

# How the concepts of coast time and radius of peak velocity were a key part to achieving capsule gain $> 5$ in ICF

APS DPP

Talk BI01

November 8, 2021

O. A. Hurricane



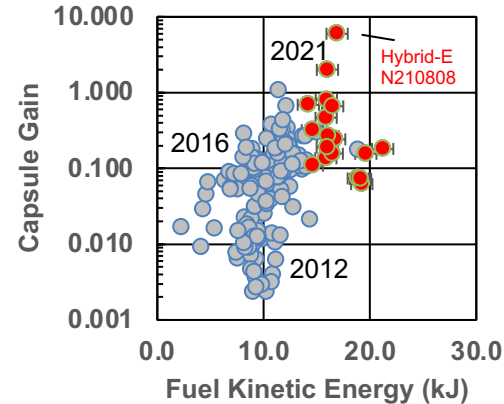
# Thanks to my collaborators and colleagues

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D. Callahan, D.T. Casey, S. Haan, A. Kritcher, O. Landen, R. Nora,  
P.K. Patel, J. Ralph, P.T. Springer, and A. Zylstra

# We will focus upon the subtle concept of coast time, how our understanding of it changed over time, and how we've leveraged it for recent advances

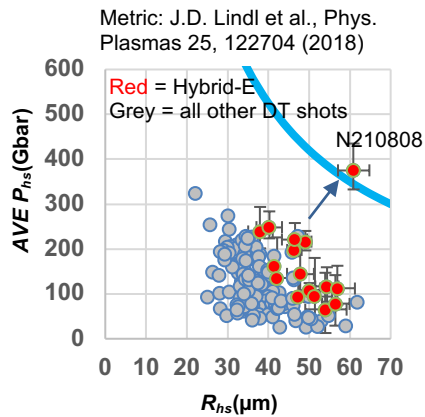
- Record fusion gain levels have been achieved
- We presently believe that reduced coast time was a key contributor to the recent performance advance
- Coast time is an important duration of time between the end of the drive on the capsule and the time of peak neutron production (“bang time” aka “BT”)
- The effectiveness of reducing coast time has been demonstrated several times over the past 8 years of work on the NIF
- Our present understanding is that reducing coast time reduces the radius at which peak implosion velocity is achieved
- Reducing the radius of peak velocity increases the rate of mechanical energy transfer from implosion kinetic energy into hot-spot internal energy



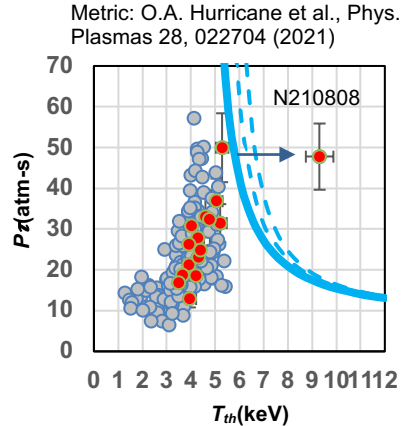
Gain	N210207	N210307	N210808
$G_{fuel}$	$7.8 \pm 1.0$	$6.2 \pm 0.9$	$70 \pm 7$
$G_{capsule}$	$0.75 \pm 0.05$	$0.57 \pm 0.04$	$6.0 \pm 0.2$
$G_{target}$	0.09	0.07	0.7

(NAS 1997 report definition of ignition is  $G_{target} = 1$ )

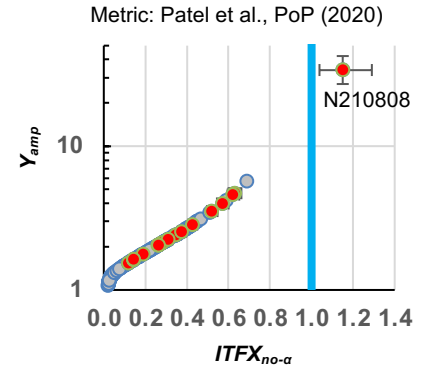
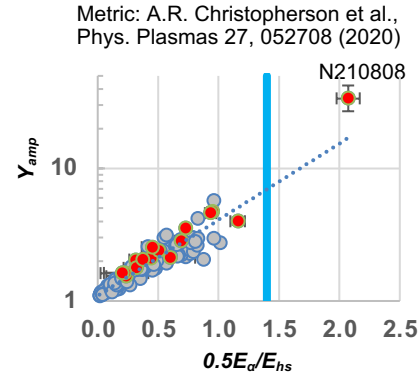
# N210808 ignited (i.e. passed the tipping-point of thermodynamic instability) by many published metrics as the hot spot pressure and temperature increased



Pressure doubled

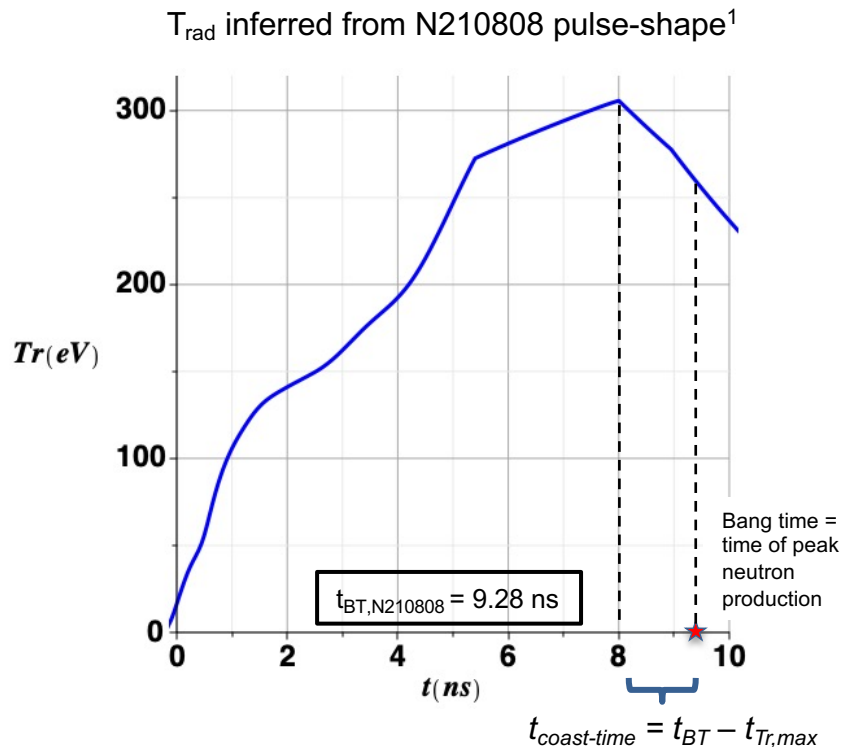


Temperature doubled



How did reducing coast time contribute?

# There have been many definitions of coast time, in this talk we will focus upon the definition linked to peak hohlraum $T_{rad}$

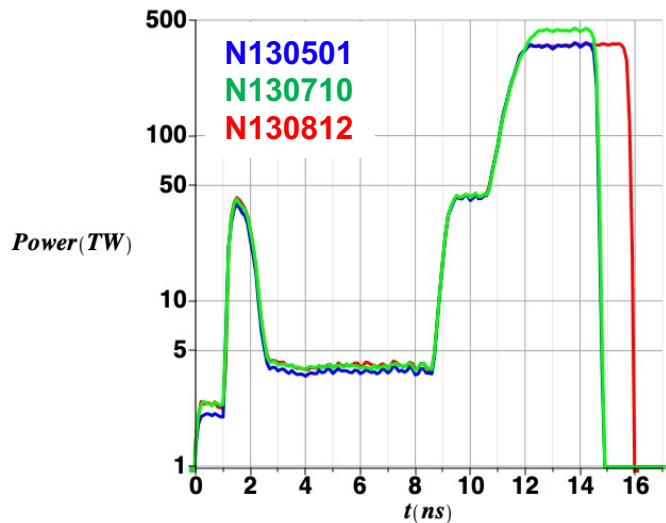


- Historically, coast time was defined using the **laser off** time, but this made less sense as the physics was better understood
- Time of maximum radiation temperature ( $T_{rad,max}$ ) is the time of maximum ablation pressure ( $p_{abl}$ )
- The theory of this talk will define the coast time ( $t_{coast}$ ) as

$$t_{coast} = t_{bang-time} - t_{Tr,max}$$

Data plots use the **50% max laser power falling edge** definition (time differences can be 0 – 0.36 ns)

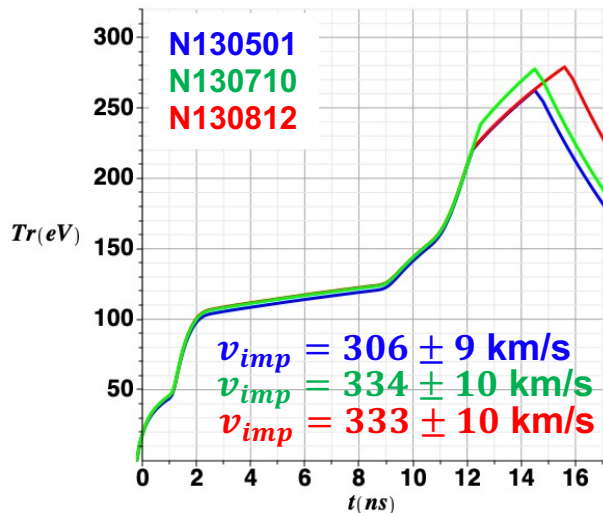
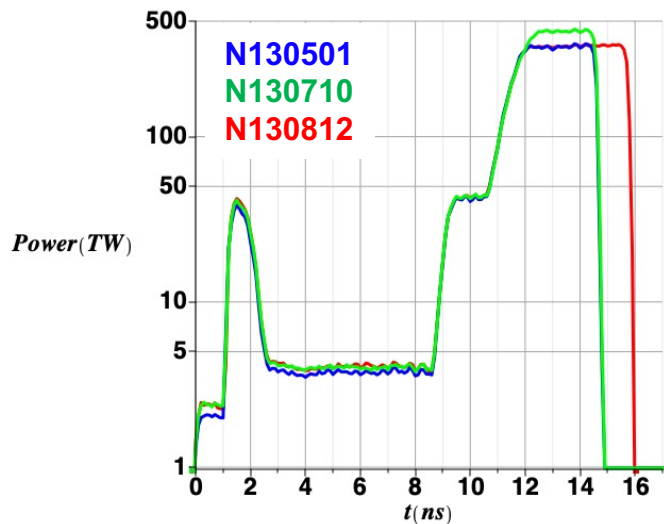
# The first systematic study of coast time started with the high-foot\* and tests that intercompare high power with high energy



Note: D.Hinkel – lead hohlraum designer

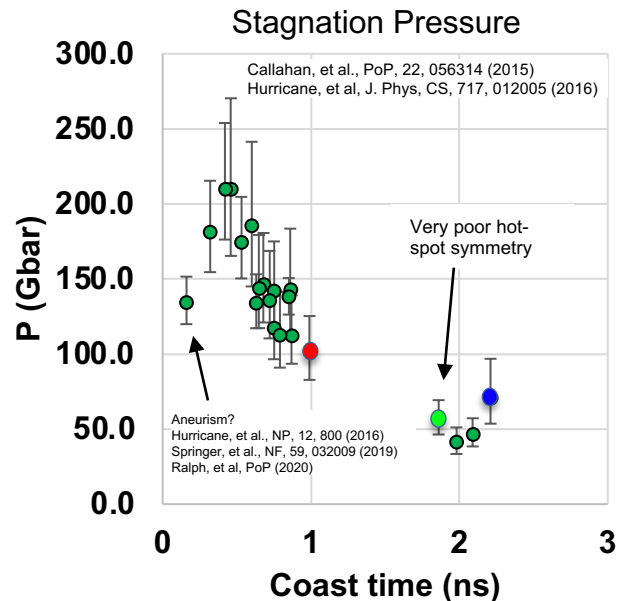
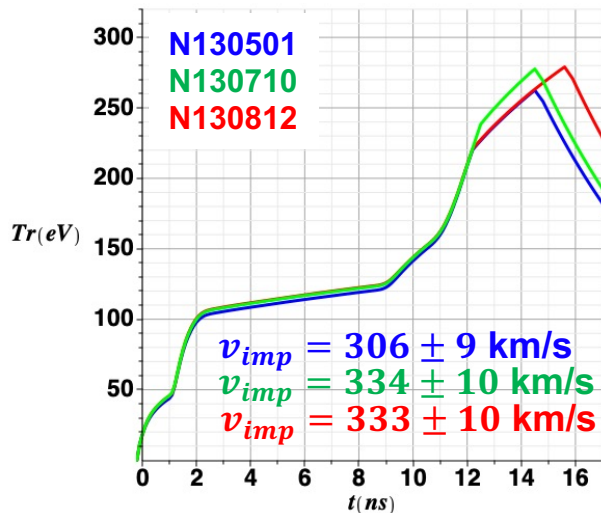
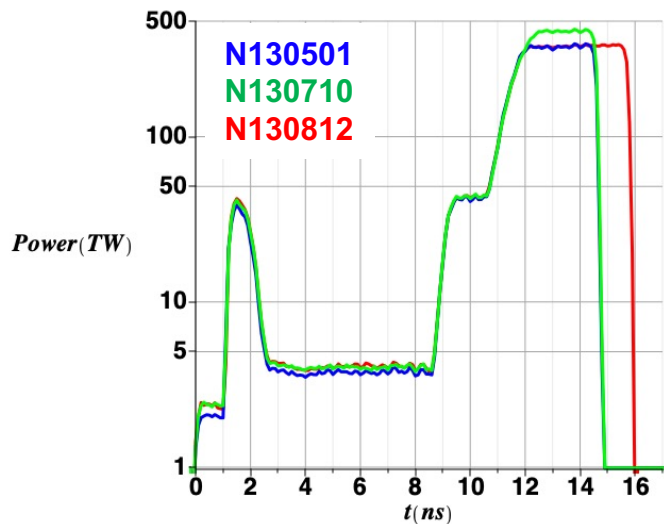
# With fixed target geometry, these three pulse shapes resulted in three different x-ray drives on the implosion

Same target geometry





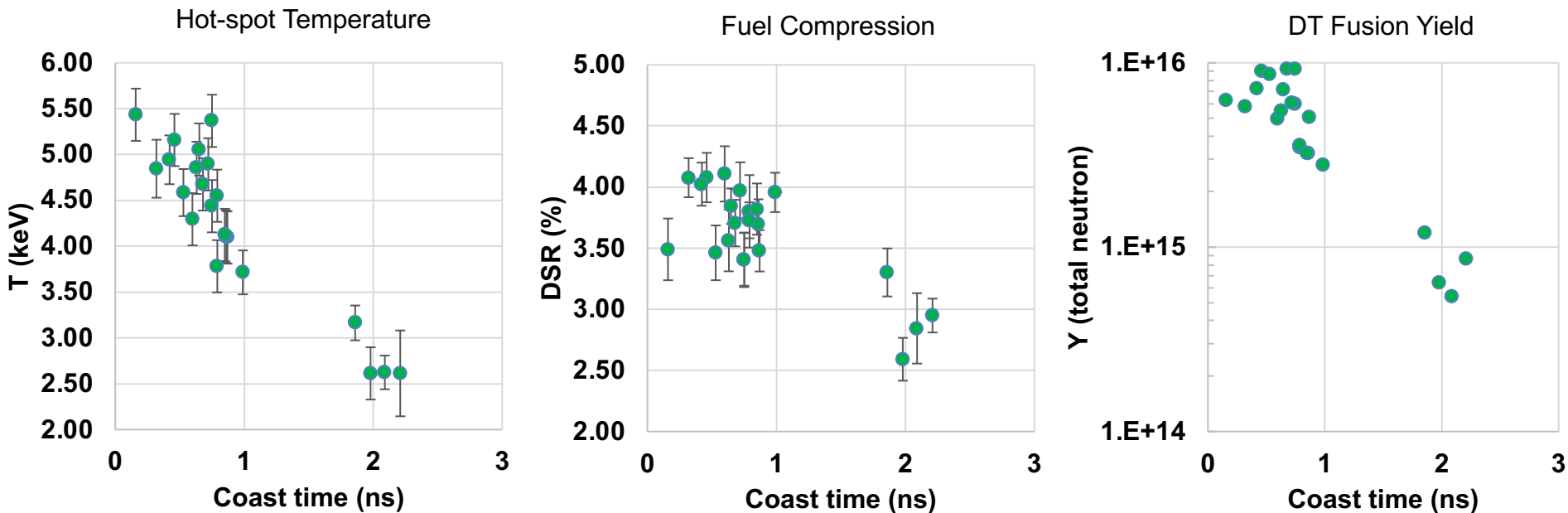
# This exploration of higher power vs. lower coast time pointed us towards lower coast, which we scanned to obtain 200+ Gbar



After this initial 3-shot study, systematically reducing coast-time at relatively low laser power became a cornerstone of the high-foot shot plan



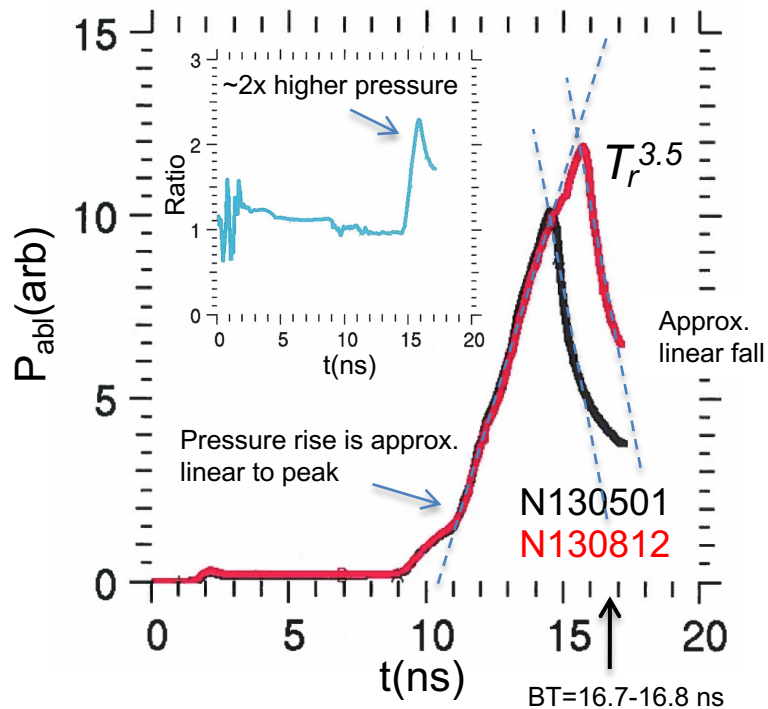
# In addition to stagnation pressure, other hot-spot properties were seen to increase with reduced coast time



At the time, we didn't fully understand why coast time reduction was such a strong lever on performance, but we treated it as an observational fact and used it

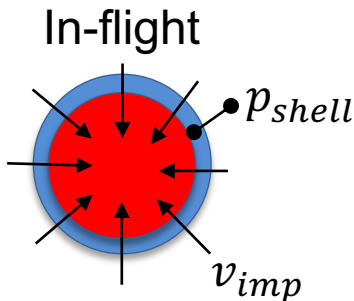
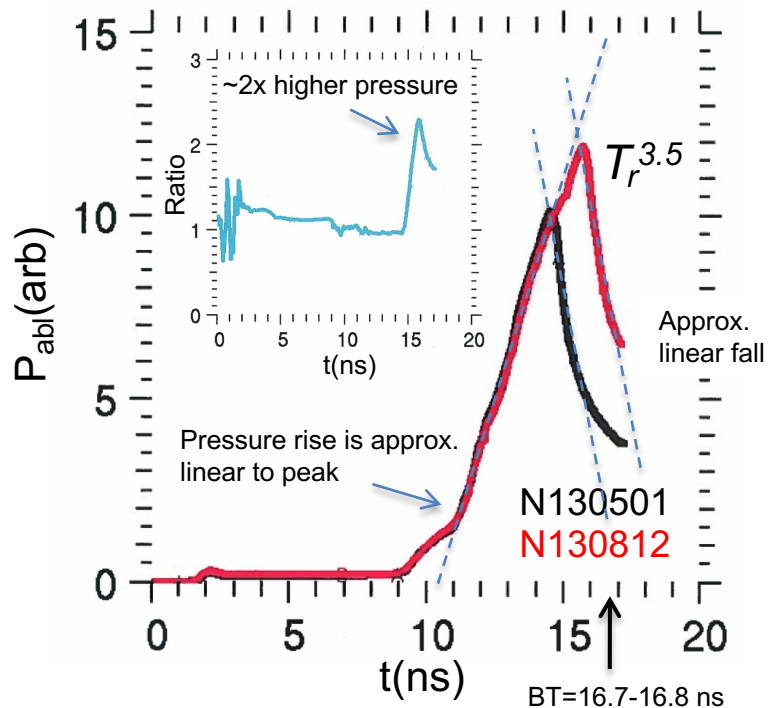
# Reducing coast time results in a larger late time ablation pressure increasing implosion velocity and increasing shell compression

## Ablation Pressure



# The stagnation pressure should be related to the DT shell pressure at peak velocity and the Mach number of the DT shell

## Ablation Pressure



$$p_{stag} = p_{shell} M^3$$

Kemp, Atzeni, Meyer-ter-Vehn, PRL (2001):

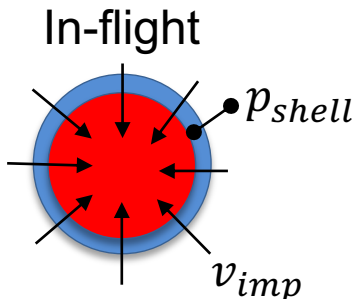
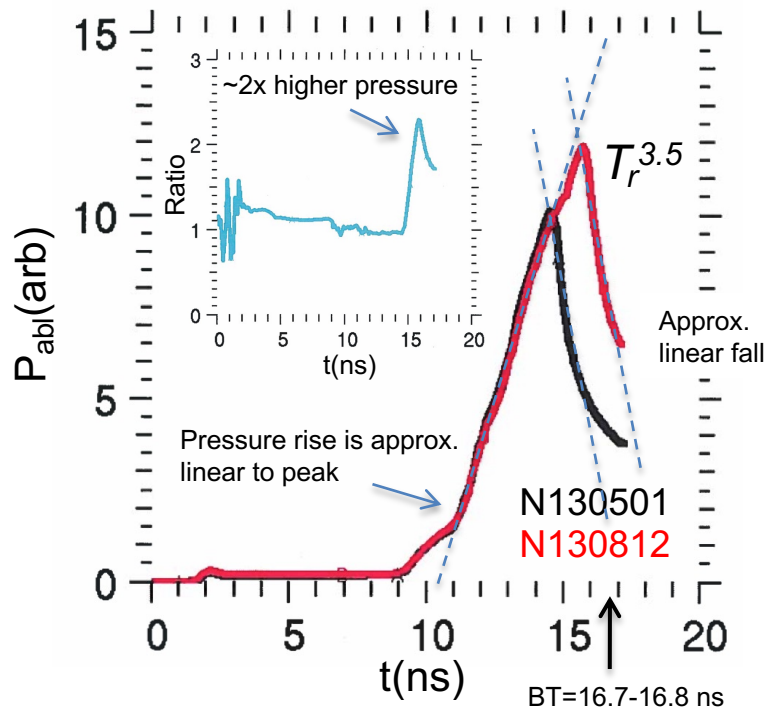
Rocket model +

$$p_{shell} \approx p_{abl,max}$$

$$\rightarrow p_{stag} \sim T_r^{7/5} v_{imp}^3$$

# One finds that the stagnation pressure of the implosion is linked to both the implosion velocity and the late time hohlraum $T_{rad}$

## Ablation Pressure



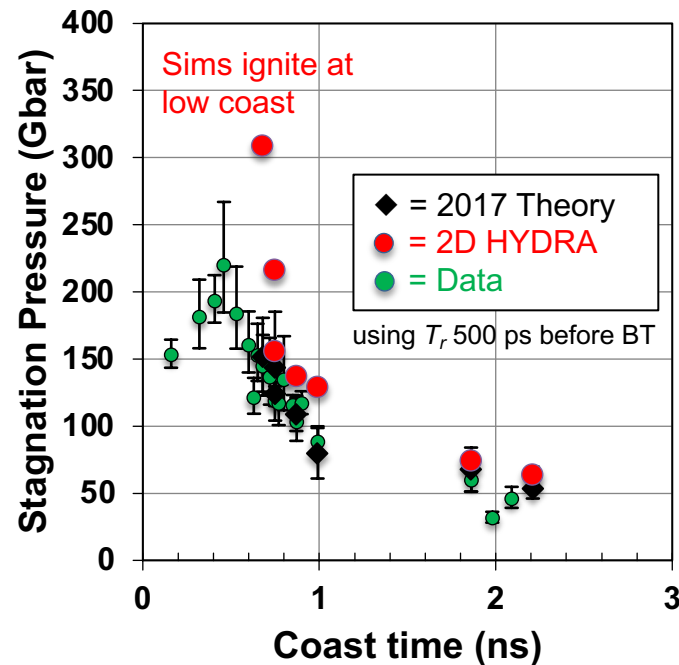
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Kemp, Atzeni, Meyer-ter-Vehn, PRL (2001):

Rocket model +

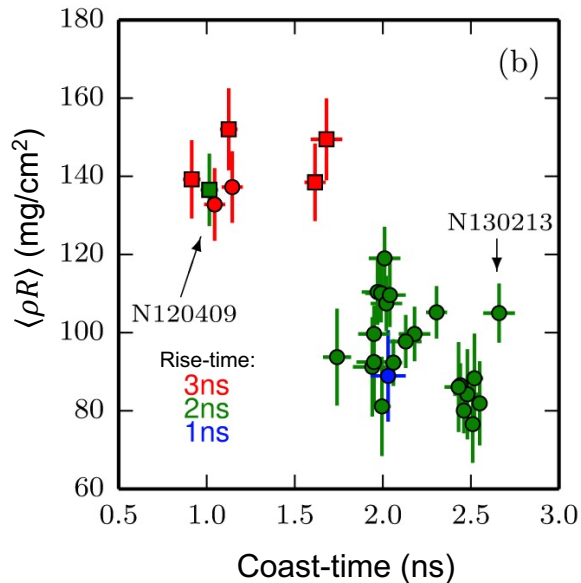
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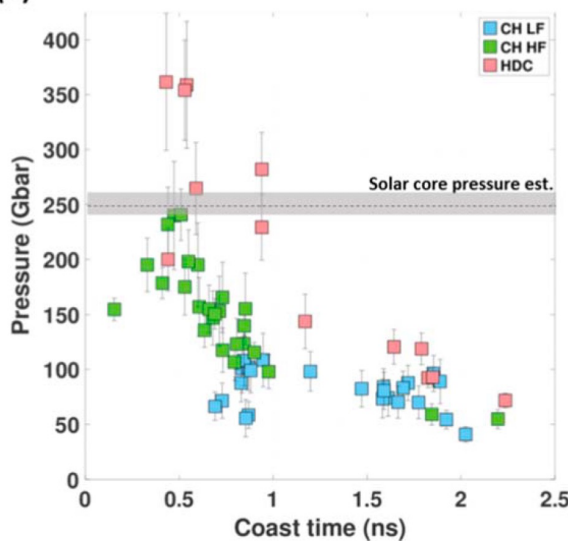


# A variety of different indirect-drive implosions have responded favorably to reduced coast time

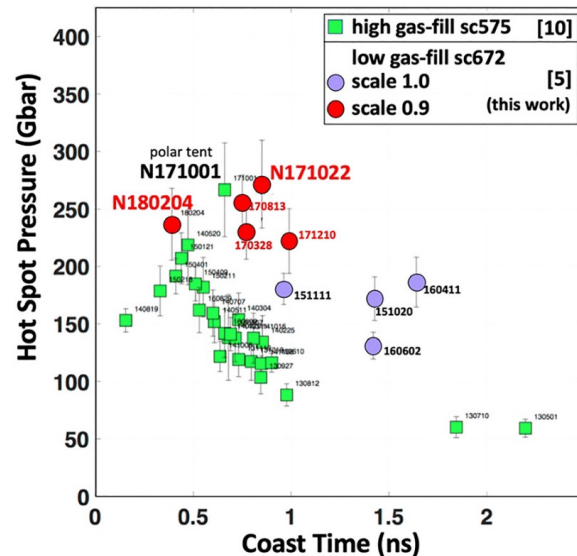
**High gas-fill hohlraum D<sup>3</sup>He gas capsules**  
Zylstra, et al., PoP, 21, 112701 (2014)



**Low gas-fill hohlraum HDC DT implosions**  
L. Berzak Hopkins, et al., PPCF, 61, 014023 (2019)

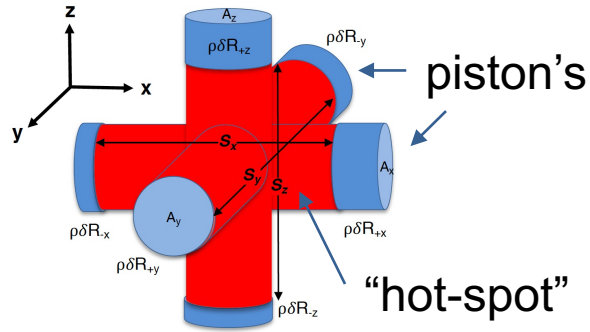


**Low gas-fill hohlraum CH DT implosions**  
T. Döppner, et al., PoP, 27, 4 (2020)



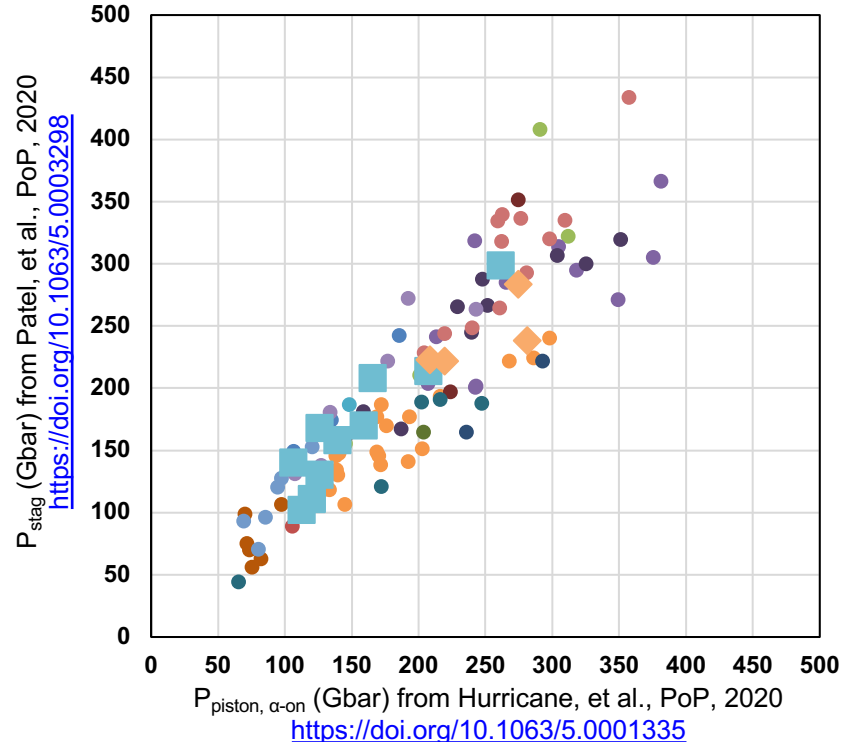
Coast time reduction is only effective if implosion degradations (e.g. mix, asymmetry, etc.) are controlled

# Piston models, developed for studying implosion asymmetry, also appeared to match data well, but how related to our 2017 picture?



One of the many formulas:

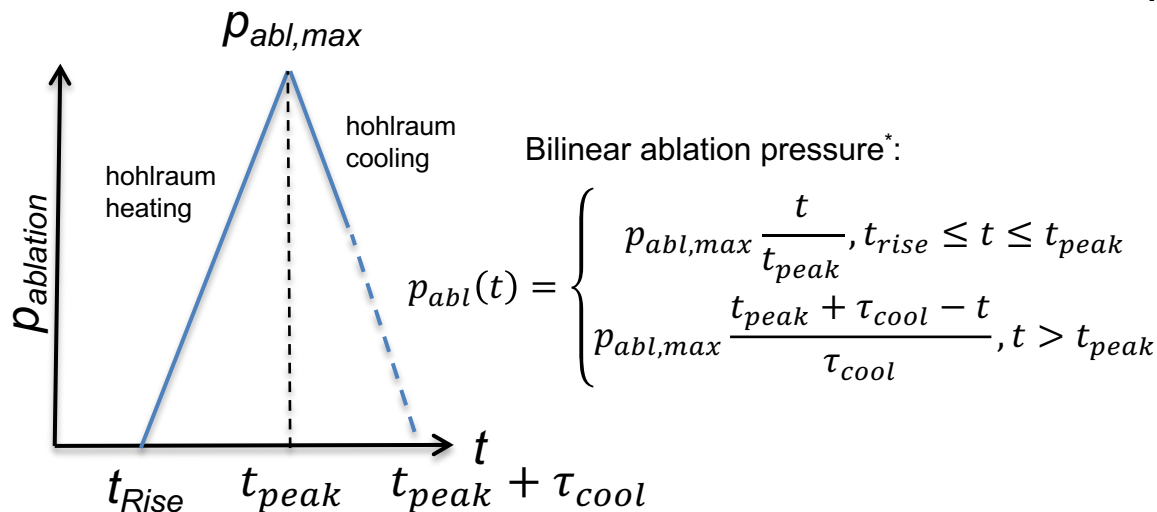
$$P_{piston, no-\alpha} = \frac{v_{imp}^5}{P_{pv}^{3/2}} \left[ \frac{\rho\delta R_{WHM}}{R_{pv}} \right]^{5/2}$$



Also see D. Casey, et al., PRL, 126, 025002 (2021) and 2<sup>nd</sup> PoP paper in preparation;

The radius of peak velocity,  $R_{pv}$ , must be related to the coast-time

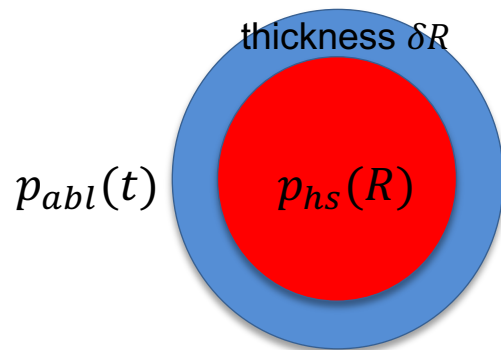
# As the hohlraum is cooling, the ablation pressure outside of the implosion is dropping, while the hot-spot pressure is increasing



beginning of  
rise to peak  
laser power

Newton's Law for shell motion:

$$\frac{d\dot{R}}{dt} \approx \frac{p_{hs}(R) - p_{abl}(t)}{\rho \delta R(R)}$$



we will assume shell mass conserved after peak velocity



# We don't need the full Newton's law solution to make the connection between the radius of peak velocity and coast-time

The shell acceleration is zero at peak velocity -- *the moment of free-fall*

So, we get a relation connecting the pressure at peak velocity to the time of peak velocity,

$$p_{pv} = p_{abl}(t_{pv}) \approx p_{abl,max} \frac{t_{peak} + \tau_{cool} - t_{pv}}{\tau_{cool}}$$

Deceleration time from piston model differential equation solution:

$$t_{decel} = \frac{R_{pv}}{v_{imp}} = t_{BT} - t_{pv} \rightarrow t_{pv} = -\frac{R_{pv}}{v_{imp}} + t_{BT}$$

## We find that the coast-time, hohlraum cooling time, and radius of implosion peak velocity are all related

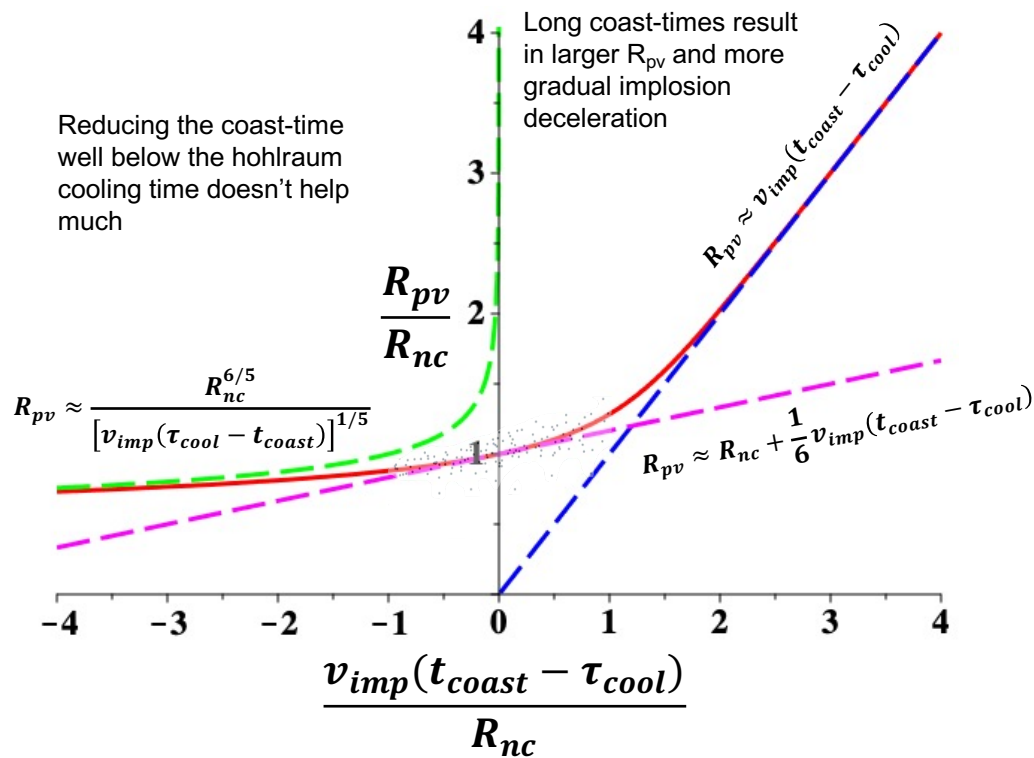
Stagnation pressure from piston model (one of a couple forms in  $Y_{amp} < 2$  limit):

$$p_{piston} = \frac{\rho \delta R_{WHM} v_{imp}^2}{R_{hs}} = p_{pv} \left( \frac{R_{pv}}{R_{hs}} \right)^5$$

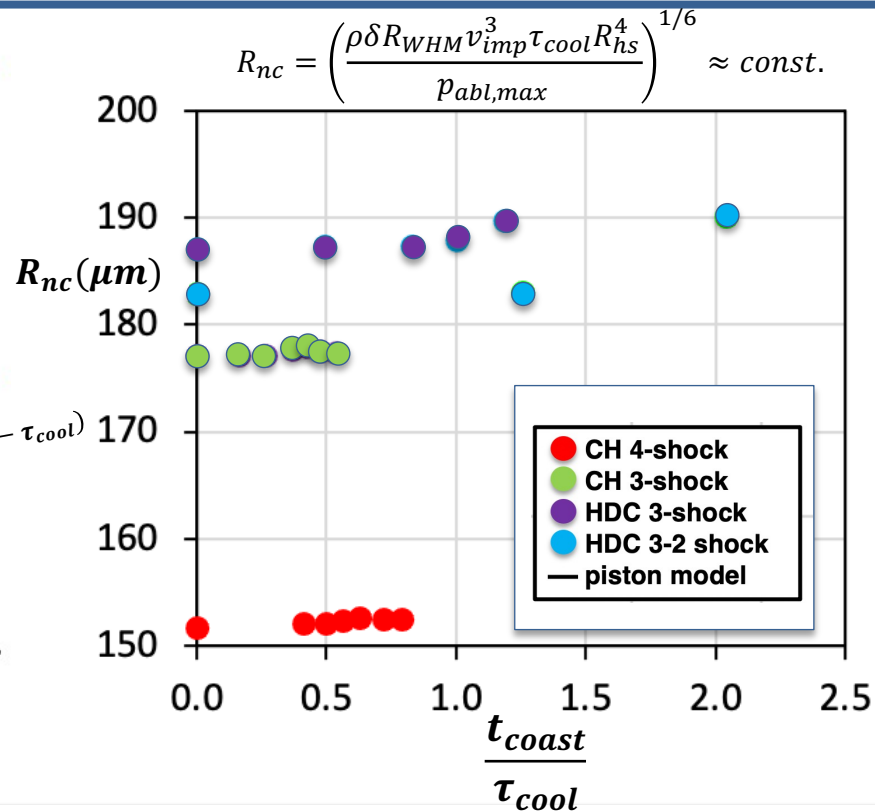
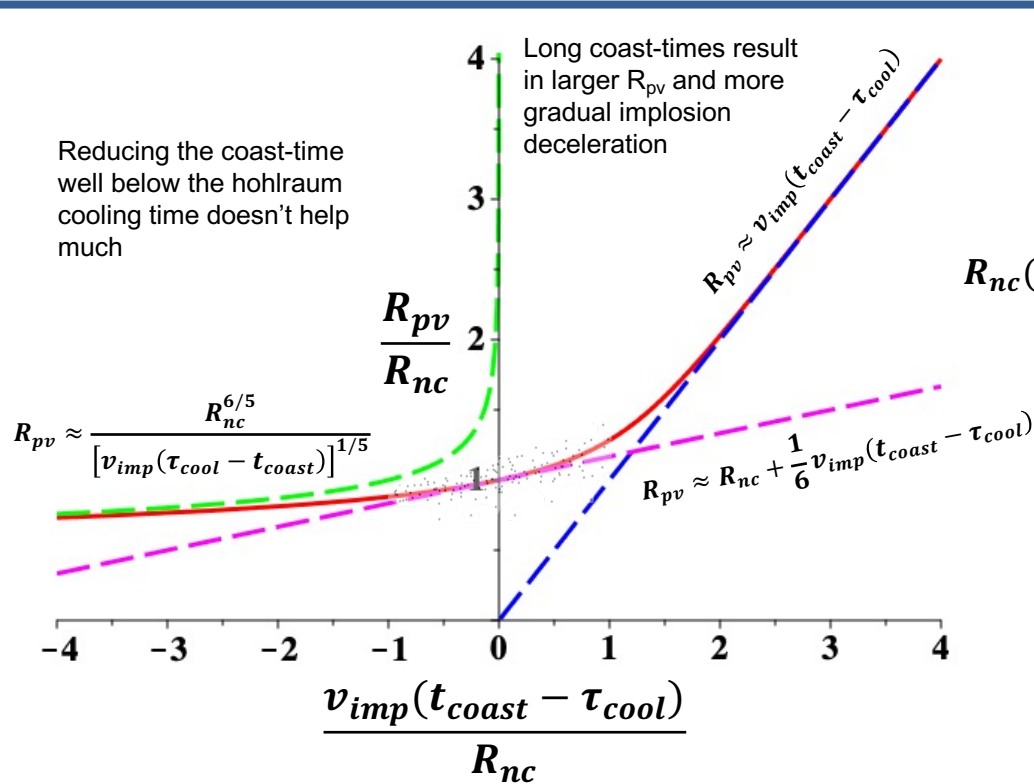
Now eliminate  $p_{pv}$  and  $t_{pv}$  noting that  $t_{coast} = t_{BT} - t_{peak}$  and we get the following:

$$R_{pv}^6 - v_{imp} (t_{coast} - \tau_{cool}) R_{pv}^5 - \frac{\rho \delta R_{WHM} v_{imp}^3 \tau_{cool} R_{hs}^4}{p_{abl,max}} = 0$$

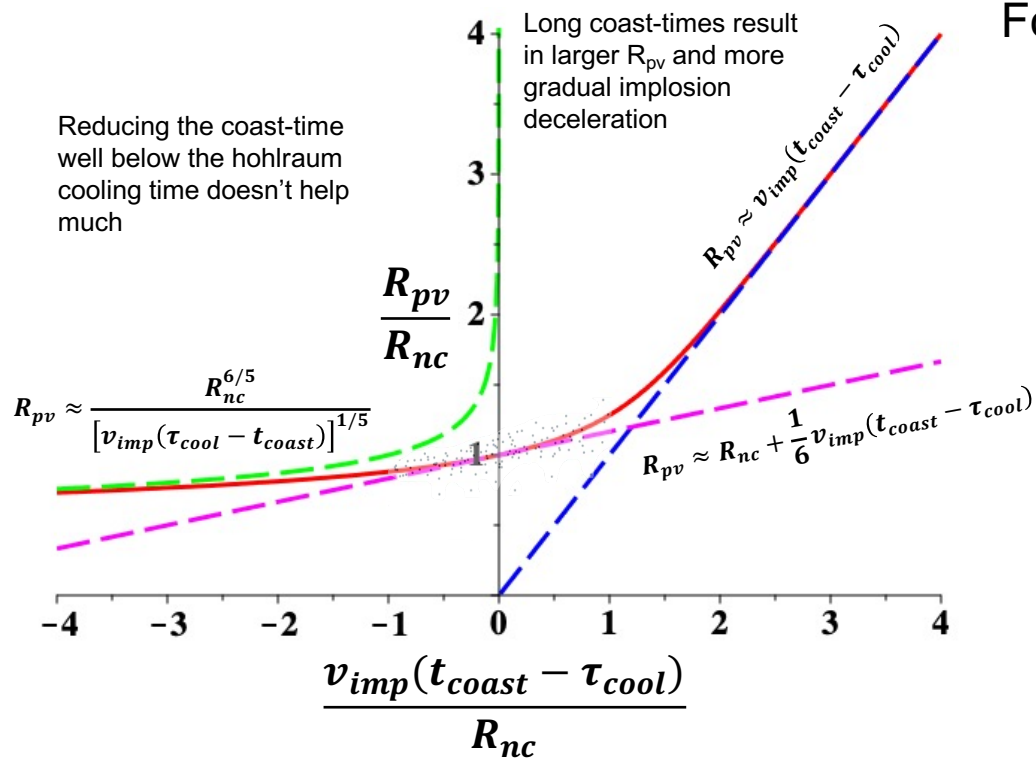
# So, what reducing coast-time does is it reduces the radius at which peak kinetic energy is obtained, forcing the implosion to decelerate more aggressively



# The no-coast radius ( $R_{nc}$ ) is the minimum $R_{pv}$ possible for a given design



# Decelerating harder, forces a more rapid transfer of kinetic energy into internal energy and this also reduces the time over which the hot-spot can cool



Forces implosion to slam on the brakes!  
("late apex" in racing)



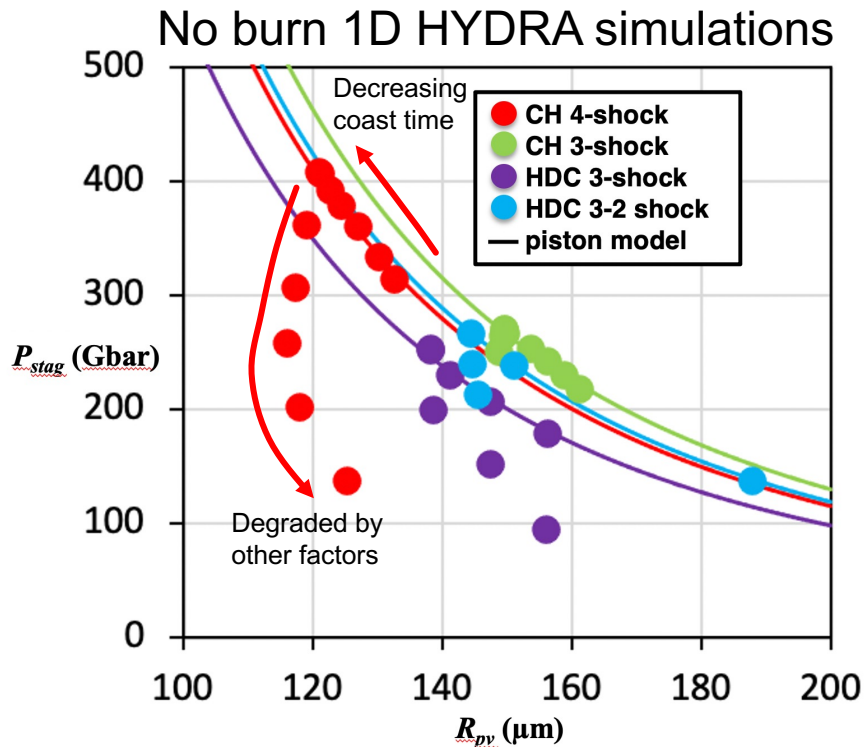
Less time for the heat to escape

$$R_{hs} T_{hs}^{7/2} \sim \frac{m_{shell} v_{imp}^2}{\tau_{decel}}$$

Compression in accelerated frame

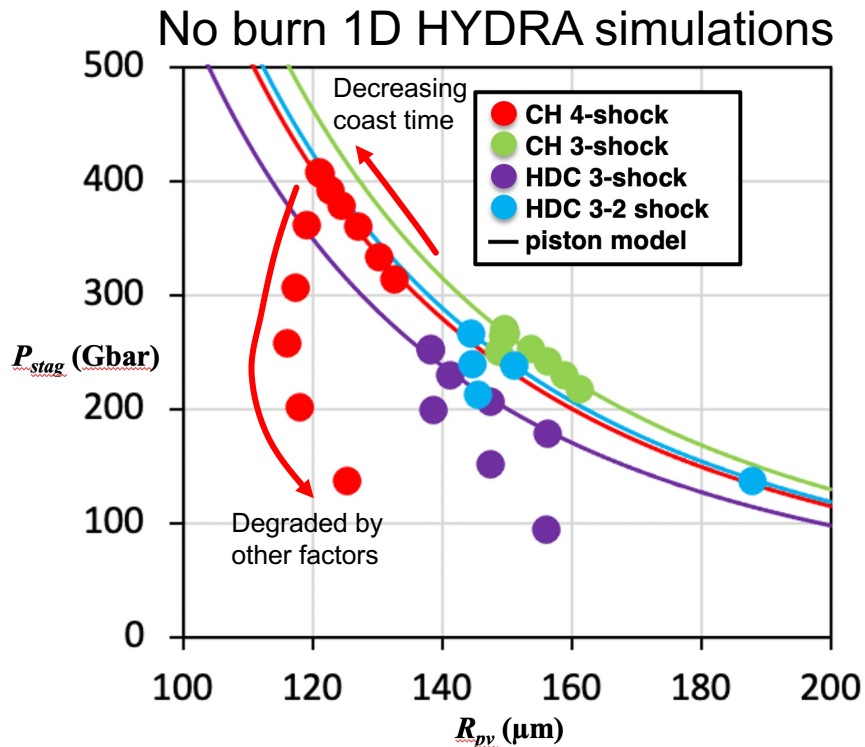
$$g_{eff} = \frac{v_{imp}^2}{R_{pv}}$$

# Stagnation pressure increases with reduced coast-time because the radius of peak velocity is decreasing



A high adiabat design can be made to act more like a low adiabat design by reducing  $R_{pv}$  and visa-versa

# Stagnation pressure increases with reduced coast-time because the radius of peak velocity is decreasing



Many hot-spot properties are linked to  $R_{pv}$ :

$$P_{stag} \sim \frac{1}{R_{pv}^{5/2}}$$

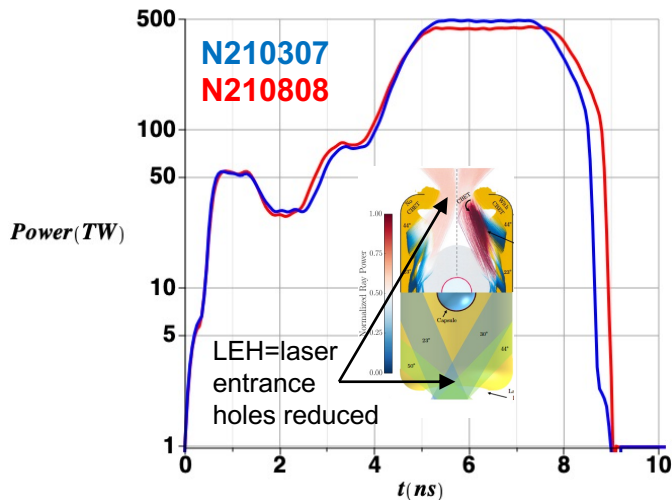
$$R_{hs} \sim \sqrt{R_{pv}}$$

$$P_{stag}^2 E_{hs} \sim \frac{1}{R_{pv}^6}$$

A high adiabat design can be made to act more like a low adiabat design by reducing  $R_{pv}$  and visa-versa



# Part of the Hybrid-E strategy<sup>+</sup> and design<sup>\*</sup> was to again leverage the tactic of reducing coast-time

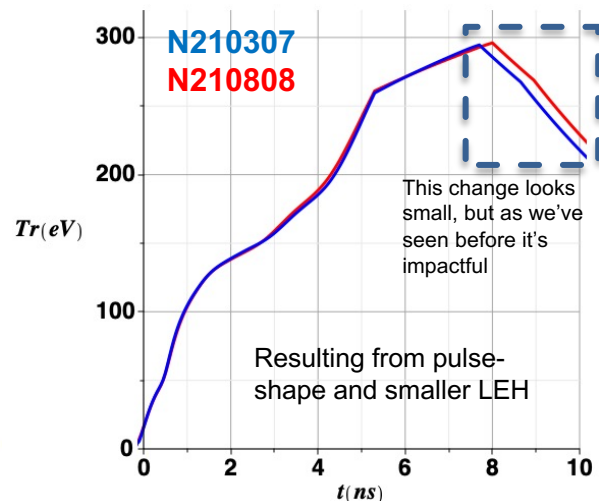
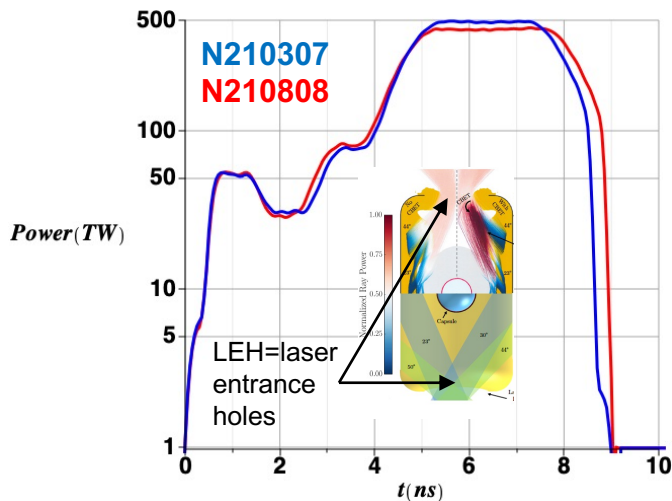


<sup>+</sup>O. Hurricane et al, APS-DPP, PO7.00001 (2017);  
PPCF 61, 014033 (2019); PoP 26, 052704 (2019);

<sup>\*</sup>A.B. Zylstra et al., PRL 126, 025001 (2021);

<sup>\*</sup>A.L. Kritcher et al., PoP 28, 072706 (2021)

# In the case of N210808 both a pulse-shape change and a laser entrance hole change resulted in an increased late time $T_{rad}$



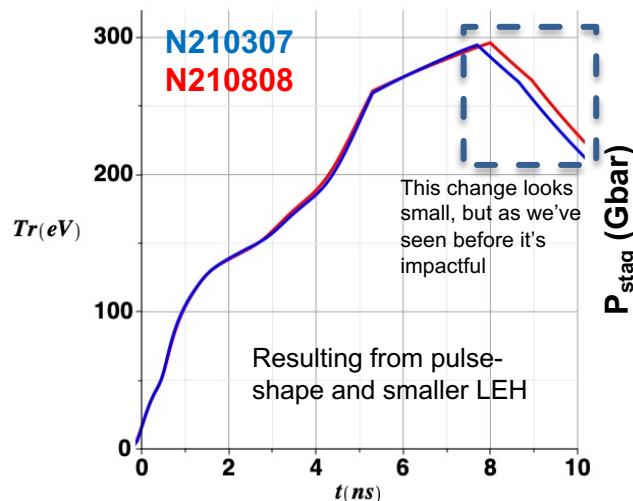
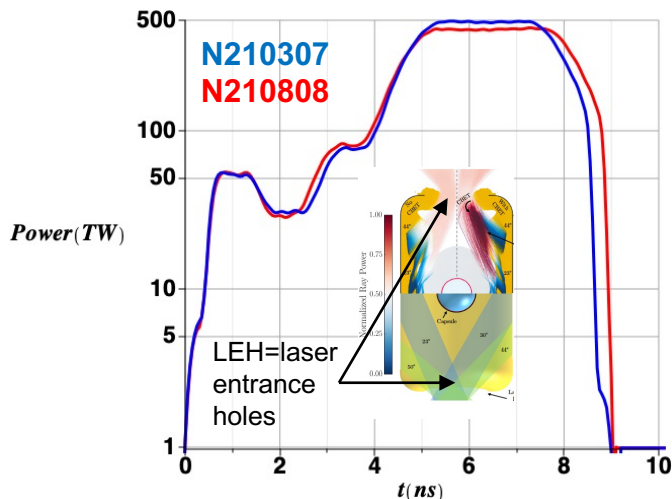
**N210808**  $R_{pv}$  reduced **30  $\mu\text{m}$**  from **N210307** which was **235  $\mu\text{m}$**

See J. Ralph talk GO04.00003 on reduced hohlraum cooling with reduced LEH

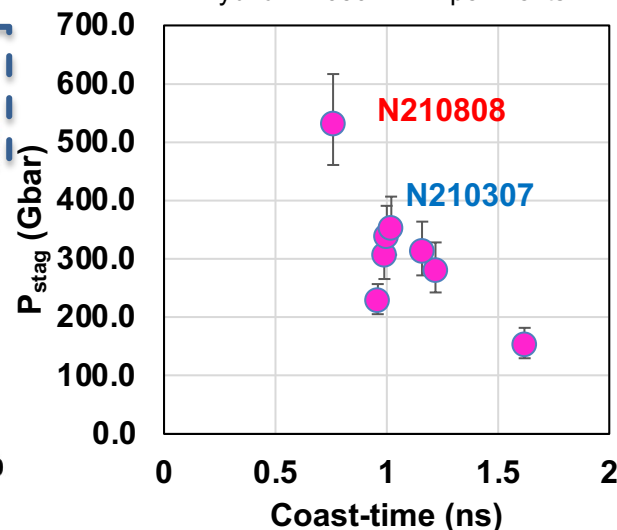
\*O. Hurricane et al, APS-DPP, PO7.00001 (2017);  
 PPCF 61, 014033 (2019); PoP 26, 052704 (2019);  
 \*A.B. Zylstra et al., PRL 126, 025001 (2021);  
 \*A.L. Kritcher et al., PoP 28, 072706 (2021)

\*see talks by A. Zylstra ZI02.00003; A. Kritcher GO04.00002

# As seen before, hot spot pressure improved, but this time we finally got to the ignition tipping-point



Hybrid-E 1050 DT Experiments

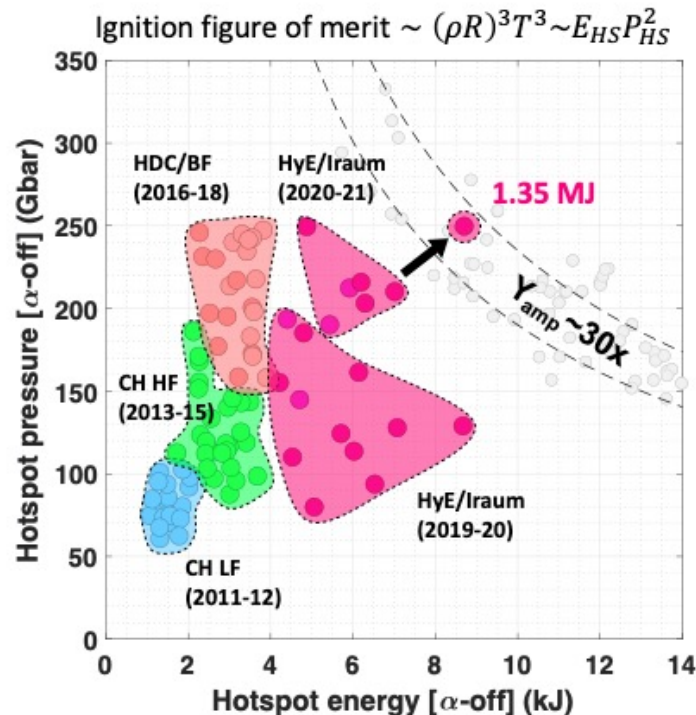


Reduced  $R_{pv}$  of 15% resulted in a 1.4x increase in pressure (no- $\alpha$ ) and a 2x increase  $P^2E$  (no- $\alpha$ )

\*O. Hurricane et al, APS-DPP, PO7.00001 (2017);  
 PPCF 61, 014033 (2019); PoP 26, 052704 (2019);  
 \*A.B. Zylstra et al., PRL 126, 025001 (2021);  
 \*A.L. Kritcher et al., PoP 28, 072706 (2021)

# Reducing coast-time is an obscure but valuable tactic for increasing indirect-drive implosion performance

- All yield record setting DT experiments on NIF have been those with low-coast time, except for the NIC implosions which mixed
- Coast-time, hohlraum cooling-rate, and the radius at which the implosion achieves its peak velocity ( $R_{pv}$ ) are related
- The fundamental parameter behind coast-time is  $R_{pv}$  and many hot-spot properties have a strong dependence upon it
- Improvements in target quality allowed us to leverage the advantage of low coast for the ignition level shot N210808 by reducing  $R_{pv}$  by 15% as compared to N210307 (see talks by Annie Kritcher, et al. GO04.00002 & Alex Zylstra, et al. ZI02.00003)
- More tests isolating coast-time vs. capsule quality are planned
- Understanding of coast-time physics implies that a hotter hohlraum would be very beneficial in general (see talk CO04.00006 by Dan Casey, et al.)



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