior conditions

D. Kraus^{1,2,3*}, J. Vorberger¹, A. Pak⁴, N. J. Hartley^{1,1}, L. B. Fletcher⁶, S. Frydrych^{4,7}, E. Galtier⁶, E. J. Gamboa⁶, D. O. Gericke⁸, S. H. Glenzer⁶, E. Granados⁶, M. J. MacDonald^{6,9}, A. J. MacKinnon⁶, E. E. McBride^{6,10}, I. Nam⁶, P. Neumayer¹¹, M. Roth⁷, A. M. Saunders², A. K. Schuster¹, P. Sun^{6,12}, T. van Driel⁶, T. Döppner⁴ and R. W. Falcone^{2,13}





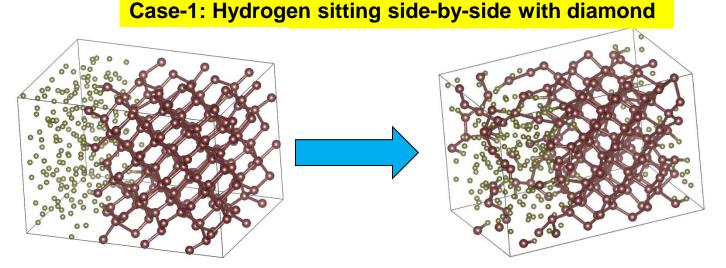


Maitrayee Ghosh

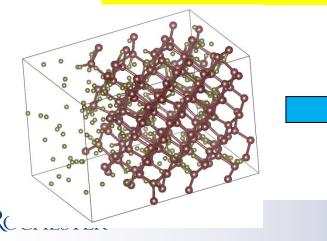
Questions remain: How did this happen? where are the hydrogen atoms? ...

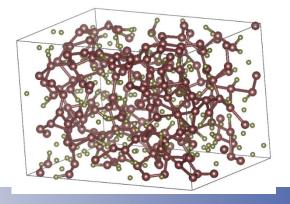


Where are the hydrogen atoms when diamond is formed? Diamond+H → CH-mixture @ ~150-Gpa?



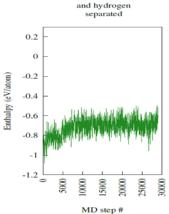
Case-2: Hydrogen randomly distributed in diamond



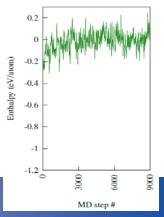




Maitrayee Ghosh



Randomly distributed hydrogen in diamond



Back to the simplest element --- Hydrogen: The understanding of its optical property is still not complete \rightarrow better xc-functional? quantum-p?

Conductivity and dissociation in liquid metallic hydrogen and implications for planetary interiors

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Edited by Vladimir E. Fortoy, Russian Academy of Sciences, Moscow, and approved September 7, 2017 (received for review May 12, 2017)

condensed matter in our solar planetary structure. The electronic the region 1.4-1.8 Mbar (6). It was argued that the transport properties of this metallic fluid are of

Liquid metallic hydrogen (LMH) is the most abundant form of plateauing of electrical conductivity at values around 2,0 conductivity was due to thermal smearing of the hand g

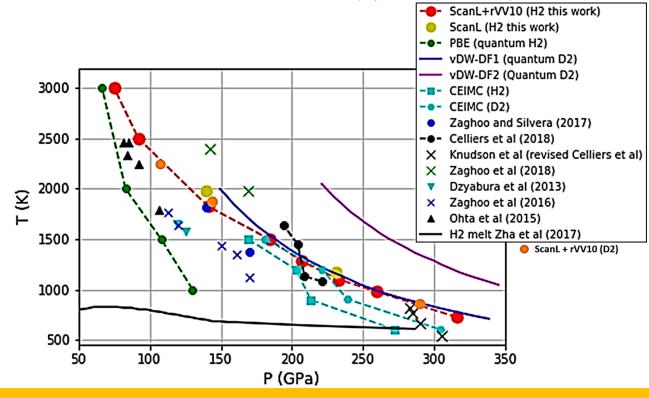
Celliers et al., Science 361, 677-682 (2018) 17 August 2018

Insulator-metal transition in dense fluid deuterium

Peter M. Celliers^{1*}, Marius Millot¹, Stephanie Brygoo², R. Stewart McWilliams³, Dayne E. Fratanduono¹, J. Ryan Rygg^{1,4}, Alexander F. Goncharov⁵, Paul Loubeyre², Jon H. Eggert¹, J. Luc Peterson¹, Nathan B. Meezan¹, Sebastien Le Pape¹, Gilbert W. Collins^{1,4}, Raymond Jeanloz⁶, Russell J. Hemley⁷



Josh Hinz



It looks like there is a winning xc-functional for hydrogen!

Conclusion & Outlook

✓



- First-principles methods developed for quantum many-body systems provide predictive capabilities for HED sciences (although limits exist);
- Significant improvements to current quantum many-body methods will be continuously made from our HEDS community;
- The HED-community efforts on seeking better understanding of the fundamental physics and chemistry at extreme conditions will make a difference to ICF, planetary science, astrophysics,...
- There are some urgent questions needed to be answered for communities of ICF and planetary science (*my personal list*):
 - ✓ What's the microphysics of non-uniform shock transition from ablator to DT? → "spall and ejecta" → mixing at the ablator/DT interface in ICF
 - What are the *true* α-particle stopping-power in ICF hot-spot and extremelydense DT-shell?
 - ✓ Are there any "excessive" thermal conduction in ICF hot-spot?
 - ✓ What drives phase separation in hydrogen-helium mixture and hydrocarbons under WDM conditions?

Y. H. Ding, V. V. Karasiev, R. Paul, M. Ghosh, J. Hinz, T. R. Boehly, P. B. Radha, V. N. Goncharov, S. Skupsky, J. R. Rygg, G. W. Collins, S. P. Regan, E. M. Campbell

> Laboratory for Laser Energetics University of Rochester

L. A. Collins, J. D. Kress, A. J. White, O. Certik

Theoretical Division, Los Alamos National Laboratory

B. Militzer

Department of Earth and Planetary Science and Astronomy University of California – Berkeley









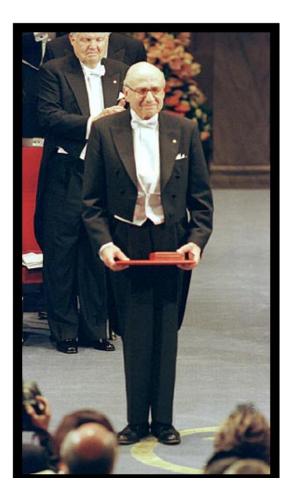
There is no free lunch! **DFT versus the Schrödinger Equation** LLE We have moved Properties of our problem the system from here ... Hard problem to solve "Easy" problem to solve Schrödinger view DFT view Formally equivalent Kohn-Sham particle electron \bigcirc interaction (non-interacting) effective potential external potential $\delta E_{xc}[n(\mathbf{r})]$ $\mathbf{v}_{eff}\left(\boldsymbol{r}\right) = \mathbf{v}\left(\boldsymbol{r}\right) + \int \frac{n\left(\boldsymbol{r}'\right)}{|\boldsymbol{r}-\boldsymbol{r}'|} d\boldsymbol{r}' +$... to here $\delta n(\mathbf{r})$

All many-body effects are included in the effective potential via the Exchange-Correlation functional, $E_{xc}[n(\mathbf{r})]$.



Walter Kohn awarded the Nobel Prize in Chemistry 1998 for Density Functional Theory

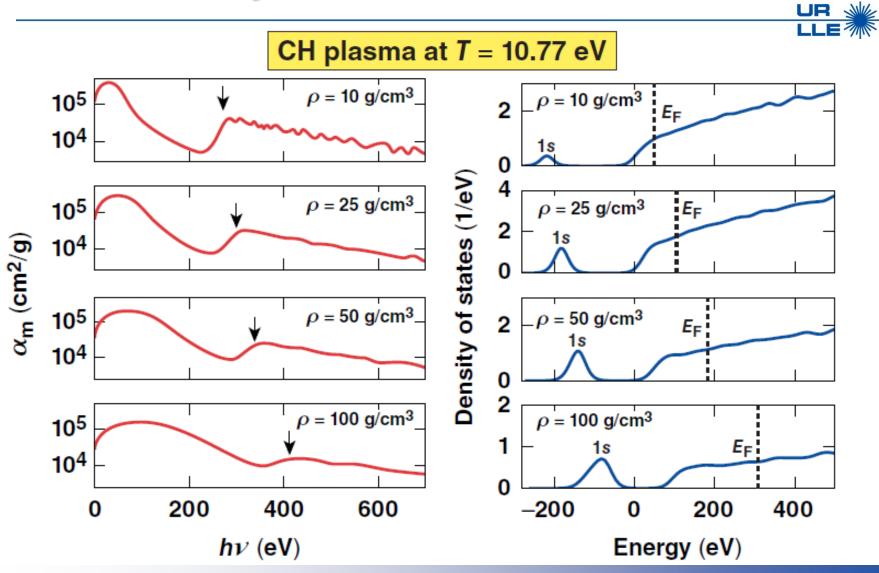




Hohenberg-Kohn theorem: Phys. Rev. 136, B864 (1964). The electron density contains all information needed to determine ground state properties of a system.

Kohn-Sham equations: Phys. Rev. 140, 1133 (1965). Practical scheme for solving the quantum mechanical problem based on the HK theorem.

The effect of *Fermi-surface-rising* on K-edge shifting can be naturally accounted in QMD simulations



ROCHESTER