

Coupling of Laser Angular Momentum to Plasma for the Generation of Kilo-Tesla Magnetic Fields

High Energy Density Science Centre Seminar 15th October 2020

Andrew Longman*

University of Alberta, Edmonton, Canada

PhD Supervisor – Robert Fedosejevs

*longman@ualberta.ca

Outline



• Motivation

- The need for strong magnetic fields
- Spin and Orbital Angular Momentum Beams
 - Brief review of Orbital Angular Momentum (OAM)
 - Diffraction of OAM beams and Laguerre-Gaussian (LG) modes
- The Inverse Faraday Effect
 - Analytic Models
 - Coupling of angular momentum to plasma and free electrons
- Numerical Modelling of the IFE
 - Modelling of Titan-like laser parameters
 - Asymmetric and realistic OAM beams
- Experimental Methods
 - Generating OAM beams at high intensity
 - Measuring magnetic fields



Laboratory Astrophysics

- Magnetic Reconnection
- Pulsars, Magnetars
- Cosmic Radiation and Particle Acceleration

B~100 - 10000T



- Laser Cyclotron Resonance
- Particle Guiding
- Enhancement of Laser Driven Light Sources

Fusion Plasmas

- Confinement of Plasmas
- Magnetically Assisted ICF
- Advanced Ignition Schemes Fast Ignition

How We Currently Generate Strong Longitudinal Magnetic Fields





Pulsed power driven coils

- Field strengths can typically range from 10 100 Tesla
- Spatial scale can be on the order of cm
- Peak field can last for μ s ms
- Sometimes destroyed in process



- Field strengths can typically range from 100 1000 Tesla
- Spatial Scale can be on the order of mm
- Peak field can last for ps ns
- Mostly destroyed in process



- Field strengths can typically range from 100 1000 Tesla
- Spatial Scale can be on the order of cm
- Peak field can last for $ns \mu s$
- Destroyed in process

Images: B. B. Pollock, et al, Rev. Sci. Inst. 77, 114703 (2006), O. V. Gotchev, et al, Phys. Rev. Lett. 103, 215004 (2009), V.T. Tikohonchuk, M. Bailly-Grandvaux, J. J. Santos, and A. Poye, Phys. Rev. E. 96, 023202 (2017)





Laser-Plasma Parameters For Above

- $0.03n_c$ He plasma
- $1 \times 10^{20} W cm^{-2}$, $\lambda = 1 \mu m$, $w_0 = 8 \mu m$, 100fs, 10J
- Linearly Polarized Laguerre-Gaussian l = 1 mode

Inverse Faraday Effect (IFE)

- Field strengths can typically range from 100 -10000 Tesla
- Spatial scale can be on the order of 100 μm+
- Peak field can last for ps's+
- Can be done at rep-rate of laser (no solid targets)
- Can be done with **linearly polarized** structured lasers

Outline



- Motivation
 - The need for strong magnetic fields
- Spin and Orbital Angular Momentum Beams
 - Brief review of Orbital Angular Momentum (OAM)
 - Diffraction of OAM beams and Laguerre-Gaussian (LG) modes
- The Inverse Faraday Effect
 - Analytic Models
 - Coupling of angular momentum to plasma and free electrons
- Numerical Modelling of the IFE
 - Modelling of Titan-like laser parameters
 - Asymmetric and realistic OAM beams
- Experimental Methods
 - Generating OAM beams at high intensity
 - Measuring magnetic fields





- Circular/elliptical polarization
- Radial/azimuthal polarization
- Carries spin angular momentum (SAM)

 ${m S}=\sigma_z\hbar$, $\sigma_z=\pm1,0$



- Usually a helical phase $e^{i\ell\phi}$
- Carries a well defined orbital angular momentum (OAM)

 $L = \ell \hbar$

$$\ell = 0, \pm 1, \pm 2, \dots, \pm \infty$$



- Interference of structured beams
- Leads to spatio-temporal intensity profiles (light springs)
- Carry orbital angular momentum spectrum (wavelength dependant)

Far-field Diffraction of OAM Beams Driven By Spiral Phase Plates







A. Longman, C. Salgado, G. Zeraouli, J. I. Apinaniz, J. A. Perez-Hernandez, M. Khairy Eltahlawy, L. Volpe, and R. Fedosejevs, "*Off-axis spiral phase mirrors for generating high-intensity optical vortices*", Opt. Lett. **45**(8) (2020)

ALBERTA

A. Longman, and R. Fedosejevs, "Optimal Laguerre-Gaussian Modes For High-Intensity Optical Vortices", J. Opt. Soc. Am. A, 37(4), 2020

Gaussian Near-Field Beam,

$$I_{nf}(r) \propto \exp\left(-2\frac{r^2}{R_0^2}\right)$$

Hankel transforms to the far-field,

$$I(\xi,\ell) = \frac{I_0\pi}{4}\xi^2 e^{-\xi^2} \left| I_{\frac{|\ell|-1}{2}} \left(\frac{\xi^2}{2}\right) - I_{\frac{|\ell|+1}{2}} \left(\frac{\xi^2}{2}\right) \right|^2$$

Where,

$$\xi = \frac{\rho}{w_0} , \qquad w_0 = \frac{\lambda f}{\pi R_0}$$

 R_0 is the near-field Gaussian beam radius, and $I_n(x)$ is the modified Bessel function of the 1st kind



OAM Beams From Flat Top Beams Previously Not Considered In Calculations and ALBERTA

A. Longman, and R. Fedosejevs, "Optimal Laguerre-Gaussian Modes For High-Intensity Optical Vortices", J. Opt. Soc. Am. A, 37(4), 2020

Flat-Top Near-Field Beam,

$$I_{nf}(r) \propto \left[circ\left(\frac{r}{R_F}\right) \right]^2$$

Hankel transforms to the far-field,

$$I(\xi,\ell) = \frac{I_0}{2} \left| \frac{\xi^{|\ell|}}{|\ell|! \left(\frac{|\ell|}{2} + 1\right)} \, _1F_2\left(\frac{|\ell|}{2} + 1; |\ell| + 1, \frac{|\ell|}{2} + 2, -\xi^2\right) \right|^2$$

Where,

$$\xi = \frac{
ho}{w_F}$$
, $w_F = \frac{\lambda f}{\pi R_F}$

 R_F is the near-field flat-top beam radius, and ${}_1F_2(a; b, c; d)$ is the generalized hyper-geometric function.





A. Longman, and R. Fedosejevs, "Optimal Laguerre-Gaussian Modes For High-Intensity Optical Vortices", J. Opt. Soc. Am. A, 37(4), 2020

The far-field diffraction equations are not ideal for • analytic or numerical modelling, so we instead use a modified Laguerre-Gaussian (LG) p = 0 basis set:

$$\psi_{\ell,p}(\xi,\phi)\Big|_{z=0} = \sqrt{\frac{p!\eta\gamma^2}{|\ell|!}} \left(\xi\gamma\sqrt{2}\right)^{|\ell|} e^{-(\xi\gamma)^2} e^{i\ell\phi} L_p^{|\ell|}(2\xi^2)$$

- The values of η and γ are optimally chosen such that • the LG mode is a good fit to the diffraction theory.
- Values of η and γ have been tabulated in the reference • above for Gaussian, Flat-top and super-Gaussian driver beams.



Gaussian Near-Field

Outline



- Motivation
 - The need for strong magnetic fields
- Spin and Orbital Angular Momentum Beams
 - Brief review of Orbital Angular Momentum (OAM)
 - Diffraction of OAM beams and Laguerre-Gaussian (LG) modes
- The Inverse Faraday Effect
 - Analytic Models
 - Coupling of angular momentum to plasma and free electrons
- Numerical Modelling of the IFE
 - Modelling of Titan-like laser parameters
 - Asymmetric and realistic OAM beams
- Experimental Methods
 - Generating OAM beams at high intensity
 - Measuring magnetic fields



• Average rate of change of electron angular momentum in the presence of a beam carrying angular momentum [1,2]:

$$m_e n_e r \left(\frac{d}{dt} + v_{ei}\right) u_{e\theta} = -e n_e r (E_\theta + u_{ez} B_r - u_{er} B_z) - \frac{dM_z}{dt}$$

• Allen (92) [3]:

$$M_z = \frac{\ell}{\omega c}I + \frac{\sigma_z r}{2\omega c} \left(\frac{\partial I}{\partial r}\right)$$

• Assuming
$$v_{ei} \sim 0$$
, $du_{e\theta}/dt = 0$, $u_{ez,r} \ll c$:

$$en_e rE_{\theta} \sim -\frac{dM_z}{dt}$$

• Using Faraday's law:

$$B_{z} = -\frac{f_{abs}}{ren_{e}\omega c} \left[\ell \frac{\partial I}{\partial r} + \frac{\sigma_{z}}{2} \frac{\partial}{\partial r} \left(r \frac{\partial I}{\partial r} \right) \right]$$

- f_{abs} is fraction of laser energy absorbed by plasma.
- Note dependence on σ_z linearly polarized lasers can drive axial magnetic fields!



$$B_{z} = -\frac{2f_{abs}}{en_{e}\omega cw_{0}^{2}}I(r,\ell)\left[\ell\left(\frac{w_{0}^{2}|\ell|}{r^{2}} - 2\right) + \sigma_{z}\left(\frac{|\ell|^{2}w_{0}^{2}}{r^{2}} - 2 - 4|\ell| + \frac{4r^{2}}{w_{0}^{2}}\right)\right]$$







$$B_{z} = -\frac{2f_{abs}}{en_{e}\omega cw_{0}^{2}}I(r,\ell)\left[\ell\left(\frac{w_{0}^{2}|\ell|}{r^{2}} - 2\right) + \sigma_{z}\left(\frac{|\ell|^{2}w_{0}^{2}}{r^{2}} - 2 - 4|\ell| + \frac{4r^{2}}{w_{0}^{2}}\right)\right]$$



Model ParametersNear-field : Flat-top $\ell = -1, \sigma_z = 0$ (LP)Peak Intensity: 2.5E19Wcm-2
(Energy is the same as previous) $w_0 = 6\mu m, n_e = 3 \times 10^{19} cm^{-3}$

Peak axial B-field: \approx **10000T**

 $f_{abs} = 1$



Model Parameters	5
Near-field : Flat-t	op
$\ell = var, \sigma_z = 0$	
Peak Intensity: 1E20Wcm-2 ($\ell = 0$) (Energy is the same for all)	
$w_0 = 6\mu m$	
$f_{abs} = 1$	
0	D

l	B _{max}
0	0
1	-9548
2	-2628
3	-1512
4	-1007







• Shown by Allen et al (1992):

$$\boldsymbol{J} = (\sigma_z + \ell) N \hbar$$

- Where, $\sigma_z = \pm 1,0$, $\ell = 0, \pm 1, \pm 2, \dots, \pm \infty$
- Spin and orbital angular momentum can constructively or destructively interfere
- This is clear as the magnetic field generated can either be enhanced or dampened



- A fundamental question concerning OAM and SAM beams is how they couple to the plasma, and if OAM/SAM can be transferred and by which mechanisms
- We started to look at this question from the fundamental point of view using single electrons in ultra-intense beams
- This however requires an accurate model of the E and B fields at focus in an LG mode



$$\boldsymbol{E} = E_0 \left[\hat{x} + \frac{\hat{y}}{2k^2} \frac{\partial^2}{\partial x \partial y} + \frac{i\hat{z}}{k} \frac{\partial}{\partial x} \right] \psi(x, y, z) e^{i(kz - \omega t)}$$
$$\boldsymbol{B} = \frac{E_0}{c} \left[\frac{\hat{x}}{2k^2} \frac{\partial^2}{\partial x \partial y} + \hat{y} + \frac{i\hat{z}}{k} \frac{\partial}{\partial y} \right] \psi(x, y, z) e^{i(kz - \omega t)}$$

• We can utilize the elegant form of the LG modes given by,

$$\psi_{\ell,p}(r,\phi) = \sqrt{\frac{\eta p! \gamma^2}{(p+|l|)!}} e^{il\phi} \left(\frac{rkw_0}{\gamma\sqrt{2}Z}\right)^{|l|} \frac{z_0}{Z} \exp\left(-\frac{kr^2}{2Z}\right) L_p^{|\ell|} \left(\frac{kr^2}{Z}\right), \qquad Z = z_0 + iz$$

[1]. W. L. Erikson, and S. Singh, Phys. Rev. E. 49, 5778-5786 (1994)
[2]. J. Peatross et al. Opt. Express 25(13), 13990-14007, (2017)

UNIVERSITY OF

OAM beams to high accuracy

٠

Deriving the Laguerre-Gaussian modes to second order paraxial has allowed the study of single electron dynamics in

Laguerre-Gaussian Modes – Analytic Forms Can Be Used For Calculations

To be published – upcoming paper on nonlinear Thomson scattering in Laguerre-Gaussian beams

UNIVERSITY OF

ТΑ

ALBER



For a beam linearly polarized in the x-direction @ z = 0:





- Modified ponderomotive force due to donut mode
- Particle trapping/guiding due to ponderomotive well and wakefield focussing forces

$$F_{p}(r,\ell) = -\frac{e^{2}}{4m_{e}\omega^{2}}|E(r)|^{2}\left(\frac{2|\ell|}{r} - \frac{4r}{w_{LG}^{2}}\right)$$

• Particles caught within the ponderomotive potential can be accelerated forward with a peak velocity as high as

$$\beta_z = \frac{a_0^2}{\sqrt{a_0^4 + 16}}$$

• No apparent AM transfer from ponderomotive force $- \operatorname{no} \boldsymbol{F}_{\theta}$ component!



2000 electrons scattering from LP Gaussian beam



Parameter	Value
Intensity	$5 \times 10^{21} W cm^{-2}$
Beam waist	10µm
Pulse duration	100fs



2000 electrons scattering from LP Laguerre-Gaussian beam





Beams have been normalized to contain same energy and focussed from same f/#





- Average number of photons absorbed per electron is ~7000 according to scattered energy
- Scattered electrons absorb ~7000ħ angular momentum from the photons
- Simple to understand using conservation of energy and angular momentum
- Direction of angular momentum absorbed changes with handedness of LG beam

OAM Coupling to single electrons scales with ponderomotive coupling:

$$L_z \propto \frac{a_0^2}{4}$$

Ponderomotive Scattering of Free Electrons can Transfer OAM

8000

6000

Average number of photons absorbed per electron is ~7000 according to scattered energy



LG10 Beam

UNIVERSITY OF

ALBERTA

Outline



- Motivation
 - The need for strong magnetic fields
- Spin and Orbital Angular Momentum Beams
 - Brief review of Orbital Angular Momentum (OAM)
 - Diffraction of OAM beams and Laguerre-Gaussian (LG) modes
- The Inverse Faraday Effect
 - Analytic Models
 - Coupling of angular momentum to plasma and free electrons
- Numerical Modelling of the IFE
 - Modelling of Titan-like laser parameters
 - Asymmetric and realistic OAM beams
- Experimental Methods
 - Generating OAM beams at high intensity
 - Measuring magnetic fields

28



$$\eta(r) \approx 1 - \frac{\omega_p^2}{\omega^2} \frac{n_e(r)}{n_0 \gamma(r)}$$

• Critical power for self focussing is modified for LG (p=0) beams to:

$$P_{c\ell}[GW] = 17.4 \frac{n_c}{n_e} 4^{|\ell|} \frac{|\ell|! (|\ell|+1)!}{(2|\ell|)!}$$



Red: LG10 Beam







UNIVERSITY OF WARWICK



Laser Electric Field Ey

29

OAM Ring Initially Pinches





OAM Ring Then Collapses







• Axial Magnetic Field is averaged over 33fs output steps



- About $100\mu m$ long from a 100fs laser pulse magnetic field length may scale with pulse duration
- 10x **longer** than shown in previous publications
- B Field direction can be flipped by changing OAM mode: $\ell = 1 \rightarrow \ell = -1$

PIC Verifies Inverse Faraday Model For Linearly Polarized LG10 mode





- From the simulation we find the model parameters:
 - $f_{abs} \sim 4\%$ @ 1ps
 - Peak intensity after ring pinch self focussing: $\sim 1.2 \times 10^{20} W cm^{-2}$
 - Electron density decreases by ~ 20%

Linearly Polarized LG₂₀ Mode Agrees With Inverse Faraday Model





- B-field is weaker as expected
- The tube of magnetic field eventually collapses to a single solid rod of field.

Plotting of Magnetic Field Energy in Simulation Finds Decay Time

- Increasing the laser OAM from $\ell = 1$ to $\ell = 2$ appears to double the decay time, at a cost of B field strength
- Decay time is much shorter than that assumed through magnetic diffusion in the plasma ~10ns assuming Spitzer resistivity

The B field Decay Time Seems To Be A Function of OAM Number

• Comparing the laser modes, we find an interesting result that increasing the OAM number in the beam looks to increase the B-field persistence

$\tau \propto |\ell|$

• Could be a result of radial electron energy and electrons leaving the grid

UNIVERSITY OF

BER

B Field Persists For ~1ps After Genesis

B Field Persists For ~1ps After Genesis

B Field Persists For ~1ps After Genesis

-100T Magnetic Field Isosurface

LG10 Simulation time $\approx 1ps$

LG10 Simulation time $\approx 2.34 ps$

• Through previous theta pinch instability work, it has been shown that the wobble instability can be suppressed by increasing azimuthal mode number [1].

Using a Perturbative Approach – We Can Model Asymmetric Beams

• Perturbing the LG (*L*) mode with the function allows us to model the beams more realistically

 $\lambda = 1 + \delta \cos(m\theta)$

• Decomposing the perturbed wavefunction into 3 orthogonal LG (ℓ) modes:

$$\eta_{L-\ell=0} = \left(1 + \frac{\delta^2}{2}\right)^{-1}$$
$$\eta_{|L-\ell|=|m|} = \frac{\Gamma^2 \left(\frac{|\ell|}{2} + \frac{|L|}{2} + 1\right)}{2|L|! |\ell|!} \left(1 + \frac{2}{\delta^2}\right)^{-1}$$

41

- Considering a 10% perturbation on the beam
- We can decompose the perturbed beam into 3 modes:

 $L = 1, m = 1, \delta = 0.1$

Decomposes to:

99.5%
$$\ell = 1$$
, 0.2% $\ell = 0$, 0.2% $\ell = 2$

Outline

- Motivation
 - The need for strong magnetic fields
- Spin and Orbital Angular Momentum Beams
 - Brief review of Orbital Angular Momentum (OAM)
 - Diffraction of OAM beams and Laguerre-Gaussian (LG) modes
- The Inverse Faraday Effect
 - Analytic Models
 - Coupling of angular momentum to plasma and free electrons
- Numerical Modelling of the IFE
 - Modelling of Titan-like laser parameters
 - Asymmetric and realistic OAM beams
- Experimental Methods
 - Generating OAM beams at high intensity
 - Measuring magnetic fields

- Currently it is difficult to generate optical vortices at ultra high intensities:
 - Issues with nonlinear effects on beam temporal and spatial profiles if transmitted through glass
 - Issues with retro-reflections and mode separation with spiral phase mirrors
 - Expensive to etch a spiral into a large diameter (>100mm) glass substrate
 - Damage threshold of optics is typically too low for high-power laser facilities

Design Parameters

- Needed to be scalable to any size (diameter)
- Needed to be compatible with ultra-short pulses
- Cost effective manufactured on campus
- Flexibility for use in any laser system (after amplifier)
- High damage threshold

Off-Axis Spiral Phase Mirror (**OASPM**)

A. Longman, and R. Fedosejevs, "Off Axis Spiral Phase Mirror," U.S. Provisional Patent #62/508,222 (2017-2019)

A. Longman, C. Salgado, G. Zeraouli, J. I. Apinaniz, J. A. Perez-Hernandez, M. Khairy Eltahlawy, L. Volpe, and R. Fedosejevs, "*Off-axis spiral phase mirrors for generating high-intensity optical vortices*", Opt. Lett. **45**(8) (2020)

Performance Was Tested With A 2 inch Prototype

- Initial tests with a lab HeNe laser beam
- OASPM was used at a 45deg incidence angle and was manufactured to a 2inch diameter.
- High symmetry focal spots, almost perfect agreement with diffraction theory using an f/30 lens

Tested At High Power Using CLPU 200TW VEGA Laser

• Testing with the Centros Laseres Pulsados Ultraintenses (CLPU) in Salamanca, Spain

CLPU VEGA 2 Beam Characteristics

- 3J, 30fs at focus using an f/4 or f/13 OAP
- 10Hz
- $\lambda = 800nm$, $\Delta \lambda = 80nm$
- 5" OASPM inserted at 17.8deg AOI

Our Experiments Yielded Highest OAM Intensity To Date

- Spatial inhomogeneities in the laser near-field seem to be the main limiting factor in the focal spot symmetry.
- Aberrations in the focus such as trefoil, astigmatism, and coma also reduced spot symmetry.

OAM Beam Characteristics

- $\ell = 0,7 \times 10^{19} W cm^{-2}$
- $\ell = 1$, $3.2 \times 10^{19} W cm^{-2}$
- $\ell = 2$, $2.4 \times 10^{19} W cm^{-2}$

A. Longman, C. Salgado, G. Zeraouli, J. I. Apinaniz, J. A. Perez-Hernandez, M. Khairy Eltahlawy, L. Volpe, and R. Fedosejevs, Opt. Lett. **45**(8) (2020)

Two Suitable Methods To Diagnose Strong Axial Magnetic Fields

-20

1000

[Tesla]

ъ×в

Faraday Rotation – Probe • pulse is polarization rotated

٠

Time = 0.967ps

- While the two previous methods of B-field measurement are being suitable for the fields we intend to measure, we are also exploring alternatives:
 - Proton radiography
 - Cyclotron emission ($\approx 10 \mu m$)
 - SRS backscatter
 - Thomson scattering

- Diffraction models of high-power OAM beams were developed allowing for the first time accurate modelling of high intensity OAM beams
 - An additional perturbation model has been developed for modelling of asymmetric OAM beams
- Determined that OAM can be transferred to free electrons through ponderomotive-like forces OAM coupling scales as a_0^2
 - Derived symmetric paraxial E and B fields of generalized Laguerre Gaussian modes
- Using EPOCH PIC code we were able to identify two new self focussing modes ring pinch and ring collapse
- Modelling of inverse Faraday effect using EPOCH confirms previous analytic models
 - In addition, we showed the magnetic field persistence (~1ps) decay time, and also typical length scales of $100\mu m$
 - Magnetic field persistence may be inhibited by wobble instabilities, can increase time by increasing OAM mode
- The off-axis spiral phase mirror has been introduced and now allows for the generation of ultra-high intensity OAM beams in almost any laser system already collaborating with two groups on implementation on other lasers
 - The highest intensity OAM beams to date were generated

I would like to thank and acknowledge the following people;

Robert Fedosejevs

CLPU Scientific, Technical, and Laser Teams

University of Alberta machine shop and nanoFAB centre – OASPM and diagnostic fabrication

Jason Myatt

EPOCH development team

And funding from;

canada

compute | calcul

canada

- 4000 x 500 x 500 cells
- 150μm x 40μm x 40μm
- 2 billion particles
- He + Ionizable Nitrogen Plasma (2.7keV)
- $3 \times 10^{19} cm^{-3} = 0.03 n_c$
- $2.5 \times 10^{19} W cm^{-2}$, 100 fs
- Linearly Polarized *LG*₁₀
- ~15CPU years / run